



Mathematics Bookmarks

*Standards Reference to Support
Planning and Instruction*



Kindergarten

Tulare County
Office of Education

Tim A. Hire, County Superintendent of Schools



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Grade-Level Introduction

In Kindergarten, instructional time should focus on two critical areas: (1) representing, relating, and operating on whole numbers, initially with sets of objects; and (2) describing shapes and space. More learning time in Kindergarten should be devoted to number than to other topics.

- (1) Students use numbers, including written numerals, to represent quantities and to solve quantitative problems, such as counting objects in a set; counting out a given number of objects; comparing sets or numerals; and modeling simple joining and separating situations with sets of objects, or eventually with equations such as $5 + 2 = 7$ and $7 - 2 = 5$. (Kindergarten students should see addition and subtraction equations, and student writing of equations in kindergarten is encouraged, but it is not required.) Students choose, combine, and apply effective strategies for answering quantitative questions, including quickly recognizing the cardinalities of small sets of objects, counting and producing sets of given sizes, counting the number of objects in combined sets, or counting the number of objects that remain in a set after some are taken away.
- (2) Students describe their physical world using geometric ideas (e.g., shape, orientation, spatial relations) and vocabulary. They identify, name, and describe basic two-dimensional shapes, such as squares, triangles, circles, rectangles, and hexagons, presented in a variety of ways (e.g., with different sizes and orientations), as well as three-dimensional shapes such as cubes, cones, cylinders, and spheres. They use basic shapes and spatial reasoning to model objects in their environment and to construct more complex shapes.

Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

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FLUENCY

In kindergarten through grade six there are individual content standards that set expectations for fluency with computations using the standard algorithm (e.g., “fluently” multiply multi-digit whole numbers using the standard algorithm (5.NBT.5 ▲). Such standards are culminations of progressions of learning, often spanning several grades, involving conceptual understanding (such as reasoning about quantities, the base-ten system, and properties of operations), thoughtful practice, and extra support where necessary.

The word “fluent” is used in the standards to mean “reasonably fast and accurate” and the ability to use certain facts and procedures with enough facility that using them does not slow down or derail the problem solver as he or she works on more complex problems. Procedural fluency requires skill in carrying out procedures flexibly, accurately, efficiently, and appropriately. Developing fluency in each grade can involve a mixture of just knowing some answers, knowing some answers from patterns, and knowing some answers from the use of strategies.

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Explanations of Major, Additional and Supporting Cluster-Level Emphases

Major [m] clusters – areas of intensive focus where students need fluent understanding and application of the core concepts. These clusters require greater emphasis than the others based on the depth of the ideas, the time that they take to master, and/or their importance to future mathematics or the demands of college and career readiness. The ▲ symbol will indicate standards in a Major Cluster in the narrative.

Additional [a] clusters – expose students to other subjects; may not connect tightly or explicitly to the major work of the grade

Supporting [s] clusters – rethinking and linking; areas where some material is being covered, but in a way that applies core understanding; designed to support and strengthen areas of major emphasis.

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Mathematical Practices

1. Make sense of problems and persevere in solving them. Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, “Does this make sense?” They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

In Kindergarten, students begin to build the understanding that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. Real life experiences should be used to support students’ ability to connect mathematics to the world. To help students connect the language of mathematics to their everyday life ask students questions such as “How many students are absent?” or have them gather enough blocks for the students at their table. Younger students may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, “Does this make sense?” or they may try another strategy.

Students:	Teachers:
<ul style="list-style-type: none"> Analyze and explain the meaning of the problem Actively engage in problem solving (Develop, carry out, and refine a plan) Show patience and positive attitudes Ask if their answers make sense Check their answers with a different method 	<ul style="list-style-type: none"> Pose rich problems and/or ask open ended questions Provide wait-time for processing/finding solutions Circulate to pose probing questions and monitor student progress Provide opportunities and time for cooperative problem solving and reciprocal teaching

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2. Reason abstractly and quantitatively. Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to *decontextualize*—to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents—and the ability to *contextualize*, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects.

Younger students begin to recognize that a number represents a specific quantity and to connect the quantity to written symbols. Quantitative reasoning entails creating a representation of a problem while attending to the meanings of the quantities. For example, a student may write the numeral “11” to represent an amount of objects counted, select the correct number card “17” to follow “16” on a vertical calendar with days arranged in tens, or build a pile of counters depending on the number drawn. In addition, kindergarten students begin to draw pictures, manipulate objects, or use diagrams or charts to express quantitative ideas. Students need to be encouraged to answer questions, such as, “How do you know”, which reinforces their reasoning and understanding and helps student develop mathematical language.

Students:	Teachers:
<ul style="list-style-type: none"> • Represent a problem with symbols • Explain their thinking • Use numbers flexibly by applying properties of operations and place value • Examine the reasonableness of their answers/calculations 	<ul style="list-style-type: none"> • Ask students to explain their thinking regardless of accuracy • Highlight flexible use of numbers • Facilitate discussion through guided questions and representations • Accept varied solutions/representations

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3. Construct viable arguments and critique the reasoning of others. Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and—if there is a flaw in an argument—explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments. Students build proofs by induction and proofs by contradiction. CA 3.1 (for higher mathematics only).

Younger students construct arguments using actions and concrete materials, such as objects, pictures, and drawings. They begin to develop their mathematical communication skills as they participate in mathematical discussions involving questions like “How did you get that?” and “Why is that true?” They explain their thinking to others and respond to others’ thinking. They begin to develop the ability to reason and analyze situations as they consider questions such as, “Are you sure...?”, “Do you think that would happen all the time...?”, and “I wonder why...?”

