

# Mathematics Bookmarks 

 Standards Reference to Support Planning and Instruction

## 2nd Grade

## Tulare Cǒunty Office of Education

Tim A. Hire, County Superintendent of Schools


## Mathematics Bookmarks

Standards Reference to Support Planning and Instruction


## 2nd Grade

## Tulare Cóunty Office of Education

## Grade-Level Introduction

In Grade 2, instructional time should focus on four critical areas: (1) extending understanding of base-ten notation; (2) building fluency with addition and subtraction; (3) using standard units of measure; and (4) describing and analyzing shapes.
(1) Students extend their understanding of the base-ten system. This includes ideas of counting in fives, tens, and multiples of hundreds, tens, and ones, as well as number relationships involving these units, including comparing. Students understand multi-digit numbers (up to 1000) written in base-ten notation, recognizing that the digits in each place represent amounts of thousands, hundreds, tens, or ones (e.g., 853 is 8 hundreds +5 tens +3 ones).
(2) Students use their understanding of addition to develop fluency with addition and subtraction within 100 . They solve problems within 1000 by applying their understanding of models for addition and subtraction, and they develop, discuss, and use efficient, accurate, and generalizable methods to compute sums and differences of whole numbers in base-ten notation, using their understanding of place value and the properties of operations. They select and accurately apply methods that are appropriate for the context and the numbers involved to mentally calculate sums and differences for numbers with only tens or only hundreds.
(3) Students recognize the need for standard units of measure (centimeter and inch) and they use rulers and other measurement tools with the understanding that linear measure involves an iteration of units. They recognize that the smaller the unit, the more iterations they need to cover a given length.
(4) Students describe and analyze shapes by examining their sides and angles. Students investigate, describe, and reason about decomposing and combining shapes to make other shapes. Through building, drawing, and analyzing two- and three-dimensional shapes, students develop a foundation for understanding area, volume, congruence, similarity, and symmetry in later grades.

## Grade-Level Introduction

In Grade 2, instructional time should focus on four critical areas: (1) extending understanding of base-ten notation; (2) building fluency with addition and subtraction; (3) using standard units of measure; and (4) describing and analyzing shapes.
(1) Students extend their understanding of the base-ten system. This includes ideas of counting in fives, tens, and multiples of hundreds, tens, and ones, as well as number relationships involving these units, including comparing. Students understand multi-digit numbers (up to 1000) written in base-ten notation, recognizing that the digits in each place represent amounts of thousands, hundreds, tens, or ones (e.g., 853 is 8 hundreds +5 tens +3 ones).
(2) Students use their understanding of addition to develop fluency with addition and subtraction within 100 . They solve problems within 1000 by applying their understanding of models for addition and subtraction, and they develop, discuss, and use efficient, accurate, and generalizable methods to compute sums and differences of whole numbers in base-ten notation, using their understanding of place value and the properties of operations. They select and accurately apply methods that are appropriate for the context and the numbers involved to mentally calculate sums and differences for numbers with only tens or only hundreds.
(3) Students recognize the need for standard units of measure (centimeter and inch) and they use rulers and other measurement tools with the understanding that linear measure involves an iteration of units. They recognize that the smaller the unit, the more iterations they need to cover a given length.
(4) Students describe and analyze shapes by examining their sides and angles. Students investigate, describe, and reason about decomposing and combining shapes to make other shapes. Through building, drawing, and analyzing two- and three-dimensional shapes, students develop a foundation for understanding area, volume, congruence, similarity, and symmetry in later grades.

| FLUENCY |
| :--- |
| In kindergarten through grade six there are individual content <br> standards that set expectations for fluency with computations <br> using the standard algorithm (e.g., "fluently"" multiply multi- <br> digit whole numbers using the standard algorithm <br> (5.NBT.5 © ). Such standards are culminations of <br> progresions of learning, often spanning several grades, <br> involving conceptual understanding (such as reasoning about <br> quantities, the base-ten system, and properties of operations), <br> thoughtful practice, and extra support where necessary. <br> The word "fluent" is used in the standards to mean <br> "reasonably fast and accurate" and the ability to use certain <br> facts and procedures with enough facility that using them <br> does not slow down or derail the problem solver as he or she <br> works on more complex problems. Procedural fluency <br> requires skill in carrying out procedures flexibly, accurately, <br> efficiently, and appropriately. Developing fluency in each <br> grade can involve a mixture of just knowing some answers, <br> knowing some answers from patterns, and knowing some <br> answers from the use of strategies. |

Explanations of Major, Additional and Supporting ClusterLevel Emphases
Major3 [m] clusters - areas of intensive focus where students need fluent understanding and application of the core concepts. These clusters require greater emphasis than the others based on the depth of the ideas, the time that they take to master, and/or their importance to future mathematics or the demands of college and career readiness. The $\boldsymbol{\Delta}$ symbol will indicate standards in a Major Cluster in the narrative.
Additional [a] clusters - expose students to other subjects; may not connect tightly or explicitly to the major work of the grade
Supporting [s] clusters - rethinking and linking; areas where some material is being covered, but in a way that applies core understanding; designed to support and strengthen areas of major emphasis.
*A Note of Caution: Neglecting material will leave gaps in students' skills and understanding and will leave students unprepared for the challenges of a later grade.

California Mathematics Framework, adopted by the California State Board of Education November 6, 2013, http://www.cde.ca.gov/ci/ma/cf/draft2mathfwchapters.a sp

## FLUENCY

In kindergarten through grade six there are individual content standards that set expectations for fluency with computations using the standard algorithm (e.g., "fluently" multiply multidigit whole numbers using the standard algorithm (5.NBT.5 © ). Such standards are culminations of progressions of learning, often spanning several grades, involving conceptual understanding (such as reasoning about quantities, the base-ten system, and properties of operations), thoughtful practice, and extra support where necessary.
The word "fluent" is used in the standards to mean "reasonably fast and accurate" and the ability to use certain facts and procedures with enough facility that using them does not slow down or derail the problem solver as he or she works on more complex problems. Procedural fluency requires skill in carrying out procedures flexibly, accurately, efficiently, and appropriately. Developing fluency in each grade can involve a mixture of just knowing some answers, knowing some answers from patterns, and knowing some answers from the use of strategies.

Explanations of Major, Additional and Supporting ClusterLevel Emphases
Major3 [m] clusters - areas of intensive focus where students need fluent understanding and application of the core concepts. These clusters require greater emphasis than the others based on the depth of the ideas, the time that they take to master, and/or their importance to future mathematics or the demands of college and career readiness. The $\mathbf{\Delta}$ symbol will indicate standards in a Major Cluster in the narrative.
Additional [a] clusters - expose students to other subjects; may not connect tightly or explicitly to the major work of the grade
Supporting [s] clusters - rethinking and linking; areas where some material is being covered, but in a way that applies core understanding; designed to support and strengthen areas of major emphasis.
*A Note of Caution: Neglecting material will leave gaps in students' skills and understanding and will leave students unprepared for the challenges of a later grade.

California Mathematics Framework, adopted by the California State Board of Education November 6, 2013, http://www.cde.ca.gov/ci/ma/cf/draft2mathfwchapters.a sp

## Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

## Mathematical Practices

## 1. Make sense of problems and persevere in solving

them. Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

In second grade, students realize that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. They may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, "Does this make sense?" They make conjectures about the solution and plan out a problem-solving approach.

| Students: | Teachers: |
| :---: | :---: |
| - Analyze and explain the meaning of the problem <br> - Actively engage in problem solving (Develop, carry out, and refine a plan) <br> - Show patience and positive attitudes <br> - Ask if their answers make sense <br> - Check their answers with a different method | - Pose rich problems and/or ask open ended questions <br> - Provide wait-time for processing/finding solutions <br> - Circulate to pose probing questions and monitor student progress <br> - Provide opportunities and time for cooperative problem solving and reciprocal teaching |

## Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

## Mathematical Practices

1. Make sense of problems and persevere in solving them. Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

In second grade, students realize that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. They may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, "Does this make sense?" They make conjectures about the solution and plan out a problem-solving approach.

| Students: | Teachers: |
| :---: | :---: |
| - Analyze and explain the meaning of the problem | - Pose rich problems and/or ask open ended questions |
| - Actively engage in problem solving (Develop, carry out, and refine a plan) | - Provide wait-time for processing/finding solutions <br> - Circulate to pose probing |
| - Show patience and positive attitudes | questions and monitor student progress |
| - Ask if their answers make sense | - Provide opportunities and time for cooperative problem |
| - Check their answers with a different method | solving and reciprocal teaching |

2. Reason abstractly and quantitatively. Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to decontextualize - to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents-and the ability to contextualize, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects.

Younger students recognize that a number represents a specific quantity. They connect the quantity to written symbols. Quantitative reasoning entails creating a representation of a problem while attending to the meanings of the quantities. Second graders begin to know and use different properties of operations and relate addition and subtraction to length.

| Students: | Teachers: |
| :---: | :---: |
| - Represent a problem with symbols <br> - Explain their thinking <br> - Use numbers flexibly by applying properties of operations and place value <br> - Examine the reasonableness of their answers/calculations | - Ask students to explain their thinking regardless of accuracy <br> - Highlight flexible use of numbers <br> - Facilitate discussion through guided questions and representations <br> - Accept varied solutions/representations |

2. Reason abstractly and quantitatively. Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to decontextualize - to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents-and the ability to contextualize, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects.

Younger students recognize that a number represents a specific quantity. They connect the quantity to written symbols. Quantitative reasoning entails creating a representation of a problem while attending to the meanings of the quantities. Second graders begin to know and use different properties of operations and relate addition and subtraction to length.

| Students: | Teachers: |
| :---: | :---: |
| - Represent a problem with symbols <br> - Explain their thinking <br> - Use numbers flexibly by applying properties of operations and place value <br> - Examine the reasonableness of their answers/calculations | - Ask students to explain their thinking regardless of accuracy <br> - Highlight flexible use of numbers <br> - Facilitate discussion through guided questions and representations <br> - Accept varied solutions/representations |

## 3. Construct viable arguments and critique the

reasoning of others. Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and-if there is a flaw in an argument-explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments. Students build proofs by induction and proofs by contradiction. CA 3.1 (for higher mathematics only).

Second graders may construct arguments using concrete referents, such as objects, pictures, drawings, and actions. They practice their mathematical communication skills as they participate in mathematical discussions involving questions like "How did you get that?", "Explain your thinking," and "Why is that true?" They not only explain their own thinking, but listen to others' explanations. They decide if the explanations make sense and ask appropriate questions.

| Students: | Teachers: |
| :---: | :---: |
| - Make reasonable guesses to explore their ideas <br> - Justify solutions and approaches <br> - Listen to the reasoning of others, compare arguments, and decide if the arguments of others makes sense <br> - Ask clarifying and probing questions | - Provide opportunities for students to listen to or read the conclusions and arguments of others <br> - Establish and facilitate a safe environment for discussion <br> - Ask clarifying and probing questions <br> - Avoid giving too much assistance (e.g., providing answers or procedures) |

3. Construct viable arguments and critique the
reasoning of others. Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and-if there is a flaw in an argument-explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments. Students build proofs by induction and proofs by contradiction. CA 3.1 (for higher mathematics only).
Second graders may construct arguments using concrete referents, such as objects, pictures, drawings, and actions. They practice their mathematical communication skills as they participate in mathematical discussions involving questions like "How did you get that?", "Explain your thinking," and "Why is that true?" They not only explain their own thinking, but listen to others' explanations. They decide if the explanations make sense and ask appropriate questions.

| Students: | Teachers: |
| :---: | :---: |
| - Make reasonable guesses to explore their ideas <br> - Justify solutions and approaches <br> - Listen to the reasoning of others, compare arguments, and decide if the arguments of others makes sense <br> - Ask clarifying and probing questions | - Provide opportunities for students to listen to or read the conclusions and arguments of others <br> - Establish and facilitate a safe environment for discussion <br> - Ask clarifying and probing questions <br> - Avoid giving too much assistance (e.g., providing answers or procedures) |

4. Model with mathematics. Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, twoway tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.
In early grades, students experiment with representing problem situations in multiple ways including numbers, words (mathematical language), drawing pictures, using objects, acting out, making a chart or list, creating equations, etc. Students need opportunities to connect the different representations and explain the connections. They should be able to use all of these representations as needed.

| Students: | Teachers: |
| :---: | :---: |
| - Make reasonable guesses to explore their ideas <br> - Justify solutions and approaches <br> - Listen to the reasoning of others, compare arguments, and decide if the arguments of others makes sense <br> - Ask clarifying questions | - Allow time for the process to take place (model, make graphs, etc.) <br> - Model desired behaviors (think alouds) and thought processes (questioning, revision, reflection/written) <br> - Make appropriate tools available <br> - Create an emotionally safe environment where risk taking is valued <br> - Provide meaningful, real world, authentic, performance-based tasks (non traditional work problems) |

4. Model with mathematics. Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.
In early grades, students experiment with representing problem situations in multiple ways including numbers, words (mathematical language), drawing pictures, using objects, acting out, making a chart or list, creating equations, etc. Students need opportunities to connect the different representations and explain the connections. They should be able to use all of these representations as needed.

| Students: | Teachers: |
| :---: | :---: |
| - Make reasonable guesses to explore their ideas <br> - Justify solutions and approaches <br> - Listen to the reasoning of others, compare arguments, and decide if the arguments of others makes sense <br> - Ask clarifying questions | - Allow time for the process to take place (model, make graphs, etc.) <br> - Model desired behaviors (think alouds) and thought processes (questioning, revision, reflection/written) <br> - Make appropriate tools available <br> - Create an emotionally safe environment where risk taking is valued <br> - Provide meaningful, real world, authentic, performance-based tasks (non traditional work problems) |

5. Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.
In second grade, students consider the available tools (including estimation) when solving a mathematical problem and decide when certain tools might be better suited. For instance, second graders may decide to solve a problem by drawing a picture rather than writing an equation.

| Students: | Teachers: |
| :---: | :---: |
| - Select and use tools strategically (and flexibly) to visualize, explore, and compare information <br> - Use technological tools and resources to solve problems and deepen understanding | - Make appropriate tools available for learning (calculators, concrete models, digital resources, pencil/paper, compass, protractor, etc.) <br> - Use tools with their instruction |

5. Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.
In second grade, students consider the available tools (including estimation) when solving a mathematical problem and decide when certain tools might be better suited. For instance, second graders may decide to solve a problem by drawing a picture rather than writing an equation.

| Students: | Teachers: |
| :---: | :---: |
| - Select and use tools strategically (and flexibly) to visualize, explore, and compare information <br> - Use technological tools and resources to solve problems and deepen understanding | - Make appropriate tools available for learning (calculators, concrete models, digital resources, pencil/paper, compass, protractor, etc.) <br> - Use tools with their instruction |

6. Attend to precision. Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

As children begin to develop their mathematical communication skills, they try to use clear and precise language in their discussions with others and when they explain their own reasoning.

| Students: | Teachers: |
| :---: | :---: |
| - Calculate accurately and efficiently <br> - Explain their thinking using mathematics vocabulary <br> - Use appropriate symbols and specify units of measure | - Recognize and model efficient strategies for computation <br> - Use (and challenging students to use) mathematics vocabulary precisely and consistently |

7. Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see 7 x 8 equals the well-remembered $7 \times 5+7 \times 3$, in preparation for learning about the distributive property. In the expression $x^{2}+9 x+14$, older students can see the 14 as $2 \times 7$ and the 9 as $2+7$. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see $5-3(x-$ $y)^{2}$ as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers $x$ and $y$.

Second graders look for patterns. For instance, they adopt mental math strategies based on patterns (making ten, fact families, doubles).

| Students: | Teachers: |
| :--- | :--- |
| •Look for, develop, and <br> generalize relationships <br> and patterns | •Provide time for applying <br> and discussing properties <br> - Apply reasonable <br> thoughts about patterns <br> and properties to new <br> situations |
| •Ask questions about the <br> application of patterns |  |
| Highlight different <br> approaches for solving <br> problems |  |

## 7. Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see 7 x 8 equals the well-remembered $7 \times 5+7 \times 3$, in preparation for learning about the distributive property. In the expression $x^{2}+9 x+14$, older students can see the 14 as $2 \times 7$ and the 9 as $2+7$. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see $5-3(x-$ $y)^{2}$ as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers $x$ and $y$.

Second graders look for patterns. For instance, they adopt mental math strategies based on patterns (making ten, fact families, doubles).

| Students: | Teachers: |
| :--- | :--- |
| -Look for, develop, and <br> generalize relationships <br> and patterns | •Provide time for applying <br> and discussing properties |
| Apply reasonable <br> thoughts about patterns <br> and properties to new <br> situations | Ask questions about the <br> application of patterns |
| •Highlight different <br> approaches for solving <br> problems |  |

8. Look for and express regularity in repeated
reasoning. Mathematically proficient students notice if calculations are repeated, and look both for general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they repeatedly check whether points are on the line through $(1,2)$ with slope 3 , middle school students might abstract the equation $(y-2) /(x-1)=$ 3. Noticing the regularity in the way terms cancel when expanding $(x-1)(x+1),(x-1)\left(x^{2}+x+1\right)$, and $(x-1)\left(x^{3}+x^{2}+x+1\right)$ might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.

In second grade, Students notice repetitive actions in counting and computation, etc. When children have multiple opportunities to add and subtract, they look for shortcuts, such as rounding up and then adjusting the answer to compensate for the rounding. Students continually check their work by asking themselves, "Does this make sense?"

| Students: | Teachers: |
| :--- | :--- | :--- |
| -Look for methods and <br> shortcuts in patterns <br> and repeated <br> calculations <br> -Evaluate the <br> reasonableness of <br> results and solutions$\quad$Provide tasks and <br> problems with patterns |  |

8. Look for and express regularity in repeated reasoning. Mathematically proficient students notice if calculations are repeated, and look both for general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they repeatedly check whether points are on the line through $(1,2)$ with slope 3 , middle school students might abstract the equation $(y-2) /(x-1)=3$. Noticing the regularity in the way terms cancel when expanding $(x-1)(x+$ 1), $(x-1)\left(x^{2}+x+1\right)$, and $(x-1)\left(x^{3}+x^{2}+x+1\right)$ might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.

In second grade, Students notice repetitive actions in counting and computation, etc. When children have multiple opportunities to add and subtract, they look for shortcuts, such as rounding up and then adjusting the answer to compensate for the rounding. Students continually check their work by asking themselves, "Does this make sense?"

| Students: | Teachers: |
| :--- | :--- |
| -Look for methods and <br> shortcuts in patterns <br> and repeated <br> calculations | -Provide tasks and <br> problems with patterns <br> - Evaluate the <br> reasonableness of <br> results and solutions |
|  | -Ask about possible <br> answers before, and <br> reasonableness after <br> computations |

## Grade 2 Overview

Operations and Algebraic Thinking

- Represent and solve problems involving addition and subtraction.
- Add and subtract within 20.
- Work with equal groups of objects to gain foundations for multiplication.

Number and Operations in Base Ten

- Understand place value.
- Use place value understanding and properties of operations to add and subtract.

Measurement and Data

- Measure and estimate lengths in standard units.
- Relate addition and subtraction to length.
- Work with time and money.
- Represent and interpret data.


## Geometry

- Reason with shapes and their attributes.


## Grade 2 Overview

Operations and Algebraic Thinking

- Represent and solve problems involving addition and subtraction.
- Add and subtract within 20.
- Work with equal groups of objects to gain foundations for multiplication.

Number and Operations in Base Ten

- Understand place value.
- Use place value understanding and properties of operations to add and subtract.

Measurement and Data

- Measure and estimate lengths in standard units.
- Relate addition and subtraction to length.
- Work with time and money.
- Represent and interpret data.

Geometry

- Reason with shapes and their attributes.


## CCSS Where to Focus Grade 2 Mathematics

Not all of the content in a given grade is emphasized equally in the Standards. Some clusters require greater emphasis than others based on the depth of the ideas, the time that they take to master, and/or their importance to future mathematics or the demands of college and career readiness. More time in these areas is also necessary for students to meet the Standards for Mathematical Practice.

To say that some things have a greater emphasis is not to say that anything in the standards can be safely neglected in instruction. Neglecting material will leave gaps in student skill and understanding and may leave students unprepared for the challenges of a later grade.

| MAJOR, SUPPORTING, AND ADDITIONAL CLUSTERS FOR GRADE 2 <br> Emphases are given at the cluster level. Refer to the Common Core State Standards for Mathematics for the specific standards that fall within each cluster. |  |  |
| :---: | :---: | :---: |
| Key: - Major Clusters | -Supporting Clusters | Additional Clusters |



## REQUIRED FLUENCIES FOR GRADE 2

| 2.OA.B.2 | Single-digit sums and differences (sums from <br> memory by end of Grade 2) |
| :--- | :--- |
| 2.NBT.B.5 | Add/subtract within 100 |

Student Achievement Partners, Achieve the Core http://achievethecore.org/, Focus by Grade Level, http://achievethecore.org/dashboard/300/search/1/2/0/1/2 /3/4/5/6/7/8/9/10/11/12/page/774/focus-by-grade-level

## CCSS Where to Focus Grade 2 Mathematics

Not all of the content in a given grade is emphasized equally in the Standards. Some clusters require greater emphasis than others based on the depth of the ideas, the time that they take to master, and/or their importance to future mathematics or the demands of college and career readiness. More time in these areas is also necessary for students to meet the Standards for Mathematical Practice.

To say that some things have a greater emphasis is not to say that anything in the standards can be safely neglected in instruction. Neglecting material will leave gaps in student skill and understanding and may leave students unprepared for the challenges of a later grade.

```
MAJOR, SUPPORTING, AND ADDITIONAL CLUSTERS FOR GRADE 2
Emphasessare given at the cluster level.Refer to the Common Core State Standards for Mathematics for the
```



```
Key: Major Clusters पSupporting Clusters Additional Clusters
```



## REQUIRED FLUENCIES FOR GRADE 2

| 2.OA.B.2 | Single-digit sums and differences (sums from <br> memory by end of Grade 2) |
| :--- | :--- |
| 2.NBT.B.5 | Add/subtract within 100 |

Student Achievement Partners, Achieve the Core http://achievethecore.org/, Focus by Grade Level, http://achievethecore.org/dashboard/300/search/1/2/0/1/2 /3/4/5/6/7/8/9/10/11/12/page/774/focus-by-grade-level

## 2.OA.A Represent and solve problems involving addition and subtraction.

2.OA. 1 Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

## Essential Skills and Concepts:

$\square$ Adding and subtract within 100
$\square$ Read and understand word problems
$\square$ Solve word problems

- Solve for unknowns in all positions
$\square$ Represent word problems using visual representations


## Question Stems and Prompts:

$\checkmark$ Summarize the story problem and tell it to your partner in your own words.
$\checkmark$ Draw an illustration for the word problem. What do the parts of your drawing mean? How do you know?
$\checkmark$ Are we trying to find the total, a part, or are we comparing?
$\checkmark$ Does your answer make sense?
$\checkmark$ What does your answer tell us about the story/word problem?

## Vocabulary

Tier 2

- solve
- symbol
- illustration/drawing

Tier 3

- equation
- addition
- subtraction


## Spanish Cognates

resolver
símbolo
ilustración
ecuación
adición
sustracción

## Standards Connections

2.OA.1 - 2.MD.5, 2.MD.8, 2.MD. 10

## 2.OA. 1 Examples:

 Name 2.OA.1Josh won 14 tokens from a game. He won 29 takens from a second game. After the second game, he used 21 tokens for a prize. How many tokens did he have left?

There were 71 books on a shelf in the media center at the start of the day. 26 books were checked out in the morning. 15 books were checked out in the afternoon. How many books were left on the shelf at the end of the day?

Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.NBT. 4

## 2.OA.A Represent and solve problems involving addition and subtraction.

2.OA. 1 Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

## Essential Skills and Concepts:

$\square$ Adding and subtract within 100
$\square$ Read and understand word problems
$\square$ Solve word problems
$\square$ Solve for unknowns in all positions
$\square$ Represent word problems using visual representations

## Question Stems and Prompts:

$\checkmark$ Summarize the story problem and tell it to your partner in your own words.
$\checkmark$ Draw an illustration for the word problem. What do the parts of your drawing mean? How do you know?
$\checkmark$ Are we trying to find the total, a part, or are we comparing?
$\checkmark$ Does your answer make sense?
$\checkmark$ What does your answer tell us about the story/word problem?

## Vocabulary

Tier 2

- solve
- symbol
- illustration/drawing

Tier 3

- equation
- addition
- subtraction


## Spanish Cognates

resolver símbolo ilustración
ecuación adición sustracción

## Standards Connections

2.OA.1-2.MD.5, 2.MD.8, 2.MD. 10

## 2.OA. 1 Examples:

Name
Josh won 14 tokens from a game. He won 29 tokens from a second game.
After the second game, he used 21 tokens for a prize. How many tokens
did he have left?
There were 71 books on a shelf in the media center at the start of the
day. 26 books were checked out in the morning. 15 books were checked
out in the afternoon. How many books were left on the shelf at the end
of the day?

Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.NBT. 4

## 2.OA.A. 1

## Standard Explanation

In grade two students add and subtract numbers within 100 in the context of one- and two-step word problems
(2.OA.1 $\mathbf{~ )}$ ) By second grade students have had prior experiences working with various problem situations (add to, take from, put together, take apart, and compare) with unknowns in all positions (result unknown, change unknown, and start unknown). Grade two students extend their work with addition and subtraction word problems in two major ways:

- They represent and solve problems of all types which involve addition and subtraction within 100 , building upon their previous work within 20, and
- They represent and solve two-step word problems of all types, extending their work with one-step word problems. (Adapted from Arizona 2012, N. Carolina 2013, Georgia Department of Education [Georgia] 2011, and the Kansas Association of Teachers of Mathematics [KATM] 2nd 122 FlipBook 2012)

For these more complex grade two problems, it is important for students to represent the problem situations with drawings and equations (2.OA. $1 \mathbf{4}$ ). Drawings can be shown more easily to the whole class during explanations and can be related to equations. Students can also use manipulatives (e.g., snap cubes, place-value blocks) but making drawings of quantities can be used anywhere to solve problems and support students in describing their strategies. Second grade students represent problems with equations and use boxes, blanks, or pictures for the unknown amount. For example, students can represent compare problems using "comparison bars" (e.g., a long bar above, a shorter bar below, followed by an oval for the difference or unknown amount, where the shorter bar plus the oval are the same length as the longer bar on top). Students can draw these bars and fill in numbers from the problem and label the bars.

One-step word problems use one operation. New at second grade are two-step word problems (2.OA.1 © ) that require students to complete two operations, which may include the same operation or opposite operations.

The following table has examples of easy and middledifficulty two-step word problems that would be appropriate.

| One-Step Word Problem One Operation | Two-Step Word Problem <br> Two Operations, Same | Two-Step Word Problem Two Operations, Opposite |
| :---: | :---: | :---: |
| There are 15 stickers on the page. Brittany put some more stickers on the page and now there are 22. How many stickers did Brittany put on the page? $\begin{aligned} & 15+\ldots=22 \\ & 22-15= \end{aligned}$ | There are 9 blue marbles and 6 red marbles in the bag. Maria put in 8 more marbles. How many marbles are in the bag now? $\begin{gathered} 9+6+8=\text { o } \\ (9+6)+8= \end{gathered}$ | There are 39 peas on the plate. Carlos ate 25 peas. Mother put 7 more peas on the plate. How many peas are on the plate now? $\begin{aligned} & 39-25+7=\text { or } \\ & (39-25)+7= \end{aligned}$ |

Second graders use a range of methods, often mastering more complex strategies such as making tens and doubles and near doubles that were introduced in grade one for problems involving single-digit addition and subtraction.
(CA Mathematics Framework, adopted Nov. 6, 2013)

## 2.OA.A. 1

## Standard Explanation

In grade two students add and subtract numbers within 100 in the context of one- and two-step word problems (2.OA.1 $\mathbf{\Delta}$ ). By second grade students have had prior experiences working with various problem situations (add to, take from, put together, take apart, and compare) with unknowns in all positions (result unknown, change unknown, and start unknown). Grade two students extend their work with addition and subtraction word problems in two major ways:

- They represent and solve problems of all types which involve addition and subtraction within 100 , building upon their previous work within 20, and
- They represent and solve two-step word problems of all types, extending their work with one-step word problems. (Adapted from Arizona 2012, N. Carolina 2013, Georgia Department of Education [Georgia] 2011, and the Kansas Association of Teachers of Mathematics [KATM] 2nd 122 FlipBook 2012)

For these more complex grade two problems, it is important for students to represent the problem situations with drawings and equations (2.OA.1 4). Drawings can be shown more easily to the whole class during explanations and can be related to equations. Students can also use manipulatives (e.g., snap cubes, place-value blocks) but making drawings of quantities can be used anywhere to solve problems and support students in describing their strategies. Second grade students represent problems with equations and use boxes, blanks, or pictures for the unknown amount. For example, students can represent compare problems using "comparison bars" (e.g., a long bar above, a shorter bar below, followed by an oval for the difference or unknown amount, where the shorter bar plus the oval are the same length as the longer bar on top). Students can draw these bars and fill in numbers from the problem and label the bars.

One-step word problems use one operation. New at second grade are two-step word problems (2.OA.1 $\mathbf{\Delta}$ ) that require students to complete two operations, which may include the same operation or opposite operations.

The following table has examples of easy and middledifficulty two-step word problems that would be appropriate.

| One-Step Word Problem One Operation | Two-Step Word Problem Two Operations, Same | Two-Step Word Problem Two Operations, Opposite |
| :---: | :---: | :---: |
| There are 15 stickers on the page. Brittany put some more stickers on the page and now there are 22. How many stickers did Brittany put on the page? $\begin{aligned} & 15+\ldots=22 \\ & 22-15= \end{aligned}$ | There are 9 blue marbles and 6 red marbles in the bag. Maria put in 8 more marbles. How many marbles are in the bag now? $\begin{aligned} & 9+6+8=\ldots \text { or } \\ & (9+6)+8= \end{aligned}$ | There are 39 peas on the plate. Carlos ate 25 peas. Mother put 7 more peas on the plate. How many peas are on the plate now? $\begin{aligned} & 39-25+7=\text { or } \\ & (39-25)+7= \end{aligned}$ |

Second graders use a range of methods, often mastering more complex strategies such as making tens and doubles and near doubles that were introduced in grade one for problems involving single-digit addition and subtraction.
(CA Mathematics Framework, adopted Nov. 6, 2013)

## 2.OA.B Add and subtract within 20.

2.OA. 2 Fluently add and subtract within 20 using mental strategies. ${ }^{2}$ By end of Grade 2, know from memory all sums of two one-digit numbers.

## Essential Skills and Concepts:

$\square \quad$ Use and explain a variety of strategies for adding and subtracting
$\square \quad$ Fluently add and subtract within 20
$\square$ Solve problems mentally and explain your thought process

## Question Stems and Prompts:

$\checkmark$ Add using two different strategies. Explain your thinking.
$\checkmark$ Subtract and explain your strategy.
$\checkmark$ What was your total? How do you know?
$\checkmark$ If you had ___ and subtracted $\qquad$ from it what would you have left over?
$\checkmark \quad$ What is the total (sum) when you add $\qquad$ and $\qquad$ ?

## Vocabulary

Tier 2

- fluently
- mental
- memory

Tier 3

- sum/total

Spanish Cognates

- digit


## Standards Connections <br> 2.OA. $2 \rightarrow 2 . N B T .5$

## Methods for Solving Addition and Subtraction Problems

```
To solve word problems, students learn to apply various computational methods. Kindergarten students generally use Level 1 methods and Level 2 and 3 methods are used in grades one and two.
```


## Methods used for solving single-digit addition and subtraction problems

```
Level 1: Direct Modeling by Counting All or Taking Away
Represent situation or numerical problem with groups of objects, a drawing, or fingers. Model the situation by composing two addend groups or decomposing a total group. Count the resulting total or addend.
Level 2: Counting On
Embed an addend within the total (the addend is perceived simultaneously as an addend and as part of the total). Count this total but abbreviate the counting by omitting the count of this addend; instead, begin with the number word of this addend. Some method of keeping track (fingers, objects, mentally imaged objects, body motions, other count words) is use to monitor the count.
Methods used to find the total or an addend, depending on what is monitored.
Level 3: Convert to an Easier Problem
Decompose an addend and compose a part with another addend.
Refer to Appendix F for additional information about methods used for solving single-digit addition and subtraction problems.
```

(Adapted from the University of Arizona Progressions Documents for the Common Core Math Standards [Progressions], K-5 CC and OA (pg. 12) 2011).

## 2.OA.B Add and subtract within 20.

2.OA. 2 Fluently add and subtract within 20 using mental strategies. ${ }^{2}$ By end of Grade 2, know from memory all sums of two one-digit numbers.

## Essential Skills and Concepts:

$\square$ Use and explain a variety of strategies for adding and subtracting
$\square \quad$ Fluently add and subtract within 20
$\square$ Solve problems mentally and explain your thought process

## Question Stems and Prompts:

$\checkmark$ Add using two different strategies. Explain your thinking.
$\checkmark$ Subtract and explain your strategy.
$\checkmark$ What was your total? How do you know?
$\checkmark$ If you had ___ and subtracted $\qquad$ from it what would you have left over?
$\checkmark \quad$ What is the total (sum) when you add $\qquad$ and $\qquad$ ?

## Vocabulary

## Spanish Cognates

Tier 2

- fluently
- mental
mental
- memory memoria

Tier 3

- sum/total suma/total
- digit dígito


## Standards Connections <br> 2.OA. $2 \rightarrow$ 2.NBT. 5

## Methods for Solving Addition and Subtraction Problems

To solve word problems, students learn to apply various computational methods. Kindergarten students generally use Level 1 methods and Level 2 and 3 methods are used in grades one and two.

## Methods used for solving single-digit addition and subtraction problems

Level 1: Direct Modeling by Counting All or Taking Away
Represent situation or numerical problem with groups of objects, a drawing, or fingers. Model the situation by composing two addend groups or decomposing a total group. Count the resulting total or addend.

Level 2: Counting On
Embed an addend within the total (the addend is perceived simultaneously as an addend and as part of the total). Count this total but abbreviate the counting by omitting the count of this addend; instead, begin with the number word of this addend. Some method of keeping track (fingers, objects, mentally imaged objects, body motions, other count words) is use to monitor the count.
Methods used to find the total or an addend, depending on what is monitored.
Level 3: Convert to an Easier Problem
Decompose an addend and compose a part with another addend.
Refer to Appendix F for additional information about methods used for solving single-digit addition and subtraction problems.
(Adapted from the University of Arizona Progressions Documents for the Common Core Math Standards [Progressions], K-5 CC and OA (pg. 12) 2011).

[^0]
## 2.OA.B. 2

## Standard Explanation

In grade two students extend their fluency with addition and subtraction from within 10 to within 20 (2.OA. $2 \mathbf{\Delta}$ ). The extended experiences students have had with addition and subtraction in kindergarten (within 5) and grade one (within 10) culminate in grade two students becoming fluent in single-digit additions and related subtractions using mental Level 2 and 3 methods and strategies as needed.

Building upon their work in First Grade, Second Graders use various addition and subtraction strategies in order to fluently add and subtract within 20. Second Graders internalize facts and develop fluency by using strategies often that make sense to them. When students are able to demonstrate fluency they are accurate, efficient, and flexible. Students must have efficient strategies in order to know sums from memory.

Students may still need to support the development of their fluency with math drawings when solving problems. Math drawings represent the number of objects counted (using dots and sticks) and do not need to represent the context of the problem. Thinking about numbers using frames of 10 or making drawings using 5 -groups and tens can be a helpful way to understand single-digit additions and subtractions. An example of interactive games students can play to develop counting and addition skills are available
at http://illuminations.nctm.org/ActivityDetail.aspx?ID=75 (National Council of Teachers of Mathematics [NCTM] Illuminations).

Mental strategies help students develop fluency as they make sense of number relationships while they add and subtract within 20. (CA Mathematics Framework, adopted Nov. 6, 2013)

Mental strategies

- Counting on
- Making tens $(9+7=(9+1)+6=10+6)$
- Decomposing a number leading to a ten ( $14-6=14-4-2=10-2=8$ )
- Fact families $(8+5=13$ and $13-8=5)$
- Doubles $(1+1,2+2,3+3$, etc.)
- Doubles plus one $(7+8=7+7+1)$

> - Relationship between addition and subtraction (e.g., knowing that $8+4=12$, one knows $12-8=4$ )
> - Equivalent but easier or known sums (e.g., adding $6+7$ by creating the known equivalent $6+6+1=12+1=13$ )
1.OA. 6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10 . Use strategies such as counting on; making ten (e.g., $8+6=8+2+4=10+4=14$ ); decomposing a number leading to a ten (e.g., $13-4=13-3-1=$ $10-1=9$ ); using the relationship between addition and subtraction (e.g., knowing that $8+4=12$, one knows $12-8=4$ ); and creating equivalent but easier or known sums (e.g., adding $6+$ 7 by creating the known equivalent $6+6+1=12+1=13$ ).

## 2.OA.B. 2

## Standard Explanation

In grade two students extend their fluency with addition and subtraction from within 10 to within 20 (2.OA. $2 \mathbf{\Delta}$ ). The extended experiences students have had
with addition and subtraction in kindergarten (within 5) and grade one (within 10) culminate in grade two students becoming fluent in single-digit additions and related subtractions using mental Level 2 and 3 methods and strategies as needed.

Building upon their work in First Grade, Second Graders use various addition and subtraction strategies in order to fluently add and subtract within 20. Second Graders internalize facts and develop fluency by using strategies often that make sense to them. When students are able to demonstrate fluency they are accurate, efficient, and flexible. Students must have efficient strategies in order to know sums from memory.

Students may still need to support the development of their fluency with math drawings when solving problems. Math drawings represent the number of objects counted (using dots and sticks) and do not need to represent the context of the problem. Thinking about numbers using frames of 10 or making drawings using 5 -groups and tens can be a helpful way to understand single-digit additions and subtractions. An example of interactive games students can play to develop counting and addition skills are available
at http://illuminations.nctm.org/ActivityDetail.aspx?ID=75 (National Council of Teachers of Mathematics [NCTM] Illuminations).

Mental strategies help students develop fluency as they make sense of number relationships while they add and subtract within 20. (CA Mathematics Framework, adopted Nov. 6, 2013)

| Mental strategies |
| :--- |
| - Counting on |
| - Making tens $(9+7=(9+1)+6=10+6)$ |
| - Decomposing a number leading to a ten $(14-6=14-4-2=10-2=8)$ |
| - Fact families $(8+5=13$ and $13-8=5)$ |
| - Doubles $(1+1,2+2,3+3$, etc.) |
| - Doubles plus one $(7+8=7+7+1)$ |

- Relationship between addition and subtraction (e.g., knowing that $8+4=12$, one knows $12-8=4$ )
- Equivalent but easier or known sums (e.g., adding $6+7$ by creating the known equivalent $6+6+1=12+1=13$ )
1.OA. 6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10 . Use strategies such as counting on; making ten (e.g., $8+6=8+2+4=10+4=14$ ); decomposing a number leading to a ten (e.g., $13-4=13-3-1=$ $10-1=9$ ); using the relationship between addition and subtraction (e.g., knowing that $8+4=12$, one knows $12-8=4$ ); and creating equivalent but easier or known sums (e.g., adding $6+$ 7 by creating the known equivalent $6+6+1=12+1=13)$.


## 2.OA.C Work with equal groups of objects to gain foundations for multiplication.

2.OA.3 Determine whether a group of objects (up to 20) has an odd or even number of members, e.g., by pairing objects or counting them by 2 s ; write an equation to express an even number as a sum of two equal addends.

## Essential Skills and Concepts:

$\square$ Represent a number using a group of objects or a drawing

- Determine and explain why a number is odd or even
$\square$ Use strategies such as pairing or counting by 2s
$\square$ Write equations for even numbers using two equal addends


## Question Stems and Prompts:

$\checkmark$ Is this number even or odd? How do you know?
$\checkmark$ Is this group of objects even or odd? How do you know?
$\checkmark$ What will happen if one more objects are added to this group? Would the group of objects be odd or even?
$\checkmark$ When you add these two numbers together is your sum/total even or odd?

## Vocabulary

Tier 2

- object
- determine


## Spanish Cognates

Tier 3

- addend
- odd
- even


## Standards Connections

2.OA. 2 - 2.NBT. 5
2.OA. 3 Examples:


Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/As sessing+2.0A. 3

## 2.OA.C Work with equal groups of objects to gain foundations for multiplication.

2.OA.3 Determine whether a group of objects (up to 20) has an odd or even number of members, e.g., by pairing objects or counting them by 2 s ; write an equation to express an even number as a sum of two equal addends.

## Essential Skills and Concepts:

$\square$ Represent a number using a group of objects or a drawing
$\square$ Determine and explain why a number is odd or even
$\square$ Use strategies such as pairing or counting by 2s
$\square$ Write equations for even numbers using two equal addends

## Question Stems and Prompts:

$\checkmark$ Is this number even or odd? How do you know?
$\checkmark$ Is this group of objects even or odd? How do you know?
$\checkmark$ What will happen if one more objects are added to this group? Would the group of objects be odd or even?
$\checkmark$ When you add these two numbers together is your sum/total even or odd?

## Vocabulary

Tier 2

- object
- determine

Tier 3

- addend
- odd
- even


## Standards Connections

2.OA. 2 - 2.NBT. 5

## 2.OA. 3 Examples:



Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/As sessing+2.0A. 3

## 2.OA.C Work with equal groups of objects to gain foundations for multiplication.

2.OA.3 Determine whether a group of objects (up to 20) has an odd or even number of members, e.g., by pairing objects or counting them by 2 s ; write an equation to express an even number as a sum of two equal addends.

## Standard Explanation

Second graders apply their work with doubles to the concept of odd and even numbers. Students should have ample experiences exploring the concept that if a number can be decomposed (broken apart) into two equal addends or doubles addition facts (e.g., $10=5+5$ ), then that number (10 in this case) is an even number. Students should explore this concept with concrete objects (e.g., counters, cubes, etc.) before moving towards pictorial representations such as circles or arrays.

Grade two students gain important foundations for multiplication as they explore odd and even numbers in a variety of ways (2.OA.3). They use concrete objects (e.g., counters, place-value cubes, etc.) and move towards pictorial representations such as circles or arrays (MP.1). Through investigations students realize an even number of objects can be separated into two equal groups (without extra objects remaining), while an odd number of objects will have one object remaining (MP. 7 and MP.8). Students also apply their work with doubles addition facts and decomposing (breaking apart) numbers into two equal addends (e.g., $10=5+5$ ) to understand the concept of even numbers. Students reinforce this concept as they write equations representing sums of two equal addends, such as $2+2=4,3+3=6,5+5=10,6+6=12$, or $8+8=16$. Students are encouraged to explain how they determined if a number is odd or even and what strategies they used. (MP.3)

## 2.OA. 3 Illustrative Tasks:

- Red and Blue Tiles, https://www.illustrativemathematics.org/illustrations/620
- Buttons Odd and Even, https://www.illustrativemathematics.org/illustrations/1418 6 is even.
$\Leftrightarrow \Leftrightarrow \Leftrightarrow \Leftrightarrow$

We can write $3+3=6$ to show this.


7 is odd.


We can write $3+3+1=7$ to show this.

## 2.OA.C Work with equal groups of objects to gain foundations for multiplication.

2.OA.3 Determine whether a group of objects (up to 20) has an odd or even number of members, e.g., by pairing objects or counting them by 2 s ; write an equation to express an even number as a sum of two equal addends.

## Standard Explanation

Second graders apply their work with doubles to the concept of odd and even numbers. Students should have ample experiences exploring the concept that if a number can be decomposed (broken apart) into two equal addends or doubles addition facts (e.g., $10=5+5$ ), then that number (10 in this case) is an even number. Students should explore this concept with concrete objects (e.g., counters, cubes, etc.) before moving towards pictorial representations such as circles or arrays.