Students:	Teachers:
<ul style="list-style-type: none"> • Make reasonable guesses to explore their ideas • Justify solutions and approaches • Listen to the reasoning of others, compare arguments, and decide if the arguments of others makes sense • Ask clarifying and probing questions 	<ul style="list-style-type: none"> • Provide opportunities for students to listen to or read the conclusions and arguments of others • Establish and facilitate a safe environment for discussion • Ask clarifying and probing questions • Avoid giving too much assistance (e.g., providing answers or procedures)

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4. Model with mathematics. Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

In early grades students begin to represent problem situations in multiple ways (e.g., using numbers, words or mathematical language, objects, acting out, making a chart or list, drawing pictures, or creating equations). For example, a student may use cubes or tiles to show the different number pairs for 5, or place three objects on a ten frame and then determine how many more are needed to “make a ten.” Students rely on manipulatives (or other visual and concrete representations) while solving tasks and record an answer with a drawing or equation.

Students:	Teachers:
<ul style="list-style-type: none"> • Make reasonable guesses to explore their ideas • Justify solutions and approaches • Listen to the reasoning of others, compare arguments, and decide if the arguments of others makes sense • Ask clarifying questions 	<ul style="list-style-type: none"> • Allow time for the process to take place (model, make graphs, etc.) • Model desired behaviors (think alouds) and thought processes (questioning, revision, reflection/written) • Make appropriate tools available • Create an emotionally safe environment where risk taking is valued • Provide meaningful, real world, authentic, performance-based tasks (non traditional work problems)

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5. Use appropriate tools strategically. Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

Younger students begin to consider the available tools when solving a mathematical problem and decide when certain tools might be helpful. For instance, kindergarteners may decide to use linking cubes to represent two quantities and then compare the two representations side-by-side or later, make math drawings of the quantities. Students decide which tools may be helpful to use depending on the problem or task and explain why they use specific mathematical tools.

Students:	Teachers:
<ul style="list-style-type: none"> • Select and use tools strategically (and flexibly) to visualize, explore, and compare information • Use technological tools and resources to solve problems and deepen understanding 	<ul style="list-style-type: none"> • Make appropriate tools available for learning (calculators, concrete models, digital resources, pencil/paper, compass, protractor, etc.) • Use tools with their instruction

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6. Attend to precision. Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

Kindergarten students begin to develop precise communication skills, calculations, and measurements. Students describe their own actions, strategies; and reasoning using grade-level appropriate vocabulary. Opportunities to work with pictorial representations and concrete objects can help students develop understanding and descriptive vocabulary. For example, students analyze and compare two- and three-dimensional shapes and they sort objects based on appearance. While measuring objects iteratively (repetitively), students check to make sure that there are no gaps or overlaps. During tasks involving number sense, students check their work to ensure the accuracy and reasonableness of solutions. Students should be encouraged to answer questions such as, “How do you know your answer is reasonable?”

Students:	Teachers:
<ul style="list-style-type: none"> • Calculate accurately and efficiently • Explain their thinking using mathematics vocabulary • Use appropriate symbols and specify units of measure 	<ul style="list-style-type: none"> • Recognize and model efficient strategies for computation • Use (and challenging students to use) mathematics vocabulary precisely and consistently

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7. Look for and make use of structure. Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see 7×8 equals the well-remembered $7 \times 5 + 7 \times 3$, in preparation for learning about the distributive property. In the expression $x^2 + 9x + 14$, older students can see the 14 as 2×7 and the 9 as $2 + 7$. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see $5 - 3(x - y)^2$ as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y .

Younger students begin to discern a pattern or structure in the number system. For instance, students recognize that $3 + 2 = 5$ and $2 + 3 = 5$. Students notice patterns in counting strategies to build fluency in facts to five. Teachers might ask, “What do you notice when...?” Students may use various strategies to attain fluency such as counting on, counting all, and taking away.

Students:	Teachers:
<ul style="list-style-type: none"> Look for, develop, and generalize relationships and patterns Apply reasonable thoughts about patterns and properties to new situations 	<ul style="list-style-type: none"> Provide time for applying and discussing properties Ask questions about the application of patterns Highlight different approaches for solving problems

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8. Look for and express regularity in repeated

reasoning. Mathematically proficient students notice if calculations are repeated, and look both for general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they repeatedly check whether points are on the line through (1, 2) with slope 3, middle school students might abstract the equation $(y - 2)/(x - 1) = 3$. Noticing the regularity in the way terms cancel when expanding $(x - 1)(x + 1)$, $(x - 1)(x^2 + x + 1)$, and $(x - 1)(x^3 + x^2 + x + 1)$ might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.

In the early grades, students notice repetitive actions in counting, computations, and mathematical tasks. For example, the next number in a counting sequence is one more when counting by ones and ten more when counting by tens (or one more group of ten). Students should be encouraged to answer questions such as “What would happen if...? In the task “There are 8 crayons in the box. Some are red and some are blue. How many of each could there be?” Kindergarten students realize 8 crayons could include 4 of each color ($8 = 4 + 4$), 5 of one color and 3 of another ($8 = 5 + 3$), etc. For each solution, students repeatedly engage in the process of finding two numbers to join together to equal 8.

Students:	Teachers:
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Grade K Overview

Counting and Cardinality

- Know number names and the count sequence.
- Count to tell the number of objects.
- Compare numbers.

Operations and Algebraic Thinking

- Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

Number and Operations in Base Ten

- Work with numbers 11–19 to gain foundations for place value.

Measurement and Data

- Describe and compare measurable attributes.
- Classify objects and count the number of objects in categories.

Geometry

- Identify and describe shapes.
- Analyze, compare, create, and compare shapes

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CCSS Where to Focus Kindergarten Mathematics

Not all of the content in a given grade is emphasized equally in the Standards. Some clusters require greater emphasis than others based on the depth of the ideas, the time that they take to master, and/or their importance to future mathematics or the demands of college and career readiness. More time in these areas is also necessary for students to meet the Standards for Mathematical Practice.

To say that some things have a greater emphasis is not to say that anything in the standards can be safely neglected in instruction. Neglecting material will leave gaps in student skill and understanding and may leave students unprepared for the challenges of a later grade.

MAJOR, SUPPORTING, AND ADDITIONAL CLUSTERS FOR KINDERGARTEN

Emphases are given at the cluster level. Refer to the Common Core State Standards for Mathematics for the specific standards that fall within each cluster.