Grade two students gain important foundations for multiplication as they explore odd and even numbers in a variety of ways (2.OA.3). They use concrete objects (e.g., counters, place-value cubes, etc.) and move towards pictorial representations such as circles or arrays (MP.1). Through investigations students realize an even number of objects can be separated into two equal groups (without extra objects remaining), while an odd number of objects will have one object remaining (MP. 7 and MP.8). Students also apply their work with doubles addition facts and decomposing (breaking apart) numbers into two equal addends (e.g., $10=5+5$ ) to understand the concept of even numbers. Students reinforce this concept as they write equations representing sums of two equal addends, such as $2+2=4,3+3=6,5+5=10,6+6=12$, or $8+8=16$. Students are encouraged to explain how they determined if a number is odd or even and what strategies they used. (MP.3)

## 2.OA. 3 Illustrative Tasks:

- Red and Blue Tiles, https://www.illustrativemathematics.org/illustrations/620
- Buttons Odd and Even, https://www.illustrativemathematics.org/illustrations/1418 6 is even.


We can write $3+3+1=7$ to show this.

## 2.OA.C Work with equal groups of objects to gain foundations for multiplication.

2.OA. 4 Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an equation to express the total as a sum of equal addends.

## Essential Skills and Concepts:

$\square$ Build and draw arrays with a specified number of rows and columns
$\square$ Write a repeated addition equation to represent an array

## Question Stems and Prompts:

$\checkmark$ Draw _ rows with _ dots in each row.
$\checkmark$ How many dots do you have?
$\checkmark$ Draw an addition equation to show how you got your answer?
$\checkmark$ Create an array to match $2+2+2+2$.
$\checkmark$ How many rows does this array have?
$\checkmark$ How many columns does this array have?

## Vocabulary

Spanish Cognates
Tier 2

- row
- column columna

Tier 3

- rectangular array
- equation ecuación
- equal addends


## Standards Connections

$2.0 \mathrm{~A} .4 \rightarrow$ 3.0A. 1
2.OA. 4 Examples:

Example: What is the total number of circles below?


| Student $\mathbf{A}$ |
| :---: |
| I see 3 counters in each column and there |
| are 4 columns. So I added |
| $3+3+3+3$. That equals 12. |
| $3+3+3+3=12$ |


| Student B |
| :--- |
| I see 4 counters in each row and there are 3 |
| rows. So I added 4+4+4. That |
| equals 12. |
| $4+4+4=12$ |

(North Carolina Unpacking Document, July 2013)
Array Picture Cards


## 2.OA.C Work with equal groups of objects to gain foundations for multiplication.

2.OA. 4 Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an equation to express the total as a sum of equal addends.

## Essential Skills and Concepts:

$\square$ Build and draw arrays with a specified number of rows and columns
$\square$ Write a repeated addition equation to represent an array

## Question Stems and Prompts:

$\checkmark$ Draw _ rows with _ dots in each row.
$\checkmark$ How many dots do you have?
$\checkmark$ Draw an addition equation to show how you got your answer?
$\checkmark$ Create an array to match $2+2+2+2$.
$\checkmark$ How many rows does this array have?
$\checkmark$ How many columns does this array have?

## Vocabulary

Spanish Cognates

## Tier 2

- row
- column
columna
Tier 3
- rectangular array
- equation ecuación
- equal addends


## Standards Connections

2.0A. $4 \rightarrow 3.0 \mathrm{~A} .1$

### 2.0A. 4 Examples:

Example: What is the total number of circles below?


| Student $\mathbf{A}$ |
| :---: |
| I see 3 counters in each column and there |
| are 4 columns. So I added |
| $3+3+3+3$. That equals 12. |
| $3+3+3+3=12$ |


| Student B |
| :--- |
| I see 4 counters in each row and there are 3 |
| rows. So I added 4+4+4. That |
| equals 12 . |
| $4+4=12$ |

(North Carolina Unpacking Document, July 2013)

## Array Picture Cards



## 2.OA.C Work with equal groups of objects to gain foundations for multiplication.

2.OA. 4 Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an equation to express the total as a sum of equal addends.

## Standard Explanation

With standard 2.OA.4, second grade students use rectangular arrays to work with repeated addition, a building block for multiplication in grade three, using concrete objects (e.g., counters, buttons, square tiles) as well as pictorial representations on grid paper or other drawings of arrays (MP.1). Based on the commutative property of multiplication, students add either the rows or the columns and arrive at the same solution (MP.2). Students write equations that represent the total as the sum of equal addends as shown in the following example.


The first example will support student understanding that $3 \times 4=4 \times 3$, while the second example supports the fact that $4 \times 5=5 \times 4$. (Adapted from Arizona 2012, N. Carolina 2013, Georgia 2011, and KATM 2nd FlipBook 2012)

Students explore this concept with concrete objects (e.g., counters, bears, square tiles, etc.) as well as pictorial representations on grid paper or other drawings.

## 2.OA. 4 Illustrative Task:

- Counting Dots in Arrays,
https://www.illustrativemathematics.org/illustrations/3
Which of the following are equal to the number of dots in the picture below? (Choose all that apply.)


## 2.OA.C Work with equal groups of objects to gain foundations for multiplication.

2.OA. 4 Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an equation to express the total as a sum of equal addends.

## Standard Explanation

With standard 2.OA.4, second grade students use rectangular arrays to work with repeated addition, a building block for multiplication in grade three, using concrete objects (e.g., counters, buttons, square tiles) as well as pictorial representations on grid paper or other drawings of arrays (MP.1). Based on the commutative property of multiplication, students add either the rows or the columns and arrive at the same solution (MP.2). Students write equations that represent the total as the sum of equal addends as shown in the following example.


The first example will support student understanding that $3 \times 4=4 \times 3$, while the second example supports the fact that $4 \times 5=5 \times 4$. (Adapted from Arizona 2012, N. Carolina 2013, Georgia 2011, and KATM 2nd FlipBook 2012)

Students explore this concept with concrete objects (e.g., counters, bears, square tiles, etc.) as well as pictorial representations on grid paper or other drawings.

## 2.OA. 4 Illustrative Task:

- Counting Dots in Arrays,
https://www.illustrativemathematics.org/illustrations/3

Which of the following are equal to the number of dots in the picture below? (Choose all that apply.)
a. $3+3+3$
b. $3+4$
c. $4+4+4$
d. $4+4+4+4$
e. $3+3+3+3$

## 2.NBT.A Understand place value.

2.NBT. 1 Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones. Understand the following as special cases:
a. 100 can be thought of as a bundle of ten tens called a "hundred."
b. The numbers $100,200,300,400,500,600,700$, 800,900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones).

## Essential Skills and Concepts:

$\square$ Understand and represent place value for 3-digit numbers
$\square$ Understand that a hundred is 10 tens, two hundreds is 20 tens...etc.

## Question Stems and Prompts:

$\checkmark$ In the number 765 what is the value of the 7 ? 6 ? 5 ?
$\checkmark$ If I had $\qquad$ hundreds, $\qquad$ tens and $\qquad$ what is my number?
$\checkmark$ If I had $\qquad$ ones how many tens do I have?
$\checkmark$ If I had $\qquad$ tens how many hundreds would I have?
$\checkmark$ If had $\qquad$ ones how many tens do I have? Do I have any ones left?
$\checkmark$ What number does the $\qquad$ stand for in the number $\qquad$ ?

## Vocabulary

## Spanish Cognates

Tier 2

- bundle
- represent representar

Tier3

- hundreds
- tens
- ones
- place value


## Standards Connections <br> 2.NBT. $1 \rightarrow$ 2.NBT.3, 4, 6, 7, 8, 9

## 2.NBT. 1 Example:

Teacher: How many blocks do you have?
Student: I have 3 hundreds, 4 tens and 2 left-overs.
Teacher: Does that help you know how many? How many do you have?
Student: Let me see. $100,200,300 \ldots$ ten, twenty, thirty, forty. So that's 340 so far. Then 2 more. 342.

## 2.NBT.A Understand place value.

2.NBT. 1 Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones. Understand the following as special cases:
a. 100 can be thought of as a bundle of ten tens called a "hundred."
b. The numbers $100,200,300,400,500,600,700$, 800,900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones).

## Essential Skills and Concepts:

$\square$ Understand and represent place value for 3-digit numbers
$\square$ Understand that a hundred is 10 tens, two hundreds is 20 tens...etc.

## Question Stems and Prompts:

$\checkmark$ In the number 765 what is the value of the 7 ? 6 ? 5 ?
$\checkmark$ If I had $\qquad$ hundreds, $\qquad$ tens and $\qquad$ what is my number?
$\checkmark$ If I had $\qquad$ ones how many tens do I have?
$\checkmark$ If I had $\qquad$ tens how many hundreds would I have?
$\checkmark$ If had ___ ones how many tens do I have? Do I have any ones left?
$\checkmark$ What number does the $\qquad$ stand for in the number $\qquad$ ?

## Vocabulary

## Spanish Cognates

Tier 2

- bundle
- represent representar

Tier3

- hundreds
- tens
- ones
- place value


## Standards Connections <br> 2.NBT. $1 \rightarrow$ 2.NBT.3, 4, 6, 7, 8, 9 <br> 2.NBT. 1 Example:

```
Teacher: How many blocks do you have?
Student: I have 3 hundreds, 4 tens and 2 left-overs.
Teacher: Does that help you know how many? How
many do you have?
Student: Let me see. 100, 200, 300... ten, twenty, thirty,
forty. So that's 340 so far. Then 2 more. 342.
```


## 2.NBT.A Understand place value.

2.NBT. 1 Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones. Understand the following as special cases:
a. 100 can be thought of as a bundle of ten tens called a "hundred."
b. The numbers $100,200,300,400,500,600,700$, 800,900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones).

## Standard Explanation

Second grade students build on their previous work with groups of tens to make bundles of 100 s , with or without leftovers, using base-ten blocks, cubes in towers of 10 , ten frames, etc. and math drawings that initially show the ten tens within one hundred but then move to a quickhundred version that is a drawn square in which students visualize ten tens. Bundling hundreds will support students' discovery of place value patterns (MP.7). Students explore the idea that numbers such as $100,200,300$, etc., are groups of hundreds that have " 0 " in the tens and ones places. Students might represent numbers using place value (base ten) blocks (MP.1).

Students use manipulative materials and pictorial representations to help make a connection between the written three-digit numbers and hundreds, tens, and ones. As students represent various numbers, they associate number names with umber quantities (MP.2). For example, can be expressed as both " 2 groups of hundred, 4 groups of ten and 3 ones" and " 24 tens and 3 ones." Students can read number names as well as place value concepts to say a number. For example, 243 should be read as "two hundred forty-three" as well as " 2 hundreds, 4 tens, and 3 ones." Flexibility with seeing a number like 240 as " 2 hundreds and 4 tens" as well as " 24 tens" is an important indicator of place-value understanding. (CA Mathematics Framework, adopted Nov. 6, 2013)


## 2.NBT.A Understand place value.

2.NBT. 1 Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones. Understand the following as special cases:
a. 100 can be thought of as a bundle of ten tens called a "hundred."
b. The numbers $100,200,300,400,500,600,700$, 800,900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones).

## Standard Explanation

Second grade students build on their previous work with groups of tens to make bundles of 100 s , with or without leftovers, using base-ten blocks, cubes in towers of 10 , ten frames, etc. and math drawings that initially show the ten tens within one hundred but then move to a quickhundred version that is a drawn square in which students visualize ten tens. Bundling hundreds will support students' discovery of place value patterns (MP.7). Students explore the idea that numbers such as $100,200,300$, etc., are groups of hundreds that have " 0 " in the tens and ones places. Students might represent numbers using place value (base ten) blocks (MP.1).

Students use manipulative materials and pictorial representations to help make a connection between the written three-digit numbers and hundreds, tens, and ones. As students represent various numbers, they associate number names with umber quantities (MP.2). For example, can be expressed as both " 2 groups of hundred, 4 groups of ten and 3 ones" and " 24 tens and 3 ones." Students can read number names as well as place value concepts to say a number. For example, 243 should be read as "two hundred forty-three" as well as " 2 hundreds, 4 tens, and 3 ones." Flexibility with seeing a number like 240 as " 2 hundreds and 4 tens" as well as " 24 tens" is an important indicator of place-value understanding. (CA Mathematics Framework, adopted Nov. 6, 2013)


## 2.NBT.A Understand place value.

2.NBT. 2 Count within 1000; skip-count by $2 \mathrm{~s}, 5 \mathrm{~s}, 10 \mathrm{~s}$, and 100s. CA

## Essential Skills and Concepts:

$\square$ Count within 1,000 from any given number
Skip count by $2 \mathrm{~s}, 5 \mathrm{~s}, 10 \mathrm{~s}, 100 \mathrm{~s}$

## Question Stems and Prompts:

$\checkmark$ Count forward starting at $\qquad$ .
$\checkmark$ Skip count forward by 2s starting at $\underline{0}$. (Teacher can change the number students are counting by as well as the number where students start counting)
$\checkmark$ Point to a number on the hundred chart. Skip count by 10 s starting at that number.
$\checkmark \quad$ Skip count by 2s for 2 minutes on paper.
$\checkmark$ A student is skip counting by $\underline{5}$. What will the pattern look like if this person continues to skip count?

## Vocabulary

Spanish Cognates
Tier 2

- pattern

Tier 3

- place value
- skip counting
- counting on


## Standards Connections

2.NBT. $2 \rightarrow$ 2.NBT. 1

## 2.NBT. 2 Examples:

Example:
What are the next 3 numbers after 498? 499, 500, 501. When you count back from 201, what are the first 3 numbers that you say? 200, 199, 198.

## Counting Routines:

- Choral counting - Point to a hundreds chart (or other chart or manipulatives) to count aloud as a class. This may be done for counting by ones in a given range or skip counting. https://www.illustrativemathematics.org/illustrations/360
- Counting circles - Select a counting sequence or range to work on while counting by ones or skip counting. Have students count around the circle or class following the given sequence. The student that says the last number in the sequence will sit down. Continue the activity for several rounds.
https://www.illustrativemathematics.org ililustrations/359
- Pick a Number Counting - Use number cards for a particular range of numbers. Have a student select a card. With the class count on from the selected number. This can be used to count by ones within 1,000 or for skip counting. https://www.illustrativemathematics.org/illustrations/927


## 2.NBT.A Understand place value.

2.NBT. 2 Count within 1000 ; skip-count by $2 \mathrm{~s}, 5 \mathrm{~s}, 10 \mathrm{~s}$, and 100s. CA

## Essential Skills and Concepts:

- Count within 1,000 from any given number
$\square$ Skip count by $2 \mathrm{~s}, 5 \mathrm{~s}, 10 \mathrm{~s}, 100 \mathrm{~s}$


## Question Stems and Prompts:

$\checkmark$ Count forward starting at $\qquad$ .
$\checkmark$ Skip count forward by $\underline{\mathbf{s}}$ starting at $\underline{0}$. (Teacher can change the number students are counting by as well as the number where students start counting)
$\checkmark$ Point to a number on the hundred chart. Skip count by 10s starting at that number.
$\checkmark \quad$ Skip count by 2s for 2 minutes on paper.
$\checkmark$ A student is skip counting by 5 s. What will the pattern look like if this person continues to skip count?

## Vocabulary

## Spanish Cognates

Tier 2

- pattern

Tier 3

- place value
- skip counting
- counting on


## Standards Connections <br> 2.NBT. $2 \rightarrow$ 2.NBT. 1

## 2.NBT. 2 Examples:

Example:
What are the next 3 numbers after 498? 499, 500, 501. When you count back from 201, what are the first 3 numbers that you say? 200, 199, 198.

## Counting Routines:

- Choral counting - Point to a hundreds chart (or other chart or manipulatives) to count aloud as a class. This may be done for counting by ones in a given range or skip counting. https://www.illustrativemathematics.org/illustrations/360
- Counting circles - Select a counting sequence or range to work on while counting by ones or skip counting. Have students count around the circle or class following the given sequence. The student that says the last number in the sequence will sit down. Continue the activity for several rounds. https://www.illustrativemathematics.org/illustrations/359
- Pick a Number Counting - Use number cards for a particular range of numbers. Have a student select a card. With the class count on from the selected number. This can be used to count by ones within 1,000 or for skip counting. https://www.illustrativemathematics.org/illustrations/927


## 2.NBT.A Understand place value.

2.NBT. 2 Count within 1000; skip-count by $2 \mathrm{~s}, 5 \mathrm{~s}, 10 \mathrm{~s}$, and 100s. CA

## Standard Explanation

In kindergarten, students were introduced to counting by tens. In second grade they extend this to skip count by $2 \mathrm{~s}, 5 \mathrm{~s}, 10 \mathrm{~s}$ and 100 s (2.NBT. $2 \mathbf{\Delta}$ ). Exploring number patterns can help students skip count. For example, when skip counting by 5 s , the ones digit alternates between 5 and 0 , and when skip counting by 10 s and 100 s, only the tens and hundreds digits change, increasing by one each time. In this way, skip counting can reinforce students' place value understanding. Work with skip counting lays a foundation for multiplication; however, since students do not keep track of the number of groups they have counted they are not yet learning true multiplication. The ultimate goal is for second graders to count in multiple ways without visual support.

Second Grade students count within 1,000 . Thus, students "count on" from any number and say the next few numbers that come afterwards. (CA Mathematics
Framework, adopted Nov. 6, 2013)

## Focus, Coherence, and Rigor: <br> As students explore number pattems to skip-count they also develop mathematical practices Such the meaxing of witten quantities (MP.2) and number patterns and structures in the number

 system (MP.7).
## 2.NBT. 2 Illustrative Task:

- Saving Money 2, https://www.illustrativemathematics.org/illustrations/1309


## a. How much mones will he have to save for both?

b. Louis getis $\$ 5$ a week ior his alowance. He plans to save his allowance every week. How many weeks does it take him to reach this goal?
c. Lovis remembers his sister's birthday is nexit month. He sets a goal o os saing \$16 tor her git. How many weeks does he have to save his allowance to reach this goal? How many weeks does he have to save his alowance tor al lhree of his goas?

## 2.NBT.A Understand place value.

## 2.NBT. 2 Count within 1000 ; skip-count by 2 s , $5 \mathrm{~s}, 10 \mathrm{~s}$, and 100s. CA

## Standard Explanation

In kindergarten, students were introduced to counting by tens. In second grade they extend this to skip count by $2 \mathrm{~s}, 5 \mathrm{~s}, 10 \mathrm{~s}$ and 100 s (2.NBT. $2 \mathbf{\Delta}$ ). Exploring number patterns can help students skip count. For example, when skip counting by 5 s , the ones digit alternates between 5 and 0 , and when skip counting by 10 s and 100 s, only the tens and hundreds digits change, increasing by one each time. In this way, skip counting can reinforce students’ place value understanding. Work with skip counting lays a foundation for multiplication; however, since students do not keep track of the number of groups they have counted they are not yet learning true multiplication. The ultimate goal is for second graders to count in multiple ways without visual support.

Second Grade students count within 1,000 . Thus, students "count on" from any number and say the next few numbers that come afterwards. (CA Mathematics
Framework, adopted Nov. 6, 2013)

| Focus, Coherence, and Rigor: <br> As suduents explore number pattems to to kip.count they aso develop mathematical practices such the meaning of witten quantities (MP.2) and number patterns and strcctures in the number system (MP.7). |
| :---: |
|  |  |

## 2.NBT. 2 Illustrative Task:

- Saving Money 2, https://www.illustrativemathematics.org/illustrations/1309
a. How much moneey will he have to save for both?
b. Louis getis \$5 w week for his allowance. He plans to save his allowance every week. How many weeks does it take him to reach this goal?
c. Lous' remembers his sister's bithday is nexi' month. He sets a goal o os saving \$16 tor her git. How many weeks does he have to save his allowance to reach hhis goal? How many weeks does he have to save h his allowance for al lhree of this goas?


## 2.NBT.A Understand place value.

2.NBT. 3 Read and write numbers to 1000 using base-ten numerals, number names, and expanded form.

## Essential Skills and Concepts:

- Read and name numbers to 1000
- Write numbers/number names to 1000
$\square$ Expand a number into hundreds, tens, and ones and write them in expanded form


## Question Stems and Prompts:

$\checkmark$ Build $\qquad$ and write it in expanded form.
$\checkmark$ Write out the number $\qquad$ in word form.
$\checkmark$ Take this number from expanded form to standard form.
$\checkmark$ Expand this number two different ways.

## Vocabulary

Spanish Cognates
Tier 2

- form
forma
- standard form

Tier 3

- expanded form
- numeral número
- number names
- digit
dígito
2.NBT. 3 Examples:


## Roll A Three-Digit Number

1. Gather three different colored dice.
2. Tell student he/she will roll the 3 dice and make a three-digit number.
3. Student will then write the number in standard form, number names, and expanded form on attached recording chart.
4. Observe how the student reads and writes the number.
Place Vale Card Sort
5. Have students cut, sort and match the cards.
6. Have students read the numbers aloud.


Howard County Public S̄chool System,
https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.NBT. 3

## 2.NBT.A Understand place value.

2.NBT. 3 Read and write numbers to 1000 using base-ten numerals, number names, and expanded form.

## Essential Skills and Concepts:

- Read and name numbers to 1000
$\square$ Write numbers/number names to 1000
$\square$ Expand a number into hundreds, tens, and ones and write them in expanded form


## Question Stems and Prompts:

$\checkmark$ Build $\qquad$ and write it in expanded form.
$\checkmark$ Write out the number $\qquad$ in word form.
$\checkmark$ Take this number from expanded form to standard form.
$\checkmark$ Expand this number two different ways.

## Vocabulary

Tier 2

- form
- standard form

Tier 3

- expanded form
- numeral
- number names
- digit


## 2.NBT. 3 Examples:

Roll A Three-Digit Number
5. Gather three different colored dice.
6. Tell student he/she will roll the 3 dice and make a three-digit number.
7. Student will then write the number in standard form, number names, and expanded form on attached recording chart.
8. Observe how the student reads and writes the number.
Place Vale Card Sort
3. Have students cut, sort and match the cards.
4. Have students read the numbers aloud.