Key: ■ Major Clusters □ Supporting Clusters ○ Additional Clusters

- K.CCA ■ Know number names and the count sequence.
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- K.MDB □ Classify objects and count the number of objects in categories.
- K.GA ○ Identify and describe shapes.
- K.GB ○ Analyze, compare, create, and compose shapes.

REQUIRED FLUENCIES FOR KINDERGARTEN

K.OA.A.5 Add/subtract within 5

Student Achievement Partners, Achieve the Core <http://achievethecore.org/>, Focus by Grade Level, <http://achievethecore.org/dashboard/300/search/1/2/0/1/2/3/4/5/6/7/8/9/10/11/12/page/774/focus-by-grade-level>

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K.CC.A Know number names and the count sequence.**K.CC.1** Count to 100 by ones and by tens.**Essential Skills and Concepts:**

- Counting by ones
- Counting by tens
- Counting sequence/order

Question Stems and Prompts:

- ✓ Count forward beginning at 1.
- ✓ What number comes next? How do you know?
- ✓ Count by ones.
- ✓ Count by tens.

Vocabulary

Tier 2

- number
- net
- order
- counting

Tier 3

- ones
- tens

Spanish Cognates

- número
- ordenar, orden
- contar

Standards Connections

K.CC.1 → K.CC.2, K.CC.4a

Counting and Cardinality Progression Information:

Students usually know or can learn to say the counting words up to a given number before they can use these numbers to count objects or to tell the number of objects. Students become fluent in saying the count sequence so that they have enough attention to focus on the pairings involved in counting objects.

K, Counting and Cardinality; K – 5 Operations and Algebraic Thinking (2011, May 29),

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K.CC.A Know number names and the count sequence.

K.CC.2 Count forward beginning from a given number within the known sequence (instead of having to begin at 1).

Essential Skills and Concepts:

- Counting by one
- Counting on
- Counting sequence/order

Question Stems and Prompts:

- ✓ Count forward beginning at 7.
- ✓ Begin counting with 12 and stop at 31.
- ✓ Beginning with 24, count as high as you can.
- ✓ What number comes next? How do you know?

Vocabulary

Tier 2

- number
- net
- order
- counting

Spanish Cognates

- número
- ordenar, orden
- contar

Tier 3

- count on/count forward
- ones
- tens

Standards Connections

K.CC.2 → K.CC.4c

Counting and Cardinality Progression Information:

To count a group of objects, they pair each word said with one object.K.CC.4a This is usually facilitated by an indicating act (such as pointing to objects or moving them) that keeps each word said in time paired to one and only one object located in space. Counting objects arranged in a line is easiest; with more practice, students learn to count objects in more difficult arrangements, such as rectangular arrays (they need to ensure they reach every row or column and do not repeat rows or columns); circles (they need to stop just before the object they started with); and scattered configurations (they need to make a single path through all of the objects).K.CC.5 Later, students can count out a given number from 1–20, count out that many objects. of objects,K.CC.5 which is more difficult than just counting that many objects, because counting must be fluent enough for the student to have enough attention to remember the number of objects that is being counted out.

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K.CC.A Know number names and the count sequence.

K.CC.2 Count forward beginning from a given number within the known sequence (instead of having to begin at 1).

Standard Explanation

Students begin a rote forward counting sequence from a number other than 1. Thus, given the number 4, the student would count, “4, 5, 6, 7 ...” This objective does not require recognition of numerals. It is focused on the rote number sequence 0-100.

Teaching Strategies:

- Counting circles
- Number lines
- Count the number of chairs of the students who are absent.
- Count the number of stairs, shoes, etc.
- Counting groups of ten such as “fingers in the classroom” (ten fingers per student). (MP.6, MP. 7, MP. 8)
- Reinforce counting throughout the day

Examples of counting sequences:

- The ones (1-10)
- The teens (10, 11, 12, 13, 14, 15, 16, 17, 18, 19)
- Numbers that "cross the decade" (15, 16, 17, 18, 19, 20, 21, 22, 23, 24, or similarly 26-34, 35-44 etc.).
- **Note:** Students often have trouble with counting forward sequences that cross from one family into the next family, such as when crossing the decade. Focusing on short counting sequences can be helpful.

K.CC.2 Illustrative Tasks:

- Pick a Number,
<https://www.illustrativemathematics.org/content-standards/K/CC/A/2/tasks/927>
- Number After Bingo,
<https://www.illustrativemathematics.org/content-standards/K/CC/A/2/tasks/373>

Number AFTER Bingo 1-15

4	10	8	13	8
9	14	2	12	11
15	3	10	5	11
6	13	16	7	9
13	7	11	12	12

Begin whole group by discussing what “number after” means. Next have the students identify and point out on a large number line the number after various numbers selected by the teacher. Initially keep these numbers in the range of 1-15. After the group seems to have an understanding of what “number after” means and how to locate them on the number line, have students play Number After bingo on the 5x5 bingo board in pairs. Students will take turns drawing a number card, stating the number after and placing his/her counter on that number on the game board. The first student with 3 counters in a row on the grid is the winner. As students progress the practice range should be increased by changing the numbers on the grid and the corresponding numbers on the cards.

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K.CC.A Know number names and the count sequence.**K.CC.1** Count to 100 by ones and by tens.**Standard Explanation**

Students count by starting at one and counting to 100. When students count by tens they are only expected to master counting on the decade (0, 10, 20, 30, 40 ...). This objective does not require recognition of numerals. It is focused on the rote number sequence.

When counting orally, students should recognize the patterns that exist from 1 to 100. They should also recognize the patterns that exist when counting by 10s.

Counting should be reinforced throughout the day, not in isolation.

Examples:

- Count the number of chairs of the students who are absent.
- Count the number of stairs, shoes, etc.
- Counting groups of ten such as “fingers in the classroom” (ten fingers per student).