Howard County Public School System,
https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.NBT. 3

## 2.NBT.A Understand place value.

2.NBT. 3 Read and write numbers to 1000 using base-ten numerals, number names, and expanded form.

## Standard Explanation

Grade two students need opportunities to read and represent numerals in various ways (2.NBT. $3 \mathbf{\Delta}$ ). For example:

- Standard form (e.g., 637)
- Base-ten numerals in standard form (e.g., 6 hundreds, 3 tens and 7 ones)
- Number names in word form (e.g., six hundred thirty seven)
- Expanded form (e.g., $600+30+7$ )
- Equivalent representations (e.g., $500+130+7 ; 600+$ $20+17 ; 30+600+7)$
When students read the expanded form for a number, they might say " 6 hundreds plus 3 tens plus 7 ones" or " 600 plus 30 plus 7." Expanded form is a valuable skill when students use place value strategies to add and subtract large numbers (see also 2.NBT.7).

Second graders read, write and represent a number of objects with a written numeral (number form or standard form). These representations can include snap cubes, place value (base 10) blocks, pictorial representations or other concrete materials.

## 2.NBT. 3 Illustrative Task:

- Looking at Numbers Every Which Way, https://www.illustrativemathematics.org/illustrations/1236
a. 127 is a number.
- Write it as a sum of $100 \mathrm{~s}, 10 \mathrm{~s}$, and 1 s s.
- Write its name in words.
- Draw a picture to represent the number.
- Locate it on the number line.
b. $500+60+8$ is a number.
- Write it as a three-digit number.
- Write its name in words.
- Draw a picture to represent the number.
- Locate it on the number line.
c. Six hundred and nine is a number.
- Write it as a three-digit number
- Write it as a sum of 100 's, 10 's, and 1 's.
- Draw a picture to represent the number.
- Locate it on the number line.
d. The picture represents a number. The big square represents 100 , the rectangle represents 10 , and the small square represents 1 .

- Write it as a three-digit number.
- Write it as a sum of 100 's, 10 's, and 1 's.
- Write its name in words.
- Locate it on the number line.


## 2.NBT.A Understand place value.

2.NBT. 3 Read and write numbers to 1000 using base-ten numerals, number names, and expanded form.

## Standard Explanation

Grade two students need opportunities to read and represent numerals in various ways (2.NBT. $3 \mathbf{\Delta}$ ). For example:

- Standard form (e.g., 637)
- Base-ten numerals in standard form (e.g., 6 hundreds, 3 tens and 7 ones)
- Number names in word form (e.g., six hundred thirty seven)
- Expanded form (e.g., $600+30+7$ )
- Equivalent representations (e.g., $500+130+7 ; 600+$ $20+17 ; 30+600+7)$
When students read the expanded form for a number, they might say " 6 hundreds plus 3 tens plus 7 ones" or " 600 plus 30 plus 7." Expanded form is a valuable skill when students use place value strategies to add and subtract large numbers (see also 2.NBT.7).

Second graders read, write and represent a number of objects with a written numeral (number form or standard form). These representations can include snap cubes, place value (base 10) blocks, pictorial representations or other concrete materials.

## 2.NBT. 3 Illustrative Task:

- Looking at Numbers Every Which Way, https://www.illustrativemathematics.org/illustrations/1236
a. 127 is a number.
- Write it as a sum of 100's, 10's, and 1's.
- Write its name in words.
- Draw a picture to represent the number.
- Locate it on the number line.
b. $500+60+8$ is a number
- Write it as a three-digit number.
- Write its name in words.
- Draw a picture to represent the number.
- Locate it on the number line.
c. Six hundred and nine is a number.
- Write it as a three-digit number
- Write it as a sum of 100 's, 10 's, and 1 's.
- Draw a picture to represent the number.
- Locate it on the number line.
d. The picture represents a number. The big square represents 100 , the rectangle represents 10 , and the small square represents 1.

- Write it as a three-digit number.
- Write it as a sum of 100 's, 10 's, and 1 's.
- Write its name in words.
- Locate it on the number line.


## 2.NBT.A Understand place value.

2.NBT. 4 Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using $>,=$, and $<$ symbols to record the results of comparisons.

## Essential Skills and Concepts:

- Compare two three-digit numbers
- Understand and use the inequality symbols $>,<,=$
- Explain and record results of comparisons using symbols


## Question Stems and Prompts:

$\checkmark$ Which number is greater? Which number is the less?
$\checkmark$ Compare these two numbers. Explain how you know which number is greater.
$\checkmark$ How are these numbers the same? How are they different?

## Vocabulary

Tier 2

- compare
- symbol
- record
- less than
- greater than

Tier 3

- inequality symbols
- equal


## Spanish Cognates

comparar
símbolo
2.NBT. 4 Examples:


Howard County Public School System,
https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.NBT. 4

## 2.NBT.A Understand place value.

2.NBT. 4 Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using $>,=$, and $<$ symbols to record the results of comparisons.

## Essential Skills and Concepts:

- Compare two three-digit numbers
- Understand and use the inequality symbols $>,<,=$
- Explain and record results of comparisons using symbols


## Question Stems and Prompts:

$\checkmark$ Which number is greater? Which number is the less?
$\checkmark$ Compare these two numbers. Explain how you know which number is greater.
$\checkmark$ How are these numbers the same? How are they different?

## Vocabulary

Tier 2

- compare
- symbol
- record
- less than
- greater than

Tier 3

- inequality symbols símbolo de la desigualdad
- equal
2.NBT. 4 Examples:

| Example: Compare 452 and 455 . |
| :--- |
| Student 1: Student might explain 452 has 4 hundreds 5 tens and 2 ones and 455 has 4 hundreds |
| 5 tens and 5 ones. They have the same number of hundreds and the same number of tens, but |
| 455 has 5 ones and 452 only has 2 ones. 50,452 is less than 455 or $452<455$. |
| Student 2 : Student might think 452 is less than 455 . I know this beccause when I count up I say |
| 452 before I say 455 . |


| HOWARD COUNTY <br> puguc schoou SSTrem |
| :--- | :--- |
| Name:- |
| 2.NBT.4 |
| Use $<,>$, or $=$ to fill in the blank. |
| 1. 732 861 |

Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.NBT. 4

## 2.NBT.A Understand place value.

2.NBT. 4 Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using $>,=$ and $<$ symbols to record the results of comparisons.

## Standard Explanation

Second grade students use the symbols for greater than ( $>$ ), less than $(<)$ and equal to $(=)$ to compare numbers within 1000 (2.NBT.4 $\mathbf{)}$ ). Students build on work in standards (2.NBT.1 4) and (2.NBT.3 4) by examining the amounts of hundreds, tens, and ones in each number. To compare numbers, students apply their understanding of place value. The goal is for students to understand they look at the numerals in the hundreds place first, then the tens place, and if necessary the ones place. Students should have experience communicating their comparisons in words before using only symbols to indicate greater than, less than, and equal to.

As students compare numbers they also develop mathematical practices such as making sense of quantities (MP.2), understanding the meaning of symbols (MP.6), and making use of number patterns and structures in the number system (MP.7).

## 2.NBT. 4 Illustrative Tasks:

- Ordering 3-digit Numbers, https://www.illustrativemathematics.org/illustrations/7

1. Arrange the following numbers from least to greatest:

| 476 | 647 | 74 | 674 | 467 |
| :--- | :--- | :--- | :--- | :--- |

2. Arrange the following numbers from greatest to least:
$326 \quad 362$
63
623
632

Number Line Comparisons,
https://www.illustrativemathematics.org/illustrations/371
a. Plot the following numbers on the number line.


## 2.NBT.A Understand place value.

2.NBT. 4 Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using >, =, and $<$ symbols to record the results of comparisons.

## Standard Explanation

Second grade students use the symbols for greater than $(>)$, less than $(<)$ and equal to $(=)$ to compare numbers within 1000 (2.NBT.4 $\mathbf{4}$ ). Students build on work in standards (2.NBT.1 ©) and (2.NBT. $3 \mathbf{\Delta}$ ) by examining the amounts of hundreds, tens, and ones in each number. To compare numbers, students apply their understanding of place value. The goal is for students to understand they look at the numerals in the hundreds place first, then the tens place, and if necessary the ones place. Students should have experience communicating their comparisons in words before using only symbols to indicate greater than, less than, and equal to.

As students compare numbers they also develop mathematical practices such as making sense of quantities (MP.2), understanding the meaning of symbols (MP.6), and making use of number patterns and structures in the number system (MP.7).

## 2.NBT. 4 Illustrative Tasks:

- Ordering 3-digit Numbers, https://www.illustrativemathematics.org/illustrations/7

1. Arrange the following numbers from least to greatest:

$$
\begin{array}{llll}
476 & 647 & 74 & 674
\end{array}
$$

467
2. Arrange the following numbers from greatest to least:
$\begin{array}{llll}326 & 362 & 63 & 623\end{array}$
632

- Number Line Comparisons, https://www.illustrativemathematics.org/illustrations/371
a. Plot the following numbers on the number line.

b. Choose eight pairs of numbers from those you plotted on the number line. Compare them.



## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 5 Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.

## Essential Skills and Concepts:

- Add and subtract within 100 using strategies
$\square$ Understand and use the relationship between addition and subtraction (i.e. inverse operations, fact families)
$\square$ Explain strategies for adding and subtracting
$\square$ Use place value understanding to add and subtract


## Question Stems and Prompts:

$\checkmark$ What is the total sum of $\qquad$ and $\qquad$ ? How do you know?
$\checkmark$ Solve this problem in at least two different ways. How are your strategies related?
$\checkmark$ How might you illustrate your strategy using a number line diagram?

## Vocabulary

Tier 2

- strategy
- fluently
- relationship

Tier 3

- addition
- subtraction
- properties of operations operaciónes


## Spanish Cognates

estrategia
fluidez
relación
adición
sustracción
propiedades de las

## Standards Connections <br> 2.NBT. 5 - 2.OA. 1

2.NBT. 5 Examples:

| Strategies for Addition and Subtraction |
| :--- |
| Addition strategies based on place value for $48+37$ may include: |
| - Adding by place value: $40+30=70$ and $8+7=15$ and $70+15=85$. |
| - Incremental adding (by tens and ones); $48+10=58,58+10=68,68+10=78,78+7$ |
| $=85$ |
| - Composing and decomposing (making a "friendly" number): $48+2=50,37-2=35,50$ |
| $+35=85$ |$\quad$| Subtraction strategies based on place value for $81-37$ may include: |
| :--- |
| - Adding up (from smaller number to larger number): $37+3=40,40+40=80,80+1=$ |
| (81, and $3+40+1=44$. |
| - Incremental subtracting: $81-10=71,71-10=61,61-10=51,51-7=44$ |
| - Subtracting by place value: $81-30=51,51-7=44$ |

$$
67+25=
$$

Place Value Strategy:
I broke both 67 and 25 into tens and ones. 6 tens plus 2 tens equals 8 tens. Then I added the ones. 7 ones plus 5 ones equals 12 ones. I then combined my tens and ones. 8 tens plus 12 ones equals 92 .
Decomposing into Tens:
I decided to start with 67 and break 25 apart. I knew I needed 3 more to get to 70, so I broke off a 3 from the 25. I then added my 20 from the 22 left and got to 90. I had 2 left. 90 plus 2 is 92 . So, $67+25=92$

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 5 Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.

## Essential Skills and Concepts:

$\square$ Add and subtract within 100 using strategies
$\square$ Understand and use the relationship between addition and subtraction (i.e. inverse operations, fact families)
$\square$ Explain strategies for adding and subtracting
$\square$ Use place value understanding to add and subtract

## Question Stems and Prompts:

$\checkmark$ What is the total sum of $\qquad$ and $\qquad$ ? How do you know?
$\checkmark$ Solve this problem in at least two different ways. How are your strategies related?
$\checkmark$ How might you illustrate your strategy using a number line diagram?

## Vocabulary

Tier 2

- strategy
- fluently
- relationship

Tier 3

- addition
- subtraction
- properties of operations operaciónes


## Spanish Cognates

## estrategia

fluidez
relación
adición sustracción
propiedades de las

## Standards Connections <br> 2.NBT. 5 - 2.OA. 1

## 2.NBT. 5 Examples:



## 2.NBT.B. 5

## Standard Explanation

Standards (2.NBT.5-7 © ) are crucial for attaining one of the four critical areas of instruction in grade two. It is here that students apply models of addition and subtraction to develop, discuss and later use efficient, accurate, and generalizable methods to compute sums and differences of whole numbers in base-ten notation. While students become fluent in such methods within 100 at grade two, they also use these methods for sums and differences within 1000 . All methods for adding and subtracting two- and three-digit numbers should be based on place value and should be learned by students with an emphasis on understanding. Math drawings should accompany such written methods as students become familiar with them.

There are various strategies that Second Grade students understand and use when adding and subtracting within 100 (such as those listed in the standard). The standard algorithm of carrying or borrowing is neither an expectation nor a focus in Second Grade. Students use multiple strategies for addition and subtraction in Grades K-3.

Written methods for addition and subtraction are based on two important features of the base-10 number system:

- When adding or subtracting numbers in the base-10 system, like units are added or subtracted (e.g., ones are added to ones, tens to tens, hundreds to hundreds).
- Adding and subtracting multi-digit numbers written in base-10 can be facilitated by composing and decomposing units appropriately, so as to reduce the methods to simply doing additions and subtractions within 20 (e.g., 10 ones make 1 ten, 100 ones make 1 hundred, 1 hundred makes 10 tens).
(CA Mathematics Framework, adopted Nov. 6, 2013)
2.NBT. 7 Illustrative Tasks:
- How Many Days Until Summer Vacation? https://www.illustrativemathematics.org/illustrations/1063
We are in school 180 days. Today is the 124th day of school. How many more days until we are out of schoo for summer vacation? Explain how you know.
- How Many Days Until Summer Vacation? $\frac{\mathrm{https}: / / \text { www.illustrativemathematics.org/illustrations/1628 }}{\text { patt }}$ Part 2

After the class has talked about all the ways they could solve the two digit addition problem the teacher should put the following three digit addition problem on the board:
$\begin{array}{r}224 \\ +132 \\ \hline\end{array}$
The students should look over the brainstormed list of solution ways and see if each solution would also apply to solving three digit addition problems. (They all should work for both two and three digit addition problems.) The class can then talk about how their skills for two digit problem solving transfer to three digit problem solving.

## 2.NBT.B. 5

## Standard Explanation

Standards (2.NBT.5-7 © ) are crucial for attaining one of the four critical areas of instruction in grade two. It is here that students apply models of addition and subtraction to develop, discuss and later use efficient, accurate, and generalizable methods to compute sums and differences of whole numbers in base-ten notation. While students become fluent in such methods within 100 at grade two, they also use these methods for sums and differences within 1000 . All methods for adding and subtracting two- and three-digit numbers should be based on place value and should be learned by students with an emphasis on understanding. Math drawings should accompany such written methods as students become familiar with them.

There are various strategies that Second Grade students understand and use when adding and subtracting within 100 (such as those listed in the standard). The standard algorithm of carrying or borrowing is neither an expectation nor a focus in Second Grade. Students use multiple strategies for addition and subtraction in Grades K-3.

Written methods for addition and subtraction are based on two important features of the base-10 number system:

- When adding or subtracting numbers in the base-10 system, like units are added or subtracted (e.g., ones are added to ones, tens to tens, hundreds to hundreds).
- Adding and subtracting multi-digit numbers written in base-10 can be facilitated by composing and decomposing units appropriately, so as to reduce the methods to simply doing additions and subtractions within 20 (e.g., 10 ones make 1 ten, 100 ones make 1 hundred, 1 hundred makes 10 tens).
(CA Mathematics Framework, adopted Nov. 6, 2013)


## 2.NBT. 7 Illustrative Tasks:

- How Many Days Until Summer Vacation? https://www.illustrativemathematics.org/illustrations/1063
We are in school 180 days. Today is the 12 th d day of school. How many more days until we are out of school for summer vacation? Explain how you know.
- How Many Days Until Summer Vacation? https://www.illustrativemathematics.org/illustrations/1628 Part 2

After the class has talked about all the ways they could solve the two digit addition problem the teacher should put the following three digit addition problem on the board:

## $\begin{array}{r}224 \\ +132 \\ \hline\end{array}$

The students should look over the brainstormed list of solution ways and see if each solution would also apply to solving three digit addition problems. (They all should work for both two and three digit addition problems.) The class can then talk about how their skills for two digit problem solving transfer to three digit problem solving.

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 6 Add up to four two-digit numbers using strategies based on place value and properties of operations.

## Essential Skills and Concepts:

$\square$ Understand and use place value strategies
$\square$ Add up to four two-digit numbers
$\square$ Explain the strategy used for adding multiple two-digit numbers

## Question Stems and Prompts:

$\checkmark$ Add these four amounts. What strategy did you use?
$\checkmark$ How did you use to place value to help you add?
$\checkmark$ What is the sum of these four numbers?
$\checkmark$ Here is a sample student strategy. Think about and explain what you see in the sample work.

## Vocabulary

Tier 2

- strategy
estrategia
Tier 3
- place value
- properties of operations propiedades de las operaciónes
2.NBT.6 Examples:


## Example: Find the sum, $43+34+57+24$.

Student A (Commutative and Associative Properties): I saw the 43 and 57 and added them first.
I know 3 plus 7 equals 10 , so when I added them 100 was my answer. Then I added 34 and had 134. Then I added 24 and had 158 . So $43+57+34+24=158$.

Student B (Place Value Strategies): I broke up all of the numbers into tens and ones. First I added the tens. $40+30+50+20=140$. Then ladded the ones. $3+4+7+4=18$. That meant। had 1 ten and 8 ones. $S 0,140+10$ is 150 . 150 and 8 more is 158 . $S o, 43+34+57+24=158$.
Student C (Place Value Strategies and Commutative and Associative Property): I broke up all the numbers into tens and ones. First I added up the tens, $40+30+50+20$. I changed the order of the numbers to make adding easier. I know that 30 plus 20 equals 50 and 50 more equals 100 . Then I added the 40 and got 140 . Then I added up the ones. $3+4+7+4.1$ changed the order of the numbers to make adding easier. I know that 3 plus 7 equals 10 and 4 plus 4 equals 8.10 plus 8 equals 18 . I then combined my tens and my ones. 140 plus 18 ( 1 ten and 8 ones) equals 158.

California Mathematics Framework, November 6, 2013, http://www.cde.ca.gov/ci/ma/cf/draft2mathfwchapters.asp

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 6 Add up to four two-digit numbers using strategies based on place value and properties of operations.

## Essential Skills and Concepts:

$\square$ Understand and use place value strategies
$\square$ Add up to four two-digit numbers
$\square$ Explain the strategy used for adding multiple two-digit numbers

## Question Stems and Prompts:

$\checkmark$ Add these four amounts. What strategy did you use?
$\checkmark$ How did you use to place value to help you add?
$\checkmark$ What is the sum of these four numbers?
$\checkmark$ Here is a sample student strategy. Think about and explain what you see in the sample work.

## Vocabulary

Tier 2

- strategy estrategia
Tier 3
- place value
- properties of operations propiedades de las operaciónes


## 2.NBT.6 Examples:

## Example: Find the sum, $43+34+57+24$.

Student A (Commutative and Associative Properties): I saw the 43 and 57 and added them first.
I know 3 plus 7 equals 10 , so when I added them 100 was my answer. Then I added 34 and had 134. Then I added 24 and had 158 . So $43+57+34+24=158$.

Student B (Place Value Strategies): I broke up all of the numbers into tens and ones. First I added the tens. $40+30+50+20=140$. Then ladded the ones. $3+4+7+4=18$. That meant had 1 ten and 8 ones. So, $140+10$ is 150 . 150 and 8 more is 158 . So, $43+34+57+24=158$.
Student C (Place Value Strategies and Commutative and Associative Property):
I broke up all the numbers into tens and ones. FirstI added up the tens, $40+30+50+20$. I changed the order of the numbers to make adding easier. I know that 30 plus 20 equals 50 and 50 more equals 100 . Then I added the 40 and got 140 . Then I added up the ones. $3+4+7+4.1$ changed the order of the numbers to make adding easier. I know that 3 plus 7 equals 10 and 4 plus 4 equals 8.10 plus 8 equals 18 . I then combined my tens and my ones. 140 plus 18 ( 1 ten and 8 ones) equals 158.

California Mathematics Framework, November 6, 2013, http://www.cde.ca.gov/ci/ma/cf/draft2mathfwchapters.asp

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 6 Add up to four two-digit numbers using strategies based on place value and properties of operations.

## Standard Explanation

Second Grade students add a string of two-digit numbers (up to four numbers) by applying place value strategies and properties of operations. Students can utilize many of the other strategies that they have been using to add when adding multiple two-digit numbers. Strategies they may use include: making a ten, decomposing numbers by their place value, using an open number line.

## 2.NBT. 6 Illustrative Tasks:

- Ordering 3-digit Numbers, https://www.illustrativemathematics.org/illustrations/755
The picture shows islands connected by bridges. To cross a bridge, you must pay a toll in coins. If you start on the island marked in blue with 100 coins, how can you make it to the island marked in red?



## 2.NBT. 6 Example:

Toss two, three, or four chips on the mat. Add the numbers the chips are on.


Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/Asses sing+2.NBT. 6

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 6 Add up to four two-digit numbers using strategies based on place value and properties of operations.

## Standard Explanation

Second Grade students add a string of two-digit numbers (up to four numbers) by applying place value strategies and properties of operations. Students can utilize many of the other strategies that they have been using to add when adding multiple two-digit numbers. Strategies they may use include: making a ten, decomposing numbers by their place value, using an open number line.

## 2.NBT. 6 Illustrative Tasks:

- Ordering 3-digit Numbers, https://www.illustrativemathematics.org/illustrations/755
The picture shows islands connected by bridges. To cross a bridge, you must pay a toll in coins. If you start on the island marked in blue with 100 coins, how can you make it to the island marked in red?

2.NBT. 6 Example:

Toss two, three, or four chips on the mat. Add the numbers the chips are on.


Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/Asses sing+2.NBT. 6

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 7 Add and subtract within 1000, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtracting three-digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds.

## Essential Skills and Concepts:

$\square$ Add and subtract within 1000 using concrete models and strategies
$\square$ Understand and use the relationship between addition and subtraction
$\square$ Use place value understanding to add each place value
$\square$ Explain strategies used to add and subtract

## Question Stems and Prompts:

$\checkmark$ What is the total sum of $\qquad$ and $\qquad$ ?
$\checkmark$ What is the total when you take away $\qquad$ from $\qquad$ ?
$\checkmark$ Use a different strategy to find the answer.
$\checkmark$ Which strategy did you use? Explain your thinking.
$\checkmark$ How does your strategy compare to other strategies used?

## Vocabulary

Tier 2

- strategy
- model
- compose
- decompose

Tier 3

- addition
- subtraction
- inverse operation
- equation


## Spanish Cognates

estrategia
modelo
componer
descomponer
adición
sustracción
operación inversa
ecuación

## Standards Connections

2.NBT. $7 \rightarrow$ 2.NBT.6, 2.NBT. 7 - 2.NBT. 8


## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 7 Add and subtract within 1000 , using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtracting three-digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds.

## Essential Skills and Concepts:

$\square$ Add and subtract within 1000 using concrete models and strategies
$\square$ Understand and use the relationship between addition and subtraction
$\square$ Use place value understanding to add each place value
$\square$ Explain strategies used to add and subtract

## Question Stems and Prompts:

$\checkmark$ What is the total sum of $\qquad$ and $\qquad$ ?
$\checkmark$ What is the total when you take away $\qquad$ from $\qquad$ ?
$\checkmark$ Use a different strategy to find the answer.
$\checkmark$ Which strategy did you use? Explain your thinking.
$\checkmark$ How does your strategy compare to other strategies used?

## Vocabulary

Tier 2

- strategy
- model
- compose
- decompose

Tier 3

- addition
- subtraction
- inverse operation
- equation


## Spanish Cognates

estrategia modelo componer descomponer

## adición

sustracción
operación inversa ecuación

## Standards Connections

2.NBT. $7 \rightarrow$ 2.NBT.6, 2.NBT. 7 - 2.NBT. 8


## 2.NBT.B. 7

## Standard Explanation

Second graders extend the work from 2.NBT.5, adding and subtracting with 2-digit numbers, to working with 3-digit numbers. Students should have ample experiences using concrete materials and pictorial representations to support their work. This standard also references composing and decomposing a ten. This work should include strategies such as making a 10 , making a 100 , breaking apart a 10 , or creating an easier problem. The standard algorithm of carrying or borrowing is not an expectation in Second Grade. Students are not expected to add and subtract whole numbers using a standard algorithm until the end of Fourth Grade.

Students first work with math drawings or manipulatives alongside the written methods; they will eventually move on to just using written methods, mentally constructing pictures as necessary and using other strategies. Teachers should note the importance of these methods; they generalize to larger numbers and decimals and emphasize the regrouping nature of combining units. Note that these two methods are only examples and are not meant to represent all such place value methods.

Students will encounter situations where students "don't have enough" to subtract. Note that this is more precise than saying, "You can't subtract a larger number from a smaller number," or the like, as the latter statement is a false mathematical statement. (CA Mathematics Framework, adopted Nov. 6, 2013)


## 2.NBT.B. 7

## Standard Explanation

Second graders extend the work from 2.NBT.5, adding and subtracting with 2-digit numbers, to working with 3-digit numbers. Students should have ample experiences using concrete materials and pictorial representations to support their work. This standard also references composing and decomposing a ten. This work should include strategies such as making a 10 , making a 100 , breaking apart a 10 , or creating an easier problem. The standard algorithm of carrying or borrowing is not an expectation in Second Grade. Students are not expected to add and subtract whole numbers using a standard algorithm until the end of Fourth Grade.

Students first work with math drawings or manipulatives alongside the written methods; they will eventually move on to just using written methods, mentally constructing pictures as necessary and using other strategies. Teachers should note the importance of these methods; they generalize to larger numbers and decimals and emphasize the regrouping nature of combining units. Note that these two methods are only examples and are not meant to represent all such place value methods.

Students will encounter situations where students "don't have enough" to subtract. Note that this is more precise than saying, "You can't subtract a larger number from a smaller number," or the like, as the latter statement is a false
mathematical statement. (CA Mathematics Framework, adopted Nov. 6, 2013)


## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT.7.1 Use estimation strategies to make reasonable estimates in problem solving. CA

## Essential Skills and Concepts:

$\square$ Use and discuss estimation strategies for solving problems

- Understand what makes an estimate reasonable


## Question Stems and Prompts:

$\checkmark$ Before adding these numbers, create an estimate.

- What is an estimate that you know is too low?
- What is an estimate that you know is too high?
$\checkmark$ How does estimating before solving a problem help you to know if your answer is reasonable?
$\checkmark$ Estimate how many $\qquad$ are in this jar.
$\checkmark$ How long do you think this is?
$\checkmark$ Guess how much ___ it will take to fill this jar.


## Vocabulary

Tier 2

- strategy
- reasonable

Tier 3

- estimate


## Spanish Cognates

estrategia
razonable
estimación

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT.7.1 Use estimation strategies to make reasonable estimates in problem solving. CA

## Essential Skills and Concepts:

$\square$ Use and discuss estimation strategies for solving problems
$\square$ Understand what makes an estimate reasonable

## Question Stems and Prompts:

$\checkmark$ Before adding these numbers, create an estimate.

- What is an estimate that you know is too low?
- What is an estimate that you know is too high?
$\checkmark$ How does estimating before solving a problem help you to know if your answer is reasonable?
$\checkmark$ Estimate how many $\qquad$ are in this jar.
$\checkmark$ How long do you think this is?
$\checkmark$ Guess how much $\qquad$ it will take to fill this jar.


## Vocabulary

Tier 2

- strategy
- reasonable

Tier 3

- estimate


## Spanish Cognates

estrategia
razonable
estimación

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT.7.1 Use estimation strategies to make reasonable estimates in problem solving. CA

## Standard Explanation

In second grade, students continue to check for reasonableness as they solve problems. They learn a variety of estimation strategies that they can utilize while they are solving problems. Students should discuss their estimation strategies with the class, allowing them to learn from one another and critique each other's reasoning (MP.3).

As students develop their estimating abilities, they should incorporate their estimation strategies into their problem solving work. These strategies will be important as they determine whether or not their solutions are reasonable based on their estimates about the problem.

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT.7.1 Use estimation strategies to make reasonable estimates in problem solving. CA

## Standard Explanation

In second grade, students continue to check for reasonableness as they solve problems. They learn a variety of estimation strategies that they can utilize while they are solving problems. Students should discuss their estimation strategies with the class, allowing them to learn from one another and critique each other's reasoning (MP.3).

As students develop their estimating abilities, they should incorporate their estimation strategies into their problem solving work. These strategies will be important as they determine whether or not their solutions are reasonable based on their estimates about the problem.

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 8 Mentally add 10 or 100 to a given number 100900 , and mentally subtract 10 or 100 from a given number 100-900.

## Essential Skills and Concepts:

- Understand place value and use this understanding to add or subtract 10 or 100 from a given problem
$\square$ Mentally add or subtract 10 from 100-900
$\square$ Mentally add or subtract 100 from 100-900


## Question Stems and Prompts:

$\checkmark$ If you add/subtract 10 to $\qquad$ what would your total be?
$\checkmark$ If you add/subtract 100 to $\qquad$ what would your total be? How do you know?
$\checkmark$ Describe what would happen if you add/subtract 10 or a hundred to a number built using base ten blocks. What would the new number be and how would your model change?

## Vocabulary

## Spanish Cognates

Tier 2

- mentally

Tier 3

- add
- subtract
- place value


## Standards Connections

2.NBT. 8 - 2.NBT.7, 2.NBT. 9

## 2.NBT. 8 Examples:

Within the same hundred
What is $\mathbf{1 0}$ more than 218 ?
What is 241-10?
Across hundreds
$293+10=$
What is 10 less than 206?

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 8 Mentally add 10 or 100 to a given number 100900 , and mentally subtract 10 or 100 from a given number 100-900.

## Essential Skills and Concepts:

$\square$ Understand place value and use this understanding to add or subtract 10 or 100 from a given problem
$\square$ Mentally add or subtract 10 from 100-900
$\square$ Mentally add or subtract 100 from 100-900
Question Stems and Prompts:
$\checkmark$ If you add/subtract 10 to $\qquad$ what would your total be?
$\checkmark$ If you add/subtract 100 to $\qquad$ what would your total be? How do you know?
$\checkmark$ Describe what would happen if you add/subtract 10 or a hundred to a number built using base ten blocks. What would the new number be and how would your model change?

## Vocabulary

Spanish Cognates
Tier 2

- mentally

Tier 3

- add
- subtract
- place value


## Standards Connections

## 2.NBT. 8 - 2.NBT.7, 2.NBT. 9

## 2.NBT. 8 Examples:

Within the same hundred
What is $\mathbf{1 0}$ more than 218 ?
What is 241 - 10?

## Across hundreds

$293+10=$
What is 10 less than 206?

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 8 Mentally add 10 or 100 to a given number 100900 , and mentally subtract 10 or 100 from a given number 100-900.

## Standard Explanation

Second Grade students mentally add or subtract either 10 or 100 to any number between 100 and 900 . As teachers provide ample experiences for students to work with pre-grouped objects and facilitate discussion, second graders realize that when one adds or subtracts 10 or 100 that only the tens place or the digit in the hundreds place changes by 1 . As the teacher facilitates opportunities for patterns to emerge and be discussed, students notice the patterns and connect the digit change with the amount changed. Opportunities to solve problems in which students cross hundreds are also provided once students have become comfortable adding and subtracting within the same hundred.

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 8 Mentally add 10 or 100 to a given number 100900 , and mentally subtract 10 or 100 from a given number 100-900.

## Standard Explanation

Second Grade students mentally add or subtract either 10 or 100 to any number between 100 and 900 . As teachers provide ample experiences for students to work with pre-grouped objects and facilitate discussion, second graders realize that when one adds or subtracts 10 or 100 that only the tens place or the digit in the hundreds place changes by 1 . As the teacher facilitates opportunities for patterns to emerge and be discussed, students notice the patterns and connect the digit change with the amount changed. Opportunities to solve problems in which students cross hundreds are also provided once students have become comfortable adding and subtracting within the same hundred.

## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 9 Explain why addition and subtraction strategies work, using place value and the properties of operations. ${ }^{3}$

## Essential Skills and Concepts:

- Understand strategies for addition and subtraction
$\square$ Explain why the strategy used works
$\square$ Verbalize and write out explanations using drawings and objects for additional support as needed


## Question Stems and Prompts:

$\checkmark$ What strategy did you use? Would other strategies work?
$\checkmark$ Why did you choose this strategy?
$\checkmark$ Can you draw out or demonstrate your strategy using objects?
$\checkmark$ Solve this problem using two different strategies.

## Vocabulary

Tier 2

- strategy
- explanations

Tier 3

- addition
- subtraction
- properties
- operations

Spanish Cognates
estrategia
explicaciones
adición
sustracción
propiedades
operaciones

## Standards Connections

2.NBT. 9 - 2.NBT.7, 2.NBT. 8

## 2.NBT. 9 Examples:

Example: There are 36 birds in the park. 25 more birds arrive. How many birds are there? Solve the problem and show your work.
Student A: I broke 36 and 25 into tens and ones $(30+6)+(20+5)$. I can change the order of my numbers, since it doesn't change any amounts, sol added $30+20$ and got 50 . Then I added 5 and 5 to make 10 and added it to the $50.50,50$ and 10 more is 60 . I added the one that was left over and got 61 . So there are 61 birds in the park.
Student B: I used a math drawing and made a pile of 36 and a pile of 25 . Altogether, I had 5 tens and 11 ones. 11 ones is the same as one ten and one left over. $\mathrm{SO}, \mathrm{I}$ really had 6 tens and 1 one. That makes 61 .

How are $14-9$ and $5+9$ related?
Howard County Public School System,
https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.NBT. 9

[^1][^2]
## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 9 Explain why addition and subtraction strategies work, using place value and the properties of operations. ${ }^{3}$

## Standard Explanation

Students explain why addition and subtraction strategies work, using place value and the properties of operations. (2.NBT.9 ) Second grade students need multiple opportunities to explain their addition and subtraction thinking (MP.2). For example, students use place value understanding, properties of operations, number names, words (including mathematical language), math drawings, number lines, and/or physical objects to explain why and how they solve a problem (MP.1, MP.6). Students can also critique the work of other students (MP.3) to deepen their understanding of addition and subtraction strategies.

Second graders may use drawings or objects to support their explanation. Students will need frequent opportunities to solve a problem and then discuss their strategies and why they did or didn't work. These opportunities should include both speaking and writing prompts. Students can practice these ideas through the use of math journals, structured partner/group talk, and Number Talks. (CA Mathematics Framework, adopted Nov. 6, 2013)

```
Focus, Coherence, and Rigor:
When students explain why addition and subtraction strategies work (2.NBT.94), they reinforce foundations for solving one- and two-step word problems (2.0A.14) and extend their understanding and use of various strategies and models, drawings, and a witter method to add and subtract (2.NBT. \(5 \mathbf{\Delta}\) and 74).
```


## 2.NBT. 9 Examples:

There are 36 birds in the park. 25 more birds arrive. How many birds are there? Solve the problem and show your work.


[^3]
## 2.NBT.B Use place value understanding and properties of operations to add and subtract.

2.NBT. 9 Explain why addition and subtraction strategies work, using place value and the properties of operations. ${ }^{3}$

## Standard Explanation

Students explain why addition and subtraction strategies work, using place value and the properties of operations. (2.NBT.9 A ) Second grade students need multiple opportunities to explain their addition and subtraction thinking (MP.2). For example, students use place value understanding, properties of operations, number names, words (including mathematical language), math drawings, number lines, and/or physical objects to explain why and how they solve a problem (MP.1, MP.6). Students can also critique the work of other students (MP.3) to deepen their understanding of addition and subtraction strategies.

Second graders may use drawings or objects to support their explanation. Students will need frequent opportunities to solve a problem and then discuss their strategies and why they did or didn't work. These opportunities should include both speaking and writing prompts. Students can practice these ideas through the use of math journals, structured partner/group talk, and Number Talks. (CA Mathematics Framework, adopted Nov. 6, 2013)

```
Focus,Coherence, and Rigor:
When students explain why addition and subtraction strategies work (2.NBT.94), they reinforce
foundations for solving one-and two-step word problems (2.0A.14) and extend their
understanding and use of various strategies and models, drawings, and a witten method to add
and subtract (2.NBT.5\ and 74).
```


## 2.NBT. 9 Examples:

There are 36 birds in the park. 25 more birds arrive. How many birds are there? Solve the problem and show your work.


[^4]
## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 1 Measure the length of an object by selecting and using appropriate tools such as rulers, yardsticks, meter sticks, and measuring tapes.

## Essential Skills and Concepts:

$\square$ Measure objects with a ruler, yardstick, meter stick, and a measuring tape
$\square$ Recognize and discuss the differences between measuring tools
$\square$ Decide which tool would be best for a given situation and justify your thinking

## Question Stems and Prompts:

$\checkmark$ Which measuring tool would you use to measuring this ? Why?
$\checkmark \overline{\text { Which }}$ measuring tool would be a better choice to measure this $\qquad$ ? Why?
$\checkmark$ Would it be appropriate to use a ruler to measure $\qquad$ ? Why or why not?
$\checkmark$ Can you explain the differences and similarities of a ruler and a yardstick? A yardstick and meter stick?

## Vocabulary

Tier 2

- object

Tier 3

- measure
- length
- ruler
- yard stick
- meter stick


## Standards Connections

2.MD. $1 \rightarrow$ 2.MD.2, 2.MD. 3
2.MD. 1 Examples:


## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 1 Measure the length of an object by selecting and using appropriate tools such as rulers, yardsticks, meter sticks, and measuring tapes.

## Essential Skills and Concepts:

$\square$ Measure objects with a ruler, yardstick, meter stick, and a measuring tape
$\square$ Recognize and discuss the differences between measuring tools
$\square$ Decide which tool would be best for a given situation and justify your thinking

## Question Stems and Prompts:

$\checkmark$ Which measuring tool would you use to measuring this ? Why?
$\checkmark$ Which measuring tool would be a better choice to measure this $\qquad$ ? Why?
$\checkmark$ Would it be appropriate to use a ruler to measure $\qquad$ ? Why or why not?
$\checkmark$ Can you explain the differences and similarities of a ruler and a yardstick? A yardstick and meter stick?

## Vocabulary

Tier 2

- object

Tier 3

- measure
- length
- ruler
- yard stick
- meter stick


## Standards Connections

2.MD. $1 \rightarrow$ 2.MD.2, 2.MD. 3

## 2.MD. 1 Examples:



## 2.MD.A. 1

## Standard Explanation

Second graders are transitioning from measuring lengths with informal or nonstandard units to measuring with standard units-inches, feet, centimeters, and meters-and using standard measurement tools (2.MD.1 ©). Students learn the measure of length as a count of how many units are needed to match the length of the object or distance being measured. Using both customary (inches and feet) and metric (centimeters and meters) units, students measure the length of objects with rulers, yardsticks, meter sticks, and tape measures. Students become familiar with standard units (e.g., 12 inches in a foot, 3 feet in a yard, and 100 centimeters in a meter) and how to estimate lengths. (Adapted from KATM 2nd 434 FlipBook 2012).

As teachers provide rich tasks that ask students to perform real measurements, these foundational understandings of measurement are developed:

- Understand that larger units (e.g., yard) can be subdivided into equivalent units (e.g., inches) (partition).
- Understand that the same object or many objects of the same size such as paper clips can be repeatedly used to determine the length of an object (iteration).
- Understand the relationship between the size of a unit and the number of units needed (compensatory principal). Thus, the smaller the unit, the more units it will take to measure the selected attribute.

Students also can learn accurate procedures and concepts by drawing simple unit rulers. Using copies of a single length-unit such as inch-long manipulatives, Students mark off length-units on strips of paper, explicitly connecting measurement with the ruler to measurement by iterating physical units. Thus, students' first rulers are simple tools to help count the iteration of length-units. Frequently comparing results of measuring the same object with manipulative standard units and with student-created rulers can help students connect their experiences and ideas. As they build and use these tools, they develop the ideas of length-unit iteration, correct alignment (with a ruler), and the zero-point concept (the idea that the zero of the ruler indicates one endpoint of a length). (CA Mathematics Framework, adopted Nov. 6, 2013)


Students use a standard unit (shown in below the ruler) to make rulers, helping them to understand the meaning of the markings on rulers.
(K-5, Geometric Measurement Progression)

## 2.MD.A. 1

## Standard Explanation

Second graders are transitioning from measuring lengths with informal or nonstandard units to measuring with standard units - inches, feet, centimeters, and meters-and using standard measurement tools (2.MD.1 ©). Students learn the measure of length as a count of how many units are needed to match the length of the object or distance being measured. Using both customary (inches and feet) and metric (centimeters and meters) units, students measure the length of objects with rulers, yardsticks, meter sticks, and tape measures. Students become familiar with standard units (e.g., 12 inches in a foot, 3 feet in a yard, and 100 centimeters in a meter) and how to estimate lengths. (Adapted from KATM 2nd 434 FlipBook 2012).

As teachers provide rich tasks that ask students to perform real measurements, these foundational understandings of measurement are developed:

- Understand that larger units (e.g., yard) can be subdivided into equivalent units (e.g., inches) (partition).
- Understand that the same object or many objects of the same size such as paper clips can be repeatedly used to determine the length of an object (iteration).
- Understand the relationship between the size of a unit and the number of units needed (compensatory principal). Thus, the smaller the unit, the more units it will take to measure the selected attribute.

Students also can learn accurate procedures and concepts by drawing simple unit rulers. Using copies of a single length-unit such as inch-long manipulatives, Students mark off length-units on strips of paper, explicitly connecting measurement with the ruler to measurement by iterating physical units. Thus, students' first rulers are simple tools to help count the iteration of length-units. Frequently comparing results of measuring the same object with manipulative standard units and with student-created rulers can help students connect their experiences and ideas. As they build and use these tools, they develop the ideas of length-unit iteration, correct alignment (with a ruler), and the zero-point concept (the idea that the zero of the ruler indicates one endpoint of a length). (CA Mathematics Framework, adopted Nov. 6, 2013)


Students use a standard unit (shown in below the ruler) to make rulers, helping them to understand the meaning of the markings on rulers.
(K-5, Geometric Measurement Progression)
2.MD.A Measure and estimate lengths in standard units.
2.MD. 2 Measure the length of an object twice, using length units of different lengths for the two measurements; describe how the two measurements relate to the size of the unit chosen.

## Essential Skills and Concepts:

$\square$ Measure an object twice with two different length units (inch squares, cm cubes, paperclips, crayon, etc.)
$\square$ Compare and discuss the results of your measurements

## Question Stems and Prompts:

$\checkmark$ Measure this $\qquad$ with cm cubes and then with inch squares. What is the length using each unit?
$\checkmark$ Which measuring unit took the most units?
$\checkmark$ Which measure unit took the least units?
$\checkmark$ Which measuring unit is a better choice to measure
$\qquad$ ? Explain your thinking.

## Vocabulary

Tier 2

- compare
- object
- unit

Tier 3

- measure
- length
- inch
- centimeter


## Spanish Cognates

comparar
objeto
unidad

## Standards Connections

2.MD. $2 \rightarrow$ 3.NF. 1
2.MD. 2 Examples:

A student measured the length of a desk in both feet and inches. She found that the desk was 3 feet long. She also found out that it was 36 inches long.

Teacher: Why do you think you have two different measurements for the same desk?
Student: It only took 3 feet because the feet are so big. It took 36 inches because an inch is a whole lot smaller than a foot.

## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 2 Measure the length of an object twice, using length units of different lengths for the two measurements; describe how the two measurements relate to the size of the unit chosen.