Teaching Strategies:

- Hundreds chart
- Number lines
- Counting/number literature

K.CC.1 Illustrative Task(s):

- Choral Counting, <https://www.illustrativemathematics.org/content-standards/K/CC/A/1/tasks/360>
- The teacher will need a 100 chart or large number line and a pointer.
 - As a whole group, have students chant the counting sequence starting with one to thirty, using the pointer to follow the number sequence. Over time, increase the range to one to fifty and then one to one hundred. Eventually have a student take over the job of pointing out the numbers in the sequence. Highlight the multiples of ten using a marker or a colored screen and have students chant the counting sequence by 10s. This should be done daily.
- Counting by Tens, <https://www.illustrativemathematics.org/content-standards/K/CC/A/1/tasks/754>
 - Have students count by ones to 100 clapping in front of their chest for each number.
 - When they count by tens, have them clap over their head.

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K.CC.A Know number names and the count sequence.

K.CC.3 Write numbers from 0 to 20. Represent a number of objects with a written numeral 0-20 (with 0 representing a count of no objects).

Essential Skills and Concepts:

- Writing numbers
- Number recognition
- One-to-one correspondence
- Counting by ones
- Counting sequence/order

Question Stems and Prompts:

- ✓ Write numbers in order beginning with 0.
- ✓ Count the objects (up to 20). How many?
- ✓ Count objects and write the number.
- ✓ Match the written numeral to the correct number of objects.

Vocabulary

Tier 2

- number
- net
- order
- counting

Tier 3

- numerals

Spanish Cognates

número

ordenar, orden

contar

Counting and Cardinality Progression Information:

Students come to quickly recognize the cardinalities of small groups without having to count the objects; this is called perceptual subitizing . Perceptual subitizing develops into conceptual subitizing —recognizing that a collection of objects is composed of two subcollections and quickly combining their cardinalities to find the cardinality of the collection (e.g., seeing a set as two subsets of cardinality 2 and saying “four”). Use of conceptual subitizing in adding and subtracting small numbers progresses to supporting steps of more advanced methods for adding, subtracting, multiplying, and dividing single-digit numbers (in several OA standards from Grade 1 to 3 that culminate in single-digit fluency).

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K.CC.A.3

Standard Explanation

Students write the numerals 0-20 and use the written numerals 0-20 to represent the amount within a set. For example, if the student has counted 9 objects, then the written numeral “9” is recorded. Students can record the quantity of a set by selecting a number card/tile (numeral recognition) or writing the numeral. Students can also create a set of objects based on the numeral presented. For example, if a student picks up the number card “13”, the student then creates a pile of 13 counters. While children may experiment with writing numbers beyond 20, this standard places emphasis on numbers 0-20.

Due to varied development of fine motor and visual development, reversal of numerals is anticipated. While reversals should be pointed out to students and correct formation modeled in instruction, the emphasis of this standard is on the use of numerals to represent quantities rather than the correct handwriting formation of the actual numeral itself.

Example: A Learning Sequence for Understanding Numbers

1. Count up to 20 objects in many settings and situations over several weeks.
2. Start to recognize, identify, and read the written numerals, and match the numerals to given sets of objects.
3. Write the numerals to represent counted objects.

K.CC.3 Illustrative Task:



- Race to the Top,

<https://www.illustrativemathematics.org/content-standards/K/CC/A/3/tasks/399>

The student rolls a number using the die or spinner and writes that number in the next box of the corresponding column. Students start at the bottom of the page and work to the top. Each time the student rolls/spins a number he/she will write the number on the paper in the next corresponding box. The winning number is the first to make it to the top of the paper. Students can also work in pairs.

				4					
				4					
0	1	2	3	4	5	6	7	8	9

K.CC.A.3

Standard Explanation

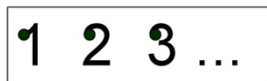
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				4					
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K.CC.B Count to tell the number of objects.

K.CC.4 Understand the relationship between numbers and quantities; connect counting to cardinality.

- When counting objects, say the number names in the standard order, pairing each object with one and only one number name and each number name with one and only one object.
- Understand that the last number name said tells the number of objects counted. The number of objects is the same regardless of their arrangement or the order in which they were counted.
- Understand that each successive number name refers to a quantity that is one larger.

Essential Skills and Concepts:

- Counting by ones
- One-to-one correspondence
- Counting sequence/order
- Greater discrimination

Question Stems and Prompts:

- ✓ Count objects in a random/scattered configuration, in a line, a rectangular or circular array, in ten frames, and in commonly recognized dot formations.
- ✓ Count the objects (up to 20). Say the number name for each object as it is counted.
- ✓ Count the objects (up to 20). Say the number name for each. How many are there?
- ✓ Count 7 objects. How many objects would you have if I gave you one more?

Vocabulary

Tier 2

- number
- groups
- pairing
- larger

Tier 3

- counting

Spanish Cognates

- número
- grupos
- emparejamient

contar

Standards Connections

K.CC.4a → K.CC.4b
 K.CC.4b → K.CC.5
 K.CC.4c → K.CC.2

Counting and Cardinality Progression Information:

Many and varied opportunities for students to manipulate concrete objects or visual representations (e.g., dot cards, tens frames) and connect number-names with their quantities can help students master the concept of counting. (Adapted from N. Carolina 2013).

K.CC.B Count to tell the number of objects.

K.CC.4 Understand the relationship between numbers and quantities; connect counting to cardinality.

- When counting objects, say the number names in the standard order, pairing each object with one and only one number name and each number name with one and only one object.
- Understand that the last number name said tells the number of objects counted. The number of objects is the same regardless of their arrangement or the order in which they were counted.
- Understand that each successive number name refers to a quantity that is one larger.

Essential Skills and Concepts:

- Counting by ones
- One-to-one correspondence
- Counting sequence/order
- Greater discrimination

Question Stems and Prompts:

- ✓ Count objects in a random/scattered configuration, in a line, a rectangular or circular array, in ten frames, and in commonly recognized dot formations.
- ✓ Count the objects (up to 20). Say the number name for each object as it is counted.
- ✓ Count the objects (up to 20). Say the number name for each. How many are there?
- ✓ Count 7 objects. How many objects would you have if I gave you one more?

Vocabulary

Tier 2

- number
- groups
- pairing
- larger

Tier 3

- counting

Spanish Cognates

- número
- grupos
- emparejamient

contar

Standards Connections

K.CC.4a → K.CC.4b
 K.CC.4b → K.CC.5
 K.CC.4c → K.CC.2

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K.CC.B.4

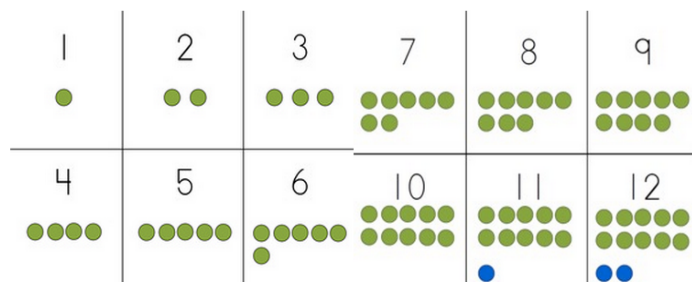
Standard Explanation

In kindergarten students develop an understanding of the relationship between numbers and quantities and connect counting to cardinality. Learning to count is a complex mental and physical activity that requires relating objects distributed in space (or in time) to words said over time. Kindergarten students use their understanding of the relationship between numbers and quantities to count a set of objects and see sets and numerals in relationship to one another, rather than as isolated concepts. Students count a set of objects and see sets and numerals in relationship to one another. These connections are higher-level skills that require students to analyze, reason about, and explain relationships between numbers and sets of objects.

Students implement correct counting procedures by pointing to one object at a time (one-to-one correspondence), using one counting word for every object (synchrony/one-to-one tagging), while keeping track of objects that have and have not been counted. This is the foundation of counting.

K.CC.4 Illustrative Task(s):

- Counting Mat, <https://www.illustrativemathematics.org/content-standards/K/CC/B/4/tasks/1209>
- The teacher gives students the counting mat and many small objects to count with. Some students will automatically read the numbers and assemble the correct number of object then match them to the dots on the counting mat to verify they counted correctly. Other students who need more scaffolding will match each object to a dot. Students who do it this way should be guided to count the objects once they have assembled them on the dots. Once a student is done with each number they can move on to the next number. The teacher should do a quick check of a student's work before the student begins working on the larger numbers.



K.CC.B.4

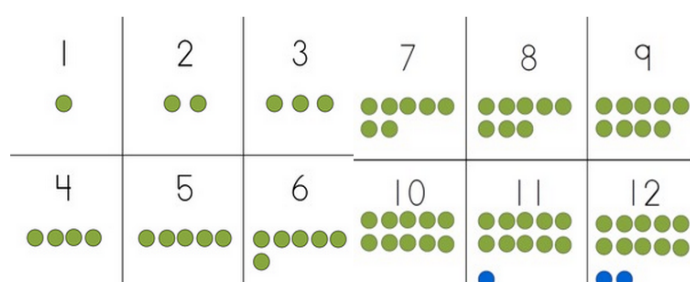
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K.CC.B Count to tell the number of objects.

K.CC.5 Count to answer “how many?” questions about as many as 20 things arranged in a line, a rectangular array, or a circle, or as many as 10 things in a scattered configuration; given a number 1-20, count out that many objects.

Essential Skills and Concepts:

- Counting by ones
- One-to-one correspondence
- Number recognition

Question Stems and Prompts:

- ✓ Count objects in a random/scattered configuration, in a line, a rectangular or circular array, in ten frames, and in commonly recognized dot formations.
- ✓ Count the objects (up to 20). How many are there?
- ✓ State a number 0-20. Have the student count that many objects.
- ✓ Show a number 0-20. Have the student count that many objects.

Vocabulary

Tier 2

- number

Tier 3

- counting

Spanish Cognates

número

contar

Standards Connections

K.CC.5 → K.CC.6

K.CC.5 Examples:**K.CC.B Count to tell the number of objects.**

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Essential Skills and Concepts:

- Counting by ones
- One-to-one correspondence
- Number recognition

Question Stems and Prompts:

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Vocabulary

Tier 2

- number

Tier 3

- counting

Spanish Cognates

número

contar

Standards Connections

K.CC.5 → K.CC.6

K.CC.5 Examples:

K.CC.B.5

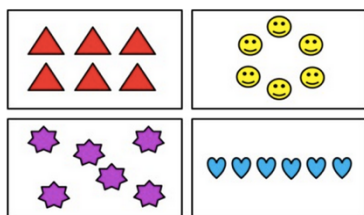
Standard Explanation

In order to answer “how many?” students need to keep track of objects when counting. Keeping track is a method of counting that is used to count each item once and only once when determining how many. After numerous experiences with counting objects, along with the developmental understanding that a group of objects counted multiple times will remain the same amount, students recognize the need for keeping track in order to accurately determine “how many”. Depending on the amount of objects to be counted, and the students’ confidence with counting a set of objects, students may move the objects as they count each, point to each object as counted, look without touching when counting, or use a combination of these strategies. It is important that children develop a strategy that makes sense to them based on the realization that keeping track is important in order to get an accurate count, as opposed to following a rule, such as “Line them all up before you count”, in order to get the right answer.

As children learn to count accurately, they may count a set correctly one time, but not another. Other times they may be able to keep track up to a certain amount, but then lose track from then on. Some arrangements, such as a line or rectangular array, are easier for them to get the correct answer but may limit their flexibility with developing meaningful tracking strategies, so providing multiple arrangements help children learn how to keep track. Since scattered arrangements are the most challenging for students, this standard specifies that students only count up to 10 objects in a scattered arrangement and count up to 20 objects in a line, rectangular array, or circle.