## Essential Skills and Concepts:

ㅁ Measure an object twice with two different length units (inch squares, cm cubes, paperclips, crayon, etc.)
$\square$ Compare and discuss the results of your measurements

## Question Stems and Prompts:

$\checkmark$ Measure this $\qquad$ with cm cubes and then with inch squares. What is the length using each unit?
$\checkmark$ Which measuring unit took the most units?
$\checkmark$ Which measure unit took the least units?
$\checkmark$ Which measuring unit is a better choice to measure
$\qquad$ ? Explain your thinking.

## Vocabulary

Tier 2

- compare
- object
- unit

Tier 3

- measure
- length
- inch
- centimeter centímetro


## Standards Connections

2.MD. $2 \rightarrow 3 . N F .1$
2.MD. 2 Examples:

A student measured the length of a desk in both feet and inches. She found that the desk was 3 feet long. She also found out that it was 36 inches long.

Teacher: Why do you think you have two different measurements for the same desk?
Student: It only took 3 feet because the feet are so big. It took 36 inches because an inch is a whole lot smaller than a foot.

## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 2 Measure the length of an object twice, using length units of different lengths for the two measurements; describe how the two measurements relate to the size of the unit chosen. ${ }^{3}$

## Standard Explanation

Second graders learn the concept of the inverse relationship between the size of the unit of length and the number of units required to cover a specific length or distance, specifically, that the larger the unit, the fewer units needed to measure something, and vice versa (2.MD. $2 \mathbf{\Delta}$ ).

Second graders learn the concept of the inverse relationship between the size of the unit of length and the number of units required to cover a specific length or distance. Students measure the length of the same object using units of different lengths (ruler with inches vs. ruler with centimeters or a foot ruler vs. a yardstick) and discuss the relationship between the size of the units and measurements.

Second Grade students measure an object using two units of different lengths. This experience helps students realize that the unit used is as important as the attribute being measured. This is a difficult concept for young children and will require numerous experiences for students to predict, measure, and discuss outcomes.

Students use this information to understand how to select appropriate tools for measuring a given object. For instance, a student might think, "The longer the unit, the fewer I need." Measurement problems also support mathematical practices such reasoning quantitatively (MP.2), justifying conclusions (MP.3), using appropriate tools (MP.5), attending to precision (MP.6), and making use of structure or patterns (MP. 7). (CA Mathematics Framework, adopted Nov. 6, 2013)

## Matches of different lengths

Row $A$ is 5 matches long-when the unit of measurement is white matches. Row $B$ is 6 matches long-when the unit of measurement is dark matches. From Inhelder, Sinclair, and Bovet, 1974, Learning and the Development of Cognition, Harvard University Press.
(K-5, Geometric Measurement Progression)

## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 2 Measure the length of an object twice, using length units of different lengths for the two measurements; describe how the two measurements relate to the size of the unit chosen. ${ }^{3}$

## Standard Explanation

Second graders learn the concept of the inverse relationship between the size of the unit of length and the number of units required to cover a specific length or distance, specifically, that the larger the unit, the fewer units needed to measure something, and vice versa (2.MD.2 $\mathbf{\Delta}$ ).

Second graders learn the concept of the inverse relationship between the size of the unit of length and the number of units required to cover a specific length or distance. Students measure the length of the same object using units of different lengths (ruler with inches vs. ruler with centimeters or a foot ruler vs. a yardstick) and discuss the relationship between the size of the units and measurements.

Second Grade students measure an object using two units of different lengths. This experience helps students realize that the unit used is as important as the attribute being measured. This is a difficult concept for young children and will require numerous experiences for students to predict, measure, and discuss outcomes.

Students use this information to understand how to select appropriate tools for measuring a given object. For instance, a student might think, "The longer the unit, the fewer I need." Measurement problems also support mathematical practices such reasoning quantitatively (MP.2), justifying conclusions (MP.3), using appropriate tools (MP.5), attending to precision (MP.6), and making use of structure or patterns (MP. 7). (CA Mathematics Framework, adopted Nov. 6, 2013)

## Matches of different lengths

Row $A$ is 5 matches long-when the unit of measurement is white matches. Row $B$ is 6 matches long-when the unit of measurement is dark matches. From Inhelder, Sinclair, and Bovet, 1974, Learning and the Development of Cognition, Harvard University Press.
(K-5, Geometric Measurement Progression)

[^5][^6]2.MD.A Measure and estimate lengths in standard units.
2.MD. 3 Estimate lengths using units of inches, feet, centimeters, and meters.

## Essential Skills and Concepts:

$\square$ Estimate a length of an object using inches, feet, centimeters, and meters

## Question Stems and Prompts:

$\checkmark$ How many inches do you think this $\qquad$ is?
$\checkmark$ How long is $\qquad$ ?
$\checkmark$ Which standard unit would you use to measure this?
$\checkmark$ About how many rulers (1 foot) would it take to measure this?

## Vocabulary

Spanish Cognates
Tier 3

- measure
- length
- standard units
- estimate
estimación
- inches
- feet
- centimeter centímetro
- meter metro


## Standards Connections

2.MD. $3 \rightarrow$ 2.MD.2, 2.MD. 4

## 2.MD. 3 Examples:

Teacher: How many inches do you think this string is if you measured it with a ruler?
Student: An inch is pretty small. I'm thinking it will be somewhere between 8 and 9 inches.
Teacher: Measure it and see.
Student: It is 9 inches. I thought that it would be somewhere around there.
(North Carolina Department of Public Instruction, Unpacked Content, updated July 2013)


[^7]
## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 3 Estimate lengths using units of inches, feet, centimeters, and meters.

## Essential Skills and Concepts:

$\square$ Estimate a length of an object using inches, feet, centimeters, and meters

## Question Stems and Prompts:

$\checkmark$ How many inches do you think this $\qquad$ is?
$\checkmark$ How long is $\qquad$ ?
$\checkmark$ Which standard unit would you use to measure this?
$\checkmark$ About how many rulers (1 foot) would it take to measure this?

## Vocabulary

Tier 3

- measure
- length
- standard units
- estimate
- inches
- feet
- centimeter centímetro
- meter metro


## Standards Connections <br> 2.MD. $3 \rightarrow$ 2.MD.2, 2.MD. 4

## 2.MD. 3 Examples:

Teacher: How many inches do you think this string is if you measured it with a ruler?
Student: An inch is pretty small. I'm thinking it will be somewhere between 8 and 9 inches.
Teacher: Measure it and see.
Student: It is 9 inches. I thought that it would be somewhere around there.
(North Carolina Department of Public Instruction, Unpacked Content, updated July 2013)


[^8]
## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 3 Estimate lengths using units of inches, feet, centimeters, and meters.

## Standard Explanation

Students estimate lengths using units of inches, feet, centimeters, and meters. (2.MD.A. $3 \mathbf{\Delta}$ ). Students estimate lengths before they measure. After measuring an object, students discuss their estimations, measurement procedures, and the differences between their estimates and the measurements. Students should begin by estimating measurements of familiar items (length of desk, pencil, favorite book, etc.). Estimation helps students focus on the attribute to be measured, the length units, and the process. Students need many experiences with using measuring tools to develop their understanding of linear measurement. (CA Mathematics Framework, adopted Nov. 6, 2013)

## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 3 Estimate lengths using units of inches, feet, centimeters, and meters.

## Standard Explanation

Students estimate lengths using units of inches, feet, centimeters, and meters. (2.MD.A. $3 \boldsymbol{\Delta}$ ). Students estimate lengths before they measure. After measuring an object, students discuss their estimations, measurement procedures, and the differences between their estimates and the measurements. Students should begin by estimating measurements of familiar items (length of desk, pencil, favorite book, etc.). Estimation helps students focus on the attribute to be measured, the length units, and the process. Students need many experiences with using measuring tools to develop their understanding of linear measurement. (CA Mathematics Framework, adopted Nov. 6, 2013)
2.MD.A Measure and estimate lengths in standard units.
2.MD. 4 Measure to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit.

## Essential Skills and Concepts:

- Compare the lengths two objects
$\square$ Describe the difference in length
$\square$ Explain how you know that one object is $\qquad$ units longer than another


## Question Stems and Prompts:

$\checkmark$ Which object is longer?
$\checkmark$ How much longer is this object than the other object?
$\checkmark$ How many inches longer is the $\qquad$ than the $\qquad$ ?
$\checkmark$ How many feet shorter is the $\qquad$ from the $\qquad$ ?

## Vocabulary <br> Spanish Cognates

Tier 3

- measure
- standard units


## Standards Connections

2.MD. $4 \rightarrow$ 2.MD. 5
2.MD. 4 Examples:

Teacher: Choose two pieces of string to measure. How many inches do you think each string is?
Student: I think String A is about 8 inches long. I think string B is only about 4 inches long. It's really short.
Teacher: Measure to see how long each string is. Student measures. What did you notice?
Student: String A is definitely the longest one. It is 10 inches long. String B was only 5 inches long. I was close!
Teacher: How many more inches does your short string need to be so that it is the same length as your long string?
Student: Hmmm. String B is 5 inches. It would need 5 more inches to be 10 inches. 5 and 5 is 10 .
(North Carolina Department of Public Instruction, Unpacked Content, updated July 2013)


Howard County Public School System,
https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.MD. 4

## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 4 Measure to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit.

## Essential Skills and Concepts:

ㅁ Compare the lengths two objects

- Describe the difference in length
$\square$ Explain how you know that one object is $\qquad$ units longer than another


## Question Stems and Prompts:

$\checkmark$ Which object is longer?
$\checkmark$ How much longer is this object than the other object?
$\checkmark$ How many inches longer is the $\qquad$ than the $\qquad$
$\checkmark$ How many feet shorter is the $\qquad$ from the $\qquad$ ?

## Vocabulary

## Spanish Cognates

Tier 3

- measure
- standard units


## Standards Connections

2.MD. $4 \rightarrow$ 2.MD. 5
2.MD. 4 Examples:

Teacher: Choose two pieces of string to measure. How many inches do you think each string is?
Student: I think String A is about 8 inches long. I think string B is only about 4 inches long. It's really short.
Teacher: Measure to see how long each string is. Student measures. What did you notice?
Student: String A is definitely the longest one. It is 10 inches long. String B was only 5 inches long. I was close! Teacher: How many more inches does your short string need to be so that it is the same length as your long string?
Student: Hmmm. String B is 5 inches. It would need 5 more inches to be 10 inches. 5 and 5 is 10 .
(North Carolina Department of Public Instruction, Unpacked Content, updated July 2013)


Howard County Public School System,
https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.MD. 4

## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 4 Measure to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit.

## Standard Explanation

Students measure to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit. (2.MD.A.4 $\mathbf{\Delta}$ ). Second graders use inches, feet, yards, centimeters, and meters to compare the lengths of two objects. Students use comparative phrases such as, "It is 2 inches longer," or, "It is shorter by 5 centimeters," to describe the difference in length between the two objects. Students use both the quantity and the unit name to precisely compare length. (Adapted from Arizona 2012 and N. Carolina 2013)

Second Grade students determine the difference in length between two objects by using the same tool and unit to measure both objects. Students choose two objects to measure, identify an appropriate tool and unit, measure both objects, and then determine the differences in lengths. (CA Mathematics Framework, adopted Nov. 6, 2013)

Geometric Measurement Progression Information:
Second graders also learn to combine and compare lengths using arithmetic operations. That is, they can add two lengths to obtain the length of the whole and subtract one length from another to find out the difference in lengths. For example, they can use a simple unit ruler or put a length of connecting cubes together to measure first one modeling clay "snake," then another, to find the total of their lengths. The snakes can be laid along a line, allowing students to compare the measurement of that length with the sum of the two measurements.

## 2.MD.A Measure and estimate lengths in standard units.

2.MD. 4 Measure to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit.

## Standard Explanation

Students measure to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit. (2.MD.A.4 4 ). Second graders use inches, feet, yards, centimeters, and meters to compare the lengths of two objects. Students use comparative phrases such as, "It is 2 inches longer," or, "It is shorter by 5 centimeters," to describe the difference in length between the two objects. Students use both the quantity and the unit name to precisely compare length. (Adapted from Arizona 2012 and N. Carolina 2013)

Second Grade students determine the difference in length between two objects by using the same tool and unit to measure both objects. Students choose two objects to measure, identify an appropriate tool and unit, measure both objects, and then determine the differences in lengths. (CA Mathematics Framework, adopted Nov. 6, 2013)

## Geometric Measurement Progression Information:

Second graders also learn to combine and compare lengths using arithmetic operations. That is, they can add two lengths to obtain the length of the whole and subtract one length from another to find out the difference in lengths. For example, they can use a simple unit ruler or put a length of connecting cubes together to measure first one modeling clay "snake," then another, to find the total of their lengths. The snakes can be laid along a line, allowing students to compare the measurement of that length with the sum of the two measurements.

## 2.MD.B Relate addition and subtraction to length.

2.MD. 5 Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem.

## Essential Skills and Concepts:

$\square$ Solve length word problems using addition and subtraction within 100
$\square$ Represent word problems using drawings or equations
$\square$ Write an equation to match the word problem using a symbol for the unknown

## Question Stems and Prompts:

$\checkmark$ If a puppy was 12 inches long and now it is 22 inches long how many inches long did it grow?
$\checkmark$ A string was 25 cm long. I cut off $\underline{12 \mathrm{~cm} \text {. How long is the }}$ string now?
$\checkmark \quad$ Write an equation for the word problem. What do the parts of your equation represent?
$\checkmark$ Describe how your drawing represents the problem.

## Vocabulary

Tier 2

- represent
- symbol

Tier 3

- length
- addition
- subtraction
- units
- equation
- number line línea de números
- open number line
- tape diagram


## Standards Connections

2.MD. 5 - 2.MD.6, 2.OA. 1
2.MD. 5 Example:


Student B: My equation is $23-14=\ldots$ since I thought about what the difference was between Kate and Lilly. I broke up 14 into 10 and 4 . I know that 23 minus 10 is 13 . Then, I broke up the 4 into 3 and 1.13 minus 3 is 10 . Then, I took one more away. That left me with 9 . So, Lilly jumped 9 inches more than Kate. That seems to make sense since 23 is almost 10 more than 14. $23-14=$ 9. (MP.2, MP. 7 and MP.8)
(California Mathematics Framework, November 6, 2013)

## 2.MD.B Relate addition and subtraction to length.

2.MD. 5 Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem.

## Essential Skills and Concepts:

$\square$ Solve length word problems using addition and subtraction within 100
$\square$ Represent word problems using drawings or equations
$\square$ Write an equation to match the word problem using a symbol for the unknown

## Question Stems and Prompts:

$\checkmark$ If a puppy was 12 inches long and now it is 22 inches long how many inches long did it grow?
$\checkmark$ A string was 25 cm long. I cut off 12 cm . How long is the string now?
$\checkmark$ Write an equation for the word problem. What do the parts of your equation represent?
$\checkmark$ Describe how your drawing represents the problem.

## Vocabulary

Tier 2

- represent
- symbol

Tier 3

- length
- addition
- subtraction sustracción
- units unidades
- equation ecuación
- number line línea de números
- open number line
- tape diagram


## Standards Connections

2.MD. 5 - 2.MD.6, 2.OA. 1

## 2.MD. 5 Example:


(California Mathematics Framework, November 6, 2013)

## 2.MD.B Relate addition and subtraction to length.

2.MD. 5 Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem.

## Standard Explanation

Students apply the concept of length to solve addition and subtraction problems. Word problems should refer to the same unit of measure (California Mathematics Framework, November 6, 2013).

Equations may vary depending on students' interpretation of the task (North Carolina Unpacking Document, July 2013).

## 2.MD.B Relate addition and subtraction to length.

2.MD. 5 Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem.

## Standard Explanation

Students apply the concept of length to solve addition and subtraction problems. Word problems should refer to the same unit of measure (California Mathematics Framework, November 6, 2013).

Equations may vary depending on students’ interpretation of the task (North Carolina Unpacking Document, July 2013).

## 2.MD.B Relate addition and subtraction to length.

2.MD. 6 Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers $0,1,2, \ldots$, and represent wholenumber sums and differences within 100 on a number line diagram.

## Essential Skills and Concepts:

$\square$ Create equally spaced points on a number line for whole numbers
$\square$ Use a number line to add and subtract to solve length problems
$\square$ Represent answers to addition and subtraction questions on the number line

## Question Stems and Prompts:

$\checkmark$ How can you represent this addition/subtraction problem using a number line?
$\checkmark$ Using a number line, explain your answer to the problem.

## Vocabulary

Tier 2

- equal
- diagram
- difference

Tier 3

- sums
- addition
- subtraction sustracción
- number line línea de números
- open number line
- tape diagram


## Standards Connections

2.MD. 6 - 2.MD.9, 2.MD. $6 \rightarrow$ 3.NF. 2

## 2.MD. 6 Examples:

Example: There were 27 students on the bus. 19 got off the bus. How many students are on the bus?
Student A: I used a number line. I started at 27. I broke up 19 into 10 and 9. That way, I could take a jump of 10. I landed on 17. Then I broke the 9 up into 7 and 2. I took a jump of 7. That got me to 10. Then I took a jump of 2 . That's 8 . So, there are 8 students now on the bus.


Student B: I used a number line. I saw that 19 is really close to 20 . Since 20 is a lot easier to work with, I took a jump of 20 . But, that was one too many. So, I took a jump of 1 to make up for the extra. I landed on 8. So, there are 8 students on the bus.

(North Carolina Unpacking Document, July 2013)

## 2.MD.B Relate addition and subtraction to length.

2.MD. 6 Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers $0,1,2, \ldots$, and represent wholenumber sums and differences within 100 on a number line diagram.

## Essential Skills and Concepts:

$\square$ Create equally spaced points on a number line for whole numbers
$\square$ Use a number line to add and subtract to solve length problems
$\square$ Represent answers to addition and subtraction questions on the number line

## Question Stems and Prompts:

$\checkmark$ How can you represent this addition/subtraction problem using a number line?
$\checkmark$ Using a number line, explain your answer to the problem.

## Vocabulary

Tier 2

- equal
- diagram
- difference

Tier 3

- sums
- addition adición
- subtraction sustracción
- number line línea de números
- open number line
- tape diagram


## Standards Connections

2.MD. 6 - 2.MD.9, 2.MD. $6 \rightarrow$ 3.NF. 2

## 2.MD. 6 Examples:

Example: There were 27 students on the bus. 19 got off the bus. How many students are on the bus?
Student A: I used a number line. I started at 27. I broke up 19 into 10 and 9. That way, I could take a jump of 10. I landed on 17. Then I broke the 9 up into 7 and 2. I took a jump of 7. That got me to 10. Then I took a jump of 2 . That's 8 . So, there are 8 students now on the bus.


Student B: I used a number line. I saw that 19 is really close to 20 . Since 20 is a lot easier to work with, I took a jump of 20 . But, that was one too many. So, I took a jump of 1 to make up for the extra. I landed on 8. So, there are 8 students on the bus.

$$
\begin{gathered}
27-20=7 \\
7+1=8
\end{gathered}
$$


(North Carolina Unpacking Document, July 2013)

## 2.MD.B Relate addition and subtraction to length.

2.MD. 6 Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers $0,1,2, \ldots$, and represent wholenumber sums and differences within 100 on a number line diagram.

## Standard Explanation

Students represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers $0,1,2 \ldots$ and represent wholenumber sums and differences within 100 on a number line diagram (California Mathematics Framework, November 6, 2013).

They build upon their experiences with open number lines to create number lines with evenly spaced points. They recognize the similarities between a number line and a ruler (North Carolina Unpacking Document, July 2013).

## 2.MD. 6 Illustrative Task:

- Frog and Toad on the Number Line, https://www.illustrativemathematics.org/illustrations/108 1
One day, Frog and Toad were sitting together on a lily pad. Some lily pads were in a line across the pond.


In the morning, Frog hopped three lily pads away. In the afternoon, he hopped two more away. In the evening, he hopped another two more.

Toad hopped four lily pads away in the moming. He rested in the afternoon and continued three further in the evening. Frog said,

Toad, we ended up at the same place!
Show each of their journeys on a number line, starting at 0 . Use different colors for the moming, afternoon, and evening hops. Write a number sentence that reflects that they ended up at the same place.

## Solution: Sample solution

Frog's journey is shown on the top number line and Toad's journey is shown on the bottom number line:


The number sentence

$$
3+2+2=4+3
$$

shows that Frog and Toad ended up at the same place.

## 2.MD.B Relate addition and subtraction to length.

2.MD. 6 Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers $0,1,2, \ldots$, and represent wholenumber sums and differences within 100 on a number line diagram.

## Standard Explanation

Students represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers $0,1,2 \ldots$ and represent wholenumber sums and differences within 100 on a number line diagram (California Mathematics Framework, November 6, 2013).

They build upon their experiences with open number lines to create number lines with evenly spaced points. They recognize the similarities between a number line and a ruler (North Carolina Unpacking Document, July 2013).

## 2.MD. 6 Illustrative Task:

- Frog and Toad on the Number Line, https://www.illustrativemathematics.org/illustrations/108 1

One day, Frog and Toad were sitting together on a lily pad. Some lily pads were in a line across the pond.


In the morning, Frog hopped three lily pads away. In the afternoon, he hopped two more away. In the evening, he hopped another two more.

Toad hopped four lily pads away in the moming. He rested in the afternoon and continued three further in the evening. Frog said,

Toad, we ended up at the same place!

Show each of their jourmeys on a number line, starting at 0 . Use different colors for the moming, afternoon, and evening hops. Write a number sentence that reflects that they ended up at the same place.

## Solution: Sample solution

Frog's journey is shown on the top number line and Toad's journey is shown on the bottom number line:


The number sentence

$$
3+2+2=4+3
$$

shows that Frog and Toad ended up at the same place.