Teaching Strategies:

- Dot images
- Five/Ten Frames
- Number talks
- Subitizing



K.CC.5 Illustrative Task:

- Finding Equal Groups, <https://www.illustrativemathematics.org/content-standards/K/CC/B/5/tasks/1420>
- The teacher will give students a timer, and the students will race against the clock to sort the groups of objects into three separate groups (grouped by quantity) by the time the timer is finished. This can be played individually or in pairs.

K.CC.B.5

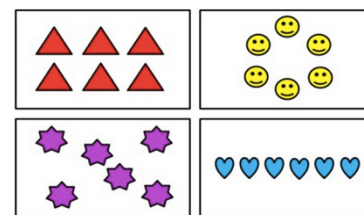
Standard Explanation

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K.CC.C Compare numbers.

K.CC.6 Identify whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group, e.g., by using matching and counting strategies.¹

¹ Include groups with up to ten objects.

Essential Skills and Concepts:

- Counting by ones
- Quantity discrimination
- Greater than/less than or equal groups

Question Stems and Prompts:

- ✓ Count the objects in each group (2 groups). How many are there? Compare the groups. Is it greater than, less than or equal to the other group?
- ✓ Make a group of 5 and a group of 7. Compare the groups. Is the first group greater than, less than or equal to the second group?
- ✓ Make a group of objects that is greater than the given group.
- ✓ Make a group of objects that is less than the given group.
- ✓ Make a group of objects that is equal to the given group.

Vocabulary

Tier 2

- number
- groups
- matching
- construct/make
- compare

Tier 3

- greater than
- less than
- equal to

Spanish Cognates

- número
- grupos
- construir
- comparar*

igual a

Standards Connections

K.CC.6 → K.CC.7, K.MD.3

K.CC.6 Examples:**K.CC.C Compare numbers.**

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Vocabulary

Tier 2

- number
- groups
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Tier 3

- greater than
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Spanish Cognates

- número
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igual a

Standards Connections

K.CC.6 → K.CC.7, K.MD.3

K.CC.6 Examples:

K.CC.C.6

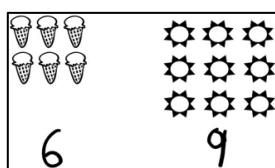
Standard Explanation

In kindergarten, students compare the number of objects in one group (with up to ten objects) to the number of objects in another group (K.CC.6▲). Students need a strong sense of the relationship between quantities and numerals to accurately compare groups and answer related questions. They can use matching strategies or counting strategies to determine whether one group is greater than, less than, or equal to the number of objects in another group. Students use their counting ability to compare sets of objects (0-10). They may use matching strategies (Student 1), counting strategies (Student 2) or equal shares (Student 3) to determine whether one group is greater than, less than, or equal to the number of objects in another group.

Example: (MP.1, MP.2)		
Student 1	Student 2	Student 3
I lined up one square to one triangle. Since there is one extra triangle, there are more triangles than squares.	I counted the squares and I got 8. Then I counted the triangles and got 9. Since 9 is bigger than 8, there are more triangles than squares.	I put them in a pile. I then took away objects. Every time I took a square. I also took a triangle. When I had taken almost all of the shapes away, there was still a triangle left. That means that there are more triangles than squares.

K.CC.6 Illustrative Task:

- Greater? Less? How do you know?, <https://www.illustrativemathematics.org/content-standards/K/CC/C/6/tasks/1210>
- The teacher will show the class two groups of objects or drawings of objects.
- The class will chorally count the two groups and record the number below the group.
- The teacher will then ask the class to chorally say which number is greater and which number is less.



K.CC.C.6

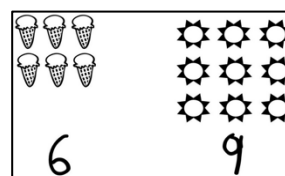
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K.CC.C Compare numbers.

K.CC.7 Compare two numbers between 1 and 10 presented as written numerals.

Essential Skills and Concepts:

- Number recognition
- Quantity discrimination
- Greater than/less than/ equal to

Question Stems and Prompts:

- ✓ Show two numbers between 1 and 10. Are the numbers equal? Which number is greater than the other? Which number is less than the other?

Vocabulary

Tier 2

- compare
- numbers
- groups

Tier 3

- greater than
- less than
- equal to
- numerals
- number line

Spanish Cognates

- comparar
- numeros
- grupos

igual a

linea de número

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Spanish Cognates

- comparar
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K.CC.C Compare numbers.

K.CC.7 Compare two numbers between 1 and 10 presented as written numerals.

Standard Explanation

An important level of understanding is reached when students can compare two numbers from 1 to 10 represented as written numerals, without counting. Students demonstrate their understanding of numbers when they can justify their answer (MP.3).

Students apply their understanding of numerals 1-10 to compare one numeral from another. Thus, looking at the numerals 8 and 10, a student is able to recognize that the numeral 10 represents a larger amount than the numeral 8. Students need ample experiences with actual sets of objects (K.CC.3 and K.CC.6) before completing this standard with only numerals.

Example:

- Students might justify an answer (e.g., 7 is greater than 5) by demonstrating a one to-one match, counting again, or other similar approaches that makes sense to explain or verify the answer. Teachers can ask probing questions, such as “How do you know?” to elicit student thinking and reasoning (MP.3, MP.8)

K.CC.7 Illustrative Task(s):

- Guess the Marbles in the Bag, <https://www.illustrativemathematics.org/content-standards/K/CC/C/7/tasks/697>

Materials: Paper bags and marbles (or some other counter, as long as it is relatively noisy).
(Whole-class version) The teacher secretly places between 1 and 10 marbles in a paper bag, then shows the bag to the class. After shaking it enough times for students to hear the marbles inside, and 4 or 5 students guess how many marbles are in the bag. The teacher writes the guesses on the board. Afterwards the contents of the bag are revealed and counted out. The teacher writes the number representing the total on the board, and the students then help sort their guesses into less than, greater than, or equal to the number of marbles in the bag. The game repeats until everyone has had a chance to guess at least once.