## 2.MD.C Work with time and money.

2.MD. 7 Tell and write time from analog and digital clocks to the nearest five minutes, using a.m. and p.m. Know relationships of time (e.g., minutes in an hour, days in a month, weeks in a year). CA

## Essential Skills and Concepts:

- Tell time to the nearest five minutes from analog and digital clocks
$\square$ Use a.m. and p.m., giving examples of each
$\square$ Write time to the nearest five minutes from analog and digital clocks
$\square$ Understand and know relationships of time


## Question Stems and Prompts:

$\checkmark$ What time is it? Is it am or pm? How do you know?
$\checkmark$ Write the time on this clock?
$\checkmark$ How many hours in a day? Days in a week?
$\checkmark$ How many minutes in an hour? Two hours?
$\checkmark$ Show the time on the digital clock on an analog clock by drawing the hands in the correct places.

## Vocabulary

Tier 2

- analog
- digital

Tier 3

- a.m.
- p.m.
- hour
- minute


## Spanish Cognates

análogo
digital
hora
minuto

## 2.MD. 7 Examples:



Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/Assessi ng+2.MD. 7

## 2.MD.C Work with time and money.

2.MD. 7 Tell and write time from analog and digital clocks to the nearest five minutes, using a.m. and p.m. Know relationships of time (e.g., minutes in an hour, days in a month, weeks in a year). CA

## Essential Skills and Concepts:

- Tell time to the nearest five minutes from analog and digital clocks
$\square$ Use a.m. and p.m., giving examples of each
$\square$ Write time to the nearest five minutes from analog and digital clocks
$\square$ Understand and know relationships of time
Question Stems and Prompts:
$\checkmark$ What time is it? Is it am or pm? How do you know?
$\checkmark$ Write the time on this clock?
$\checkmark$ How many hours in a day? Days in a week?
$\checkmark$ How many minutes in an hour? Two hours?
$\checkmark$ Show the time on the digital clock on an analog clock by drawing the hands in the correct places.


## Vocabulary

Tier 2

- analog
- digital

Tier 3

- a.m.
- p.m.
- hour
- minute


## Spanish Cognates

análogo digital
2.MD. 7 Examples:


Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/Assessi ng+2.MD. 7

## 2.MD.C Work with time and money.

2.MD. 7 Tell and write time from analog and digital clocks to the nearest five minutes, using a.m. and p.m. Know relationships of time (e.g., minutes in an hour, days in a month, weeks in a year). CA

## Standard Explanation

In first grade, students learned to tell time to the nearest hour and half-hour. In second grade students tell time to the nearest five minutes (2.MD.7 © ). Students can make connections between skip counting by 5 s (2.NBT. $2 \mathbf{A}$ ) and 5minute intervals on the clock. Students work with both digital and analog clocks. They recognize time in both formats and communicate their understanding of time using both numbers and language.

Second grade students understand that there are two cycles of twelve hours in a day-a.m. and p.m. A daily journal can help students make real-world connections and understand the difference between these two cycles (California Mathematics Framework, November 6, 2013).

```
Focus, Coherence, and Rigor:
Students understanding and use of skip counting by 5s and 10s (2.NBT.24) can also suppoor
telling and witing time to the nearest five minutes (2.MD. 17). Sudents notice the patterm of
numbers and applythis understandingto time (MP.7)
```


## 2.MD. 7 Illustrative Task:

```
- Ordering Time, https://www.illustrativemathematics.org/illustrations/106 \(\underline{9}\)
```


## MATERIALS

- Sets of 3-6 "analog clock cards," enough for each student
- Sets of 3-6 "digital clock cards," enough for each student
- Paper and pencil


## ACTIONS

Students will work individually or in pairs so they can compare their orderings. Students should start with the analog clocks. They arrange they clocks in order of increasing time and then the can write the times in increasing order on their paper. Once they have arranged the first set, they can move onto the set of digital times. The teacher should be walking around at this time checking student progress.

If students finish early, they can get another set of cards. The card sets attached to this task get increasingly difficult, so students who find the first sets easy will be challenged by other sets.


## 2.MD.C Work with time and money.

2.MD. 7 Tell and write time from analog and digital clocks to the nearest five minutes, using a.m. and p.m. Know relationships of time (e.g., minutes in an hour, days in a month, weeks in a year). CA

## Standard Explanation

In first grade, students learned to tell time to the nearest hour and half-hour. In second grade students tell time to the nearest five minutes (2.MD.7 $\mathbf{\Delta}$ ). Students can make connections between skip counting by 5 s (2.NBT. $2 \mathbf{\Delta}$ ) and 5minute intervals on the clock. Students work with both digital and analog clocks. They recognize time in both formats and communicate their understanding of time using both numbers and language.

Second grade students understand that there are two cycles of twelve hours in a day-a.m. and p.m. A daily journal can help students make real-world connections and understand the difference between these two cycles (California Mathematics Framework, November 6, 2013).

## Focus, Cobereence, and Rigor: <br> Students undestananing and sse of skip couning by 5 s and 10 S (2.NBT.24) can also support  numbers and apply this understandingototime (MP.7)

## 2.MD. 7 Illustrative Task:

- Ordering Time,
https://www.illustrativemathematics.org/illustrations/106
$\underline{9}$


## MATERIALS

- Sets of 3-6 "analog clock cards," enough for each student
- Sets of 3-6 "digital clock cards," enough for each student
- Paper and pencil


## ACTIONS

Students will work individually or in pairs so they can compare their orderings. Students should start with the analog clocks. They arrange they clocks in order of increasing time and then the can write the times in increasing order on their paper. Once they have arranged the first set, they can move onto the set of digital times. The teacher should be walking around at this time checking student progress.

If students finish early, they can get another set of cards. The card sets attached to this task get increasingly difficult, so students who find the first sets easy will be challenged by other sets.


## 2.MD.C Work with time and money

2.MD. 8 Solve word problems involving dollar bills, quarters, dimes, nickels, and pennies, using $\$$ and $\Varangle$ symbols appropriately. Example: If you have 2 dimes and 3 pennies, how many cents do you have?

## Essential Skills and Concepts:

$\square$ Identify and name coins and bills, including their values
$\square$ Solve word problems about money
$\square$ Use the symbols $\$$ and $\phi$ correctly
$\square$ Count money and represent values in different ways

## Question Stems and Prompts:

$\checkmark$ If you had __quaters and $\qquad$ nickels how many cents would you have?
$\checkmark$ If you had __ quarters, __dimes, and ___ pennies. How much money would you have?

## Vocabulary

Spanish Cognates
Tier 2

- money
- value valor

Tier 3

- dollar
dólar
- quarter
- dime
- nickel
- penny
- cent centavo


## Standards Connections

2.MD. 8 - 2.OA. 1

## 2.MD. 8 Examples:

| Example: How many different ways can you make $37 \%$ using pennies, nickels, dimes, and |
| :--- |
| quarters? |
| Example: How many different ways can you make 12 dollars using $\$ 1, \$ 5$, and $\$ 10$ bills? |

(Adapted from Arizona 2012 and N. Carolina 2013)

## 2.MD. 8 Illustrative Task:

- Alexander, Who Used to be Rich Last Sunday https://www.illustrativemathematics.org/illustrations/131 4
- Alexander, Who Used to be Rich Last Sunday by Judith Viorst

- Plastic coins
- Labels for items Alexander spent his money on (attached)
- Paper coins (attached)
- Scissors, glue, and construction paper


## 2.MD.C Work with time and money

2.MD. 8 Solve word problems involving dollar bills, quarters, dimes, nickels, and pennies, using $\$$ and $¢$ symbols appropriately. Example: If you have 2 dimes and 3 pennies, how many cents do you have?

## Essential Skills and Concepts:

$\square$ Identify and name coins and bills, including their values
$\square$ Solve word problems about money
$\square$ Use the symbols \$ and $\phi$ correctly
$\square$ Count money and represent values in different ways

## Question Stems and Prompts:

$\checkmark$ If you had $\qquad$ quaters and $\qquad$ nickels how many cents would you have?
$\checkmark$ If you had $\qquad$ quarters, $\qquad$ dimes, and $\qquad$ pennies. How much money would you have?

## Vocabulary

## Spanish Cognates

Tier 2

- money
- value valor

Tier 3

- dollar
- quarter
- dime
- nickel
- penny
- cent
centavo


## Standards Connections

2.MD. 8 - 2.OA. 1

## 2.MD. 8 Examples:

Example: How many different ways can you make $37 \phi$ using pennies, nickels, dimes, and quarters?

Example: How many different ways can you make 12 dollars using $\$ 1, \$ 5$, and $\$ 10$ bills?
(Adapted from Arizona 2012 and N. Carolina 2013)

## 2.MD. 8 Illustrative Task:

- Alexander, Who Used to be Rich Last Sunday https://www.illustrativemathematics.org/illustrations/131 4
- Alexander, Who Used to be Rich Last Sunday by Judith Viorst

- Plastic coins
- Labels for items Alexander spent his money on (attached)
- Paper coins (attached)
- Scissors, glue, and construction paper


## 2.MD.C. 8

## Standard Explanation

Students solve word problems involving dollars or cents (2.MD.8). Students identify, count, recognize, and use coins and bills in and out of context. They should have opportunities to make equivalent amounts using both coins and bills. "Dollar bills" should include denominations up to one hundred ( $\$ 1, \$ 5, \$ 10, \$ 20, \$ 100$ ). Note that students in second grade do not express money amounts using decimal points.

Just as students learn that a number (38) can be represented different ways ( 3 tens and 8 ones; 2 tens and 18 ones) and still remain the same amount (38), students can apply this understanding to money. For example, 25 cents could be represented as a quarter, two dimes and a nickel, or 25 pennies, all of which have the same value. Building the concept of equivalent worth takes time and students will need numerous opportunities to create and count different sets of coins and to recognize the "purchase power" of coins (a nickel can buy the same things as 5 pennies).

As teachers provide students with opportunities to explore coin values ( 25 cents), actual coins ( 2 dimes, 1 nickel), and drawings of circles that have values indicated, students gradually learn to mentally give each coin in a set a value, place a random set of coins in order, use mental math, add on to find differences, and skip count to determine the total amount (California Mathematics Framework, November 6, 2013).

## 2.MD. 8 Illustrative Tasks:

## - Jamir's Penny Jar,

 https://www.illustrativemathematics.org/illustrations/1071Jamir has collected some pennies in a jar. Recently, he added coins other than pennies to his jar. Jamir reached his hand into the jar and pulled out this combination:


[^9]
## 2.MD.C. 8

## Standard Explanation

Students solve word problems involving dollars or cents (2.MD.8). Students identify, count, recognize, and use coins and bills in and out of context. They should have opportunities to make equivalent amounts using both coins and bills. "Dollar bills" should include denominations up to one hundred ( $\$ 1, \$ 5, \$ 10, \$ 20, \$ 100$ ). Note that students in second grade do not express money amounts using decimal points.

Just as students learn that a number (38) can be represented different ways ( 3 tens and 8 ones; 2 tens and 18 ones) and still remain the same amount (38), students can apply this understanding to money. For example, 25 cents could be represented as a quarter, two dimes and a nickel, or 25 pennies, all of which have the same value. Building the concept of equivalent worth takes time and students will need numerous opportunities to create and count different sets of coins and to recognize the "purchase power" of coins (a nickel can buy the same things as 5 pennies).

As teachers provide students with opportunities to explore coin values ( 25 cents), actual coins ( 2 dimes, 1 nickel), and drawings of circles that have values indicated, students gradually learn to mentally give each coin in a set a value, place a random set of coins in order, use mental math, add on to find differences, and skip count to determine the total amount (California Mathematics Framework, November 6, 2013).

## 2.MD. 8 Illustrative Tasks:

- Jamir's Penny Jar, https://www.illustrativemathematics.org/illustrations/1071
Jamir has collected some pennies in a jar. Recently, he added coins other than pennies to his jar. Jamir reached his hand into the jar and pulled out this combination:

a. Jamir wants to count the total value of these coins. What coin do you suggest he start with? Why would Jamir want to start counting with this coin?
b. What is the total value of these coins? Write a number sentence that represents the total value of the coins.
c. Jamir reached into the jar again and was surprised to pull out a different combination of coins with the same total value as before. Draw a collection of coins that Jamir could have pulled from the jar. Write a number sentence that represents the total value of the coins.
- Visiting the Arcade, https://www.illustrativemathematics.org/illustrations/1296
Amy went to the arcade. At the arcade, people can buy tokens to use for the games.
a. Amy paid $\$ 5$ to get some tokens. Show two different ways she could have paid using some bills and some coins.
b. Amy finished playing games. She has 4 tokens left over. Can she use these at the grocery store to buy some food? Why or why not?
c. The arcade trades tokens for 15 cents. How much money could Amy trade for her 4 tokens? Can she use these at the grocery store to buy some food? Why or why not?


## 2.MD.D Represent and interpret data.

2.MD. 9 Generate measurement data by measuring lengths of several objects to the nearest whole unit, or by making repeated measurements of the same object. Show the measurements by making a line plot, where the horizontal scale is marked off in whole-number units.

## Essential Skills and Concepts:

$\square$ Generate data by measuring lengths of objects
$\square$ Create a line plot
$\square$ Represent data on a line plot

## Question Stems and Prompts:

$\checkmark$ Measure the items in your pencil box. Create a line plot to illustrate your data.
$\checkmark$ Measure these 5 different books. Draw the data points on this line plot.
$\checkmark$ How many objects have the same measurement?
$\checkmark$ How many objects measure 2inches?

## Vocabulary

Tier 2

- generate
- object
- scale
- horizontal


## Spanish Cognates

Tier 3

- line plot
- data
- unit

> generar
objeto
escala
horizontal

- measure


## Standards Connections

2.MD. 9 - 2.MD. 6

## 2.MD. 9 Illustrative Tasks:

- The Longest Walk, https://www.illustrativemathematics.org/illustrations/486
a. Pick two points on the outside borders of the United States map (excluding Hawaii and
Alaska) so that the line between them stays within the borders. Draw the line. How far Alaska) so that the line between them stays within the borders. Draw the line. How tar
apart are the points? Measure the length of the line to find out. Do this 10 times and mak apart are the points? Me
b. Starting anywhere on the map of the United States and drawing in a straight line until
hitting a border, what is the longest line you can draw? it might help to ask your classmates what lengths they found as well.

- Growing Bean Plants, https://www.illustrativemathematics.org/illustrations/493



## 2.MD.D Represent and interpret data.

2.MD. 9 Generate measurement data by measuring lengths of several objects to the nearest whole unit, or by making repeated measurements of the same object. Show the measurements by making a line plot, where the horizontal scale is marked off in whole-number units.

## Essential Skills and Concepts:

$\square$ Generate data by measuring lengths of objects
$\square$ Create a line plot
$\square$ Represent data on a line plot

## Question Stems and Prompts:

$\checkmark$ Measure the items in your pencil box. Create a line plot to illustrate your data.
$\checkmark$ Measure these 5 different books. Draw the data points on this line plot.
$\checkmark$ How many objects have the same measurement?
$\checkmark$ How many objects measure 2inches?

## Vocabulary

## Spanish Cognates

Tier 2

- generate
- object
- scale
- horizontal

Tier 3

- line plot
- data
- unit
- measure


## Standards Connections

2.MD. 9 - 2.MD. 6

## 2.MD. 9 Illustrative Tasks:

- The Longest Walk, https://www.illustrativemathematics.org/illustrations/486
a. Pick two points on the outside borders of the United States map (excluding Hawaii and
Alaska) so that the line between them stays within the borders. Draw the line. How far
apart are the points? Measwre the length of the line to find out. Do this 10 times and apart are the points? Me
a lime-plot or your data.
b. Starting anywhere on the map of the United States and drawing in a straight line until hitting a border what is the lorigest line you can drawi? it might help to ask your
classmates what lengths they found as well.

- Growing Bean Plants, https://www.illustrativemathematics.org/illustrations/493 weok 1 Line piot:



## 2.MD.D. 9

## Standard Explanation

Students use the measurement skills learned in earlier standards to measure objects and create measurement data (2.MD.9). For example they measure objects in their desk to the nearest inch, display the data collected on a line plot, and answer related questions. Line plots are first introduced in this grade level. A line plot can be thought of as plotting data on a number line. For example:


Representing and interpreting data to solve problems also develops mathematical practices such making sense of problems (MP.1), reasoning quantitatively (MP.2), justifying conclusions (MP.3), appropriate use of tools (MP.5), attention to precision (MP.6), and evaluating the reasonableness of results (MP. 8) (California Mathematics Framework, November 6, 2013).

## 2.MD. 9 Examples:

## 2.MD.D. 9

## Standard Explanation

Students use the measurement skills learned in earlier standards to measure objects and create measurement data (2.MD.9). For example they measure objects in their desk to the nearest inch, display the data collected on a line plot, and answer related questions. Line plots are first introduced in this grade level. A line plot can be thought of as plotting data on a number line. For example:


Representing and interpreting data to solve problems also develops mathematical practices such making sense of problems (MP.1), reasoning quantitatively (MP.2), justifying conclusions (MP.3), appropriate use of tools (MP.5), attention to precision (MP.6), and evaluating the reasonableness of results (MP. 8) (California Mathematics Framework, November 6, 2013).

## 2.MD. 9 Examples:



Use the information below to fill in the line plot.

| 3 boys: 10 feet | 3 girrs: 10 feet | 2 boys: 5 feet |
| :--- | :--- | :--- |
| 2 boys: 15 feet | 1 girl: 5 feet | 4 girls: 15 feet |

How Far Kids Jumped in the Standing Long Jump at P.E.
Navi:

How many kids jumped more than 5 feet into the water?

| X |  |  | x |
| :---: | :---: | :---: | :---: |
| X | X |  | X |
| X | X |  | X |
| X | X | x | X |
| x | X | x | x |
| 3 | 5 | 8 | 10 |

Number of Feet into the Water Kids Jumped from the Diving Board

Howard County Public School System,
https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.MD. 9

[^10]
## 2.MD.D Represent and interpret data

2.MD. 10 Draw a picture graph and a bar graph (with singleunit scale) to represent a data set with up to four categories. Solve simple put-together, take-apart, and compare problems ${ }^{4}$ using information presented in a bar graph.

## Essential Skills and Concepts:

$\square$ Draw and label a bar graph
$\square$ Draw and label a picture graph
$\square$ Solve problems using the data on the graphs

## Question Stems and Prompts:

$\checkmark$ How many more $\qquad$ is there then $\qquad$ ?
$\checkmark$ How many __ and __ are there together?
$\checkmark$ Which category received the least amount of votes?
$\checkmark$ Which category received the greatest amount of votes?

## Vocabulary

Spanish Cognates
Tier 2

- category
categoría
- compare comprarar
- information
información
- key

Tier 3

- bar graph
- picture graph
- data datos
- unit unidad


## Standards Connections

2.MD. 10 - 2.OA. 1

## 2.MD. 10 Examples:



Thereare students altogether
How many students voted for cats?
$\qquad$
$\qquad$
How mony voted for cats ond birds togethere?

Use the following data to make a picture graph.

| Favorite Fruit |  |
| :---: | :---: |
| Grapes | 5 |
| Plums | 9 |
| Peaches | 3 |

Howard County Public School System,
https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.MD. 10

## 2.MD.D Represent and interpret data

2.MD. 10 Draw a picture graph and a bar graph (with singleunit scale) to represent a data set with up to four categories. Solve simple put-together, take-apart, and compare problems ${ }^{4}$ using information presented in a bar graph.

## Essential Skills and Concepts:

$\square$ Draw and label a bar graph
$\square$ Draw and label a picture graph
Solve problems using the data on the graphs

## Question Stems and Prompts:

$\checkmark$ How many more is there then $\qquad$ ?
$\checkmark$ How many __ and __ are there together?
$\checkmark$ Which category received the least amount of votes?
$\checkmark$ Which category received the greatest amount of votes?

## Vocabulary

Tier 2

- category
- compare
- information información
- key

Tier 3

- bar graph
- picture graph
- data datos
- unit unidad


## Standards Connections

2.MD. 10 - 2.OA. 1

## 2.MD. 10 Examples:



Use the following data to make a picture graph.

| Favorite Fruit |  |
| :---: | :---: |
| Grapes | 5 |
| Plums | 9 |
| Peaches | 3 |

Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.MD. 10

[^11]
## 2.MD.D. 10

## Standard Explanation

Students draw a picture graph and a bar graph (with single-unit scale) to represent a data set with up to four categories. They solve simple put-together, take-apart, and compare problems using information presented in a bar graph.

In first grade, students worked with three categories of data. In second grade, students represent data on a picture graph or bar graph (with single-unit scale) and interpret the results. Students organize, represent, and interpret data with up to four categories. In second grade, picture graphs (pictographs) use symbols that represent single units. Pictographs should include a title, categories, category label, key, and data.

Students use data to pose and solve simple one-step addition and subtraction problems. The use of picture graphs and bar graphs to represent a data set (2.MD.D.10) reinforces major work at the grade in the cluster "Represent and solve problems involving addition and subtraction" and provides a context for students to solve related addition and subtraction problems (2.OA.A. $1 \mathbf{\Delta}$ ).

Representing and interpreting data to solve problems also develops mathematical practices such making sense of problems (MP.1), reasoning quantitatively (MP.2), justifying conclusions (MP.3), appropriate use of tools (MP.5), attention to precision (MP.6), and evaluating the reasonableness of results (MP. 8) (California Mathematics Framework, November 6, 2013).
2.MD.10 Example: Students are responsible for purchasing ice cream for an event at school. They decide to collect data to determine which flavors to buy for the event. Students decide on the question, "What is your favorite flavor of ice cream?" and four likely responses, chocolate, vanilla, strawberry, and cherry. Students form two teams and collect information from different classes in their school. Each team decides how to keep track of the data (e.g., tally marks, in a table, check marks). Each team selects either a picture graph or a bar graph to display their data. They create the graph using paper or a computer. Examples of graphs are provided below.


## 2.MD.D. 10

## Standard Explanation

Students draw a picture graph and a bar graph (with single-unit scale) to represent a data set with up to four categories. They solve simple put-together, take-apart, and compare problems using information presented in a bar graph.

In first grade, students worked with three categories of data. In second grade, students represent data on a picture graph or bar graph (with single-unit scale) and interpret the results. Students organize, represent, and interpret data with up to four categories. In second grade, picture graphs (pictographs) use symbols that represent single units. Pictographs should include a title, categories, category label, key, and data.

Students use data to pose and solve simple one-step addition and subtraction problems. The use of picture graphs and bar graphs to represent a data set (2.MD.D.10) reinforces major work at the grade in the cluster "Represent and solve problems involving addition and subtraction" and provides a context for students to solve related addition and subtraction problems (2.OA.A.1 © ).

Representing and interpreting data to solve problems also develops mathematical practices such making sense of problems (MP.1), reasoning quantitatively (MP.2), justifying conclusions (MP.3), appropriate use of tools (MP.5), attention to precision (MP.6), and evaluating the reasonableness of results (MP. 8) (California Mathematics Framework, November 6, 2013).
2.MD.10 Example: Students are responsible for purchasing ice cream for an event at school. They decide to collect data to determine which flavors to buy for the event. Students decide on the question, "What is your favorite flavor of ice cream?" and four likely responses, chocolate, vanilla, strawberry, and cherry. Students form two teams and collect information from different classes in their school. Each team decides how to keep track of the data (e.g., tally marks, in a table, check marks). Each team selects either a picture graph or a bar graph to display their data. They create the graph using paper or a computer. Examples of graphs are provided below.


## 2.G.A Reason with shapes and their attributes.

2.G. 1 Recognize and draw shapes having specified attributes, such as a given number of angles or a given number of equal faces. ${ }^{5}$ Identify triangles, quadrilaterals, pentagons, hexagons, and cubes.

## Essential Skills and Concepts:

$\square$ Recognize that shapes have specified attributes
$\square$ Draw shapes with given attributes
$\square$ Identify triangles, quadrilaterals, pentagons, hexagons, and cubes

## Question Stems and Prompts:

$\checkmark$ What shape is this? How do you know?
$\checkmark$ Draw a shape that has $\qquad$ faces? $\qquad$ sides? Or $\qquad$ vertices?
$\checkmark$ How many faces does a $\qquad$ have?
$\checkmark$ If a shape has no angles, what is it?
$\checkmark$ Draw a shape then describe its attributes.

## Vocabulary

Tier 2

- attribute
- angles
- equal
- draw

Tier 3

- triangle
- quadrilateral
- pentagon
- hexagon
- cube

Spanish Cognates
atributo
ángulos
igual
triángulo
cuadriláteral
pentágono
hexágono
cubo

## Standards Connections

2.G. $1 \rightarrow$ 3.G. 1

## 2.G. 1 Example:

## 2.G.A Reason with shapes and their attributes.

2.G. 1 Recognize and draw shapes having specified attributes, such as a given number of angles or a given number of equal faces. ${ }^{5}$ Identify triangles, quadrilaterals, pentagons, hexagons, and cubes.

## Essential Skills and Concepts:

$\square$ Recognize that shapes have specified attributes
$\square$ Draw shapes with given attributes
$\square$ Identify triangles, quadrilaterals, pentagons, hexagons, and cubes

## Question Stems and Prompts:

$\checkmark$ What shape is this? How do you know?
$\checkmark$ Draw a shape that has __ faces? ___ sides? Or $\qquad$ vertices?
$\checkmark$ How many faces does a $\qquad$ have?
$\checkmark$ If a shape has no angles, what is it?
$\checkmark$ Draw a shape then describe its attributes.

## Vocabulary

Tier 2

- attribute
- angles
- equal
- draw

Tier 3

- triangle
- quadrilateral
- pentagon
- hexagon
- cube


## Spanish Cognates

atributo
ángulos
igual
triángulo
cuadriláteral
pentágono
hexágono
cubo

## Standards Connections

2.G. $1 \rightarrow$ 3.G. 1

## 2.G. 1 Example:

Look at the chart. Fill in the missing boxes.


[^12]
## 2.G.A. 1

## Standard Explanation

Grade one students reasoned about attributes of geometric shapes. A critical area of instruction in second grade is for students to describe and analyze shapes by examining their sides and angles. This work will develop a foundation for understanding area, volume, congruence, similarity, and symmetry in later grades.

Students identify, describe, and draw triangles, quadrilaterals (squares, rectangles and parallelograms, and trapezoids), pentagons, hexagons, and cubes (2.G.1). Pentagons, triangles, and hexagons should appear as both regular (equal sides and equal angles) and irregular. Students recognize all four sided shapes as quadrilaterals. Students use the vocabulary word "angle" in place of "corner," but they do not need to name angle types (e.g. right, acute, obtuse). Shapes should be presented in a variety of orientations and configurations.

As students use attributes to identify and describe shapes they also develop mathematical practices such as analyzing givens and constraints (MP.1), justifying conclusions (MP.3), modeling with mathematics (MP.4) appropriate use of tools (MP.5), attention to precision (MP.6), and looking for a pattern or structure (MP. 7) (California Mathematics Framework, November 6, 2013).


## 2.G. 1 Illustrative Task:

- Polygons, https://www.illustrativemathematics.org/illustrations/150 6
- Color the inside of all the triangles blue.
- Color the inside of all the quadrilaterals red.
- Color the inside of all the pentagons orange.
- Color the inside of all the hexagons green.
- Circle all the shapes that have sides that are equal.



## 2.G.A. 1

## Standard Explanation

Grade one students reasoned about attributes of geometric shapes. A critical area of instruction in second grade is for students to describe and analyze shapes by examining their sides and angles. This work will develop a foundation for understanding area, volume, congruence, similarity, and symmetry in later grades.

Students identify, describe, and draw triangles, quadrilaterals (squares, rectangles and parallelograms, and trapezoids), pentagons, hexagons, and cubes (2.G.1). Pentagons, triangles, and hexagons should appear as both regular (equal sides and equal angles) and irregular. Students recognize all four sided shapes as quadrilaterals. Students use the vocabulary word "angle" in place of "corner," but they do not need to name angle types (e.g. right, acute, obtuse). Shapes should be presented in a variety of orientations and configurations.

As students use attributes to identify and describe shapes they also develop mathematical practices such as analyzing givens and constraints (MP.1), justifying conclusions (MP.3), modeling with mathematics (MP.4) appropriate use of tools (MP.5), attention to precision (MP.6), and looking for a pattern or structure (MP. 7) (California Mathematics Framework, November 6, 2013).


## 2.G. 1 Illustrative Task:

- Polygons, https://www.illustrativemathematics.org/illustrations/150 6
- Color the inside of all the triangles blue.
- Color the inside of all the quadrilaterals red.
- Color the inside of all the pentagons orange.
- Color the inside of all the hexagons green.
- Circle all the shapes that have sides that are equal.



## 2.G.A Reason with shapes and their attributes.

2.G. 2 Partition a rectangle into rows and columns of samesize squares and count to find the total number of them.

## Essential Skills and Concepts:

$\square$ Divide a rectangle into rows and columns
$\square$ Count the number of squares in the array

## Question Stems and Prompts:

$\checkmark$ What is the total number of squares in this rectangle?
$\checkmark$ Break this rectangle into $\qquad$ rows and $\qquad$ columns. How many same size squares did you create?

## Vocabulary

Tier 2

- partition
- row
- columns

Tier 3

- array
- rectangle
- square

Standards Connections
2.G. $2 \rightarrow$ 2.G. 3

## 2.G. 2 Example:

```
Name:
2.G. 2
```

1. How many different rectangles can you make using 12 squares? Draw them below:
2. Label how many squares are in each row and column in each rectangle.

Howard County Public School System,
https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.G.2

## 2.G.A Reason with shapes and their attributes.

2.G. 2 Partition a rectangle into rows and columns of samesize squares and count to find the total number of them.

## Essential Skills and Concepts:

$\square$ Divide a rectangle into rows and columns
$\square$ Count the number of squares in the array

## Question Stems and Prompts:

$\checkmark$ What is the total number of squares in this rectangle?
$\checkmark$ Break this rectangle into $\qquad$ rows and $\qquad$ columns. How many same size squares did you create?

## Vocabulary

Tier 2

- partition
- row
- columns columnas

Tier 3

- array
- rectangle rectángulo
- square


## Standards Connections

2.G. $2 \rightarrow$ 2.G. 3

## 2.G.2 Example:

Name:
2.G.2

1. How many different rectangles can you make using 12 squares? Draw them
below:
2. Label how many squares are in each row and column in each rectangle.

Howard County Public School System, https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.G. 2

## 2.G.A Reason with shapes and their attributes.

2.G. 2 Partition a rectangle into rows and columns of samesize squares and count to find the total number of them.

## Standard Explanation

Students partition a rectangle into rows and columns of same-size squares and count to find the total number of squares. (2.G.2) As students partition rectangles into rows and columns they build a foundation for learning about the area of a rectangle and using arrays for multiplication.

An interactive whiteboard or manipulatives such as square tiles, cubes, or other square-shaped objects can be used to help students partition rectangles (MP.5) (California Mathematics Framework, November 6, 2013).


## 2.G.A Reason with shapes and their attributes.

2.G. 2 Partition a rectangle into rows and columns of samesize squares and count to find the total number of them.

## Standard Explanation

Students partition a rectangle into rows and columns of same-size squares and count to find the total number of squares. (2.G.2) As students partition rectangles into rows and columns they build a foundation for learning about the area of a rectangle and using arrays for multiplication.

An interactive whiteboard or manipulatives such as square tiles, cubes, or other square-shaped objects can be used to help students partition rectangles (MP.5) (California Mathematics Framework, November 6, 2013).

| Example: Partition the rectangle into 3 equal rows and 4 equal columns. How can into 3 equal rows? Then into 4 equal columns? Can you do oit in the other order? small squares did you make? | pupartion <br> ow many |
| :---: | :---: |
| Student:" counted 12 squares in this rectiangle. This is a lot like when we counted |  |
| arays by counting 4+4+4=12." |  |
|  |  |

## 2.G.A Reason with shapes and their attributes.

2.G. 3 Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, half of, a third of, etc., and describe the whole as two halves, three thirds, four fourths. Recognize that equal shares of identical wholes need not have the same shape.

## Essential Skills and Concepts:

$\square$ Partition/cut circles and rectangles into equal shares of two, three, or four
$\square$ Identify the shares of the shapes using academic language such as halves, thirds, half of, a third of, etc.

## Question Stems and Prompts:

$\checkmark$ Partition/cut the circle into equal parts?
$\checkmark$ What is this one equal part called?
$\checkmark$ How many equal parts make a whole?

## Vocabulary

Tier 2

- Partition
- equal
- identical
- whole
- part

Tier 3

- half/half of
- third/a third of
- fourth/a fourth of
- quarter/a quarter of
- circle
- rectangle


## Standards Connections

2.G. $3 \rightarrow$ 3.NF. 1

## 2.G. 3 Example:



## 2.G.A Reason with shapes and their attributes.

2.G. 3 Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, half of, a third of, etc., and describe the whole as two halves, three thirds, four fourths. Recognize that equal shares of identical wholes need not have the same shape.

## Essential Skills and Concepts:

$\square$ Partition/cut circles and rectangles into equal shares of two, three, or four
$\square$ Identify the shares of the shapes using academic language such as halves, thirds, half of, a third of, etc.

## Question Stems and Prompts:

$\checkmark$ Partition/cut the circle into $\qquad$ equal parts?
$\checkmark$ What is this one equal part called?
$\checkmark$ How many equal parts make a whole?

## Vocabulary

Tier 2

- Partition
- equal
- identical
- whole
- part

Tier 3

- half/half of
- third/a third of
- fourth/a fourth of
- quarter/a quarter of
- circle
- rectangle


## Spanish Cognates

partición
igual
idéntico
parte

Standards Connections
2.G. $3 \rightarrow$ 3.NF. 1

## 2.G. 3 Example:



| Name:_ (2.6.3) |  |
| :--- | :--- |
| Partition the circles into equal shares. |  |
| A. HALF | D. THIRDS |

## 2.G.A Reason with shapes and their attributes.

2.G. 3 Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, half of, a third of, etc., and describe the whole as two halves, three thirds, four fourths. Recognize that equal shares of identical wholes need not have the same shape.

## Standard Explanation

In first grade students partitioned shapes into halves, fourth and quarters. Second grade students partition circles and rectangles into 2,3 or 4 equal shares (regions). Students explore this concept with paper strips and pictorial representations and work with the vocabulary terms halves, thirds, halves, and fourths. (2.G.3) Students recognize that when they cut a circle into three equal pieces, each piece will equal one third of its original whole and students describe the whole as three thirds. If a circle is cut into four equal pieces, each piece will equal one fourth of its original whole and the whole is described as four fourths.


Circle cut into halves


Circle cut into thirds


Circle NOT cut


Circle cut into fourths

Students should see circles and rectangles partitioned in multiple ways so they learn to recognize that equal shares can be different shapes within the same whole.


As students partition circles and squares and explain their thinking they develop mathematical practices such as making sense of quantities (MP.2), justifying conclusions (MP.3), attending to precision (MP.6), and evaluating the reasonableness of their results (MP. 7). They also develop understandings that will support major work at grade three in the cluster "Develop understanding of fractions as numbers". (Adapted from Arizona 2012 and N. Carolina 2013)

## 2.G.A Reason with shapes and their attributes.

2.G. 3 Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, half of, a third of, etc., and describe the whole as two halves, three thirds, four fourths. Recognize that equal shares of identical wholes need not have the same shape.

## Standard Explanation

In first grade students partitioned shapes into halves, fourth and quarters. Second grade students partition circles and rectangles into 2,3 or 4 equal shares (regions). Students explore this concept with paper strips and pictorial representations and work with the vocabulary terms halves, thirds, halves, and fourths. (2.G.3) Students recognize that when they cut a circle into three equal pieces, each piece will equal one third of its original whole and students describe the whole as three thirds. If a circle is cut into four equal pieces, each piece will equal one fourth of its original whole and the whole is described as four fourths.



Circle cut into thirds


Circle NOT cut into thirds


Circle cut into fourths

Students should see circles and rectangles partitioned in multiple ways so they learn to recognize that equal shares can be different shapes within the same whole.


As students partition circles and squares and explain their thinking they develop mathematical practices such as making sense of quantities (MP.2), justifying conclusions (MP.3), attending to precision (MP.6), and evaluating the reasonableness of their results (MP. 7). They also develop understandings that will support major work at grade three in the cluster "Develop understanding of fractions as numbers". (Adapted from Arizona 2012 and N. Carolina 2013)

## Resources for the CCSS $2^{\text {nd }}$ Grade Bookmarks

California Mathematics Framework, adopted by the California State Board of Education November 6, 2013, http://www.cde.ca.gov/ci/ma/cf/draft2mathfwchapters.as p

Student Achievement Partners, Achieve the Core http://achievethecore.org/, Focus by Grade Level, http://achievethecore.org/dashboard/300/search/1/2/0/1/2/3/4/ 5/6/7/8/9/10/11/12/page/774/focus-by-grade-level

Common Core Standards Writing Team. Progressions for the Common Core State Standards in Mathematics Tucson, AZ: Institute for Mathematics and Education, University of Arizona (Drafts)

- K, Counting and Cardinality; $\mathrm{K}-5$ Operations and Algebraic Thinking (2011, May 29)
- K - 5, Number and Operations in Base Ten (2012, April 21)
- $\mathrm{K}-3$, Categorical Data; Grades $2-5$, Measurement Data* (2011, June 20)
- K - 5, Geometric Measurement (2012, June 23)
- K - 6, Geometry (2012, June 23)
- Number and Operations - Fractions, 3 - 5 (2013, September 19)

Illustrative Mathematics ${ }^{\mathrm{TM}}$ was originally developed at the University of Arizona (2011), nonprofit corporation (2013), Illustrative Tasks, http://www.illustrativemathematics.org/

Student Achievement Partners, Achieve the Core http://achievethecore.org/, Focus by Grade Level, http://achievethecore.org/dashboard/300/search/1/2/0/1/2/3/4/ 5/6/7/8/9/10/11/12/page/774/focus-by-grade-level

North Carolina Department of Public Instruction, Instructional Support Tools for Achieving New Standards, Math Unpacking Standards 2012, http://www.ncpublicschools.org/acre/standards/common-core-tools/ - unmath

Common Core Flipbooks 2012, Kansas Association of Teachers of Mathematics (KATM) http://www.katm.org/baker/pages/common-coreresources.php

## Resources for the CCSS $2^{\text {nd }}$ Grade Bookmarks

California Mathematics Framework, adopted by the California State Board of Education November 6, 2013, http://www.cde.ca.gov/ci/ma/cf/draft2mathfwchapters.as p

Student Achievement Partners, Achieve the Core http://achievethecore.org/, Focus by Grade Level, http://achievethecore.org/dashboard/300/search/1/2/0/1/2/3/4/ 5/6/7/8/9/10/11/12/page/774/focus-by-grade-level

Common Core Standards Writing Team. Progressions for the Common Core State Standards in Mathematics Tucson, AZ: Institute for Mathematics and Education, University of Arizona (Drafts)

- K, Counting and Cardinality; $\mathrm{K}-5$ Operations and Algebraic Thinking (2011, May 29)
- K - 5, Number and Operations in Base Ten (2012, April 21)
- $\mathrm{K}-3$, Categorical Data; Grades $2-5$, Measurement Data* (2011, June 20)
- K-5, Geometric Measurement (2012, June 23)
- K - 6, Geometry (2012, June 23)
- Number and Operations - Fractions, 3 - 5 (2013, September 19)

Illustrative Mathematics ${ }^{\mathrm{TM}}$ was originally developed at the University of Arizona (2011), nonprofit corporation (2013), Illustrative Tasks, http://www.illustrativemathematics.org/

Student Achievement Partners, Achieve the Core http://achievethecore.org/, Focus by Grade Level, http://achievethecore.org/dashboard/300/search/1/2/0/1/2/3/4/ 5/6/7/8/9/10/11/12/page/774/focus-by-grade-level

North Carolina Department of Public Instruction, Instructional Support Tools for Achieving New Standards, Math Unpacking Standards 2012, http://www.ncpublicschools.org/acre/standards/common-core-tools/ - unmath

Common Core Flipbooks 2012, Kansas Association of Teachers of Mathematics (KATM) http://www.katm.org/baker/pages/common-coreresources.php

Arizona's College and Career Ready Standards Mathematics - Kindergarten, Arizona Department of Education - High Academic Standards for Students Arizona's College and Career Ready Standards - Mathematics, State Board Approved June 2010 October 2013 Publication, http://www.azed.gov/azccrs/mathstandards/

Howard County Public School System, Elementary
Mathematics Office, Standards for Mathematical Practice for Parents, Draft 2011,
https://grade3commoncoremath.wikispaces.hcpss.org/file/vie w/SFMP for Parents.docx/286906254/SFMP for Parents.docx

Howard County Public School System, Elementary and Secondary Mathematics Offices, Wiki Content and Resources, Elementary by grade level
https://grade5commoncoremath.wikispaces.hcpss.org/home, and Secondary
https://secondarymathcommoncore.wikispaces.hcpss.org
Long Beach Unified School District, Math Cognates, retrieved on $7 / 14 / 14$, http://www.lbschools.net/Main Offices/Curriculum/Areas/M athematics/XCD/ListOfMathCognates.pdf

A Graph of the Content Standards, Jason Zimba, June 7, 2012, http://tinyurl.com/ccssmgraph

Arizona's College and Career Ready Standards Mathematics - Kindergarten, Arizona Department of Education - High Academic Standards for Students Arizona's College and Career Ready Standards - Mathematics, State Board Approved June 2010 October 2013 Publication, http://www.azed.gov/azccrs/mathstandards/

Howard County Public School System, Elementary Mathematics Office, Standards for Mathematical Practice for Parents, Draft 2011, https://grade3commoncoremath.wikispaces.hcpss.org/file/vie w/SFMP for Parents.docx/286906254/SFMP for Parents.docx

Howard County Public School System, Elementary and Secondary Mathematics Offices, Wiki Content and Resources, Elementary by grade level https://grade5commoncoremath.wikispaces.hcpss.org/home, and Secondary
https://secondarymathcommoncore.wikispaces.hcpss.org
Long Beach Unified School District, Math Cognates, retrieved on $7 / 14 / 14$, http://www.lbschools.net/Main Offices/Curriculum/Areas/M athematics/XCD/ListOfMathCognates.pdf

A Graph of the Content Standards, Jason Zimba, June 7, 2012, http://tinyurl.com/ccssmgraph


[^0]:    ${ }^{2}$ See standard 1.OA. 6 for a list of mental strategies.

[^1]:    ${ }^{3}$ Explanations may be supported by drawings or objects.

[^2]:    ${ }^{3}$ Explanations may be supported by drawings or objects.

[^3]:    ${ }^{3}$ Explanations may be supported by drawings or objects.

[^4]:    ${ }^{3}$ Explanations may be supported by drawings or objects.

[^5]:    ${ }^{3}$ Explanations may be supported by drawings or objects.

[^6]:    ${ }^{3}$ Explanations may be supported by drawings or objects.

[^7]:    Howard County Public School System,
    https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.MD.3

[^8]:    Howard County Public School System,
    https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.MD. 3

[^9]:    a. Jamir wants to count the total value of these coins. What coin do you suggest he start with? Why would Jamir want to start counting with this coin?
    b. What is the total value of these coins? Write a number sentence that represents the total value of the
    coins. coins.
    c. Jamir reached into the jar again and was surprised to pull out a different combination of coins with the same total value as before. Draw a collection of coins that Jamir could have pulled from the jar. Write
    a number sentence that represents the total value of the coins.

    - Visiting the Arcade, https://www.illustrativemathematics.org/illustrations/1296

    Amy went to the arcade. At the arcade, people can buy tokens to use for the games.
    a. Amy paid $\$ 5$ to get some tokens. Show two different ways she could have paid using some bills and some coins.
    b. Amy finished playing games. She has 4 tokens left over. Can she use these at the grocery store to buy some food? Why or why not?
    c. The arcade trades tokens for 15 cents. How much money could Amy trade for her 4 tokens? Can she use these at the grocery store to buy some food? Why or why not?

[^10]:    Howard County Public School System,
    https://grade2commoncoremath.wikispaces.hcpss.org/Assessing+2.MD. 9

[^11]:    ${ }^{4}$ See Glossary, Table 1.

[^12]:    ${ }^{5}$ Sizes are compared directly or visually, not compared by measuring.