(Small group version) This works like the class version but one student in a group fill the bag with marbles themselves and the rest of the group tries to guess the number. With this variation it is practical to allow the students to both hear and feel the marbles inside the bag before they make their guess.

K.CC.C Compare numbers.

K.CC.7 Compare two numbers between 1 and 10 presented as written numerals.

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K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

K.OA.1 Represent addition and subtraction with objects, fingers, mental images, drawings², sounds (e.g., claps), acting out situations, verbal explanations, expressions, or equations.

Essential Skills and Concepts:

- Addition
- Subtraction
- Counting on
- Symbol recognition (i.e. + - =)

Question Stems and Prompts:

- ✓ Using objects. You have two apples. You have two oranges. How much fruit do you have altogether?
- ✓ Using images. There are 5 apples on a tree. Three apples fall off. How many apples are left on the tree?
- ✓ Acting out. There are 2 girls at the yellow table. One more girl sits at the yellow table. How many girls are at the yellow table altogether?
- ✓ Written expression. ●+● ●●=●
- ✓ Written equation. $2+3 = \underline{\quad}$; $5-1 = \underline{\quad}$

Vocabulary

- Tier 2
- altogether
 - left
 - more
 - take away

- Tier 3
- addition
 - subtraction
 - counting on
 - addition sign
 - subtraction sign
 - equal sign
 - equation

Spanish Cognates

adición

la ecuación

Standards Connections

K.OA.1 → K.OA.2

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Spanish Cognates

adición

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Standards Connections

K.OA.1 → K.OA.2

K.OA.A.1**Standard Explanation**

Students demonstrate the understanding of how objects can be joined (addition) and separated (subtraction) by representing addition and subtraction situations in various ways. This objective is focused on understanding the concept of addition and subtraction, rather than reading and solving addition and subtraction number sentences (equations). Common Core State Standards for Mathematics states, “Kindergarten students should see addition and subtraction equations, and student writing of equations in kindergarten is encouraged, but it is not required.” Please note that it is not until First Grade when “Understand the meaning of the equal sign” is an expectation. Therefore, before introducing symbols (+, -, =) and equations, kindergarteners require numerous experiences using joining (addition) and separating (subtraction) vocabulary in order to attach meaning to the various symbols. For example, when explaining a solution, kindergartens may state, “Three and two is the same amount as 5.” While the meaning of the equal sign is not introduced as a standard until First Grade, if equations are going to be modeled and used in Kindergarten, students must connect the symbol (=) with its meaning (is the same amount/quantity as).

Teaching Strategies:

- Number talks
- Rekenreks
- Make Five It Makes Sense p. 92
- Collect Ten It Makes Sense p.100

K.OA.1 Illustrative Task(s):

- Ten Frame Addition, <https://www.illustrativemathematics.org/content-standards/K/OA/A/1/tasks/1406>
- Dice Addition 2,

<https://www.illustrativemathematics.org/content-standards/K/OA/A/1/tasks/1405>

Dice Addition		
___	+	___ = ___
___	+	___ = ___
___	+	___ = ___

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- Rekenreks
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- Collect Ten It Makes Sense p.100

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- Ten Frame Addition, <https://www.illustrativemathematics.org/content-standards/K/OA/A/1/tasks/1406>
- Dice Addition 2,

<https://www.illustrativemathematics.org/content-standards/K/OA/A/1/tasks/1405>

Dice Addition		
___	+	___ = ___
___	+	___ = ___
___	+	___ = ___

K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

K.OA.2 Solve addition and subtraction word problems, and add and subtract within 10, e.g., by using objects or drawings to represent the problem.

Essential Skills and Concepts:

- Adding within 10
- Subtracting within 10

Question Stems and Prompts:

- ✓ Using objects. You have four pencils. Your number gives you four more pencils. How many pencils do you have altogether?
- ✓ Using drawings. You have 3 circles. You draw 4 more circles. How many circles have you drawn altogether?
- ✓ Using drawings. You have 7 lines. Then you erase 5 lines. How many lines are left?

Vocabulary

Tier 2

- numbers
- altogether
- left
- more
- take away

Tier 3

- addition
- subtraction
- counting on
- addition sign
- subtraction sign
- equal sign
- equation

Spanish Cognates

número

adición

la ecuación

Standards Connections

K.OA.2 → K.OA.3

K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

K.OA.2 Solve addition and subtraction word problems, and add and subtract within 10, e.g., by using objects or drawings to represent the problem.

Essential Skills and Concepts:

- Adding within 10
- Subtracting within 10

Question Stems and Prompts:

- ✓ Using objects. You have four pencils. Your number gives you four more pencils. How many pencils do you have altogether?
- ✓ Using drawings. You have 3 circles. You draw 4 more circles. How many circles have you drawn altogether?
- ✓ Using drawings. You have 7 lines. Then you erase 5 lines. How many lines are left?

Vocabulary

Tier 2

- numbers
- altogether
- left
- more
- take away

Tier 3

- addition
- subtraction
- counting on
- addition sign
- subtraction sign
- equal sign
- equation

Spanish Cognates

número

adición

la ecuación

Standards Connections

K.OA.2 → K.OA.3

K.OA.A.2

Standard Explanation

Word problems with real-life applications provide students with a context to develop their understanding of addition and subtraction. In kindergarten, students learn addition is putting together and adding to, and subtraction is taking apart and taking from. Kindergarteners use objects or math drawings (with simple shapes like circles) to model word problems.

Kindergarten students solve four types of problems within 10: Result Unknown/Add To; Result Unknown/Take From; Total Unknown/Put Together-Take Apart; and Addend Unknown/Put Together-Take Apart. Kindergarteners use counting to solve the four problem types by acting out the situation and/or with objects, fingers, and drawings. The main addition and subtraction situations in kindergarten are the dark shaded problem types in the following table. Students add and subtract within 10 to solve these problems types.

TABLE 1. Common addition and subtraction situations.			
	Result Unknown	Change Unknown	Start Unknown
Add to	Two bunnies sat on the grass. Three more bunnies hopped there. How many bunnies are on the grass now? $2 + 3 = ?$	Two bunnies were sitting on the grass. Some more bunnies hopped there. Then there were five bunnies. How many bunnies hopped over to the first two? $2 + ? = 5$	Some bunnies were sitting on the grass. Three more bunnies hopped there. Then there were five bunnies. How many bunnies were on the grass before? $? + 3 = 5$
Take from	Five apples were on the table. I ate two apples. How many apples are on the table now? $5 - 2 = ?$	Five apples were on the table. I ate some apples. Then there were three apples. How many apples did I eat? $5 - ? = 3$	Some apples were on the table. I ate two apples. Then there were three apples. How many apples were on the table before? $? - 2 = 3$
	Total Unknown	Addend Unknown	Both Addends Unknown¹²⁷
Put Together/ Take Apart	Three red apples and two green apples are on the table. How many apples are on the table? $3 + 2 = ?$	Five apples are on the table. Three are red and the rest are green. How many apples are green? $3 + ? = 5, 5 - 3 = ?$	Grandma has five flowers. How many can she put in her red vase and how many in her blue vase? $5 = 0 + 5, 5 = 5 + 0$ $5 = 1 + 4, 5 = 4 + 1$ $5 = 2 + 3, 5 = 3 + 2$

K.OA.2 Illustrative Task(s):

- What’s Missing?
<https://www.illustrativemathematics.org/content-standards/K/OA/A/2/tasks/70>
- Show the student 6 counters (small, flat objects). Ask the student to close his/her eyes. Hide some of the counters under a sheet of heavy paper. When the student opens his/her eyes, s/he determines how many were hidden based on the number of counters still showing.

K.OA.A.2

Standard Explanation

Word problems with real-life applications provide students with a context to develop their understanding of addition and subtraction. In kindergarten, students learn addition is putting together and adding to, and subtraction is taking apart and taking from. Kindergarteners use objects or math drawings (with simple shapes like circles) to model word problems.

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Take from	Five apples were on the table. I ate two apples. How many apples are on the table now? $5 - 2 = ?$	Five apples were on the table. I ate some apples. Then there were three apples. How many apples did I eat? $5 - ? = 3$	Some apples were on the table. I ate two apples. Then there were three apples. How many apples were on the table before? $? - 2 = 3$
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K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

K.OA.3 Decompose numbers less than or equal to 10 into pairs in more than one way, e.g., by using objects, or drawings, and record each decomposition by a drawing or equations (e.g., $5 = 2 + 3$ and $5 = 4 + 1$).

Essential Skills and Concepts:

- Decomposing numbers
- Recording compositions
- Variety of number pairs

Question Stems and Prompts:

- ✓ Using objects. There are seven blocks. Using these blocks make two groups. How many is in the first group? How many is in the second group? Record that. Now can you make two different groups?
- ✓ Using drawings. Using two different colored crayons (i.e. green and yellow), draw 9 circles. How many green circles did you make? How many yellow? Record that. Now can you make two different groups?

Vocabulary

Tier 2

- numbers
- pairs
- groups
- recording
- different

Spanish Cognates

número
pares
grupos

diferente

Tier 3

- decompose
- equation

descomponer
la ecuación

Standards Connections

K.OA.3 → K.OA.4, K.OA.5, K.NBT.1

K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

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Standards Connections

K.OA.3 → K.OA.4, K.OA.5, K.NBT.1

K.OA.A.3**Standard Explanation**

Students experience a variety of addition situations that involve putting together and adding to and a variety of subtraction situations that involve taking apart and taking from. Students use objects (such as two-color counters, clothespins on hangers, connecting cubes, five-frames and stickers), fingers, mental images, drawing, sounds, acting out situations, and verbal explanations to represent these operations (MP. 1, MP.2, MP.4, MP.5)

Students develop an understanding of part -whole relationships as they recognize that a set of objects (5) can be broken into smaller sub-sets(3 and 2) and still remain the total amount (5). In addition, this objective asks students to realize that a set of objects (5) can be broken in multiple ways (3 and 2; 4 and 1). Thus, when breaking apart a set (decompose), students use the understanding that a smaller set of objects exists within that larger set (inclusion).

In Kindergarten, students need ample experiences breaking apart numbers and using the vocabulary “and” & “same amount as” before symbols (+, =) and equations ($5 = 3 + 2$) are introduced. If equations are used, a mathematical representation (picture, objects) needs to be present as well.

Teaching Strategies:

- Number bonds/Tape diagrams with counters
- Rekenreks
- Shake and Spill
- Number families

K.OA.3 Illustrative Tasks:

- Shake and Spill,
<https://www.illustrativemathematics.org/content-standards/K/OA/A/3/tasks/165>
- For each student: you’ll need 5 two-color counters (e.g., red on one side and yellow on the other) & a cup (optional).
- The students put the counters in the cup, shake it, and spill them onto the table. Alternatively, they can use their hands. The students determine how many of each color is showing and record the sum using drawings or equations. The students should "shake and spill" several times to show different pairs of numbers that sum to 5.
- My Book of Five,

<https://www.illustrativemathematics.org/content-standards/K/OA/A/3/tasks/1408>

K.OA.A.3**Standard Explanation**

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K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

K.OA.4 For any number from 1 to 9, find the number that makes 10 when added to the given number, e.g., by using objects or drawings, and record the answer with a drawing or equation.

Essential Skills and Concepts:

- Addition to 10
- Number pairs
- Recording compositions

Question Stems and Prompts:

- ✓ Using objects. Count 4 objects. How many more objects are needed to make 10? Record the answer.
- ✓ Using objects. Place 6 objects onto an empty ten frame. How many more objects are needed to make 10? Record the answer.
- ✓ Using drawings. Draw 2 circles. How many more circles are needed to make 10? Record the answer.
- ✓ Using drawings. Color in 7 squares on an empty ten frame. How many more are needed to make 10? Record the answer.

Vocabulary

Tier 2

- numbers
- pairs
- groups
- recording
- different
- more

Tier 3

- compose
- decompose
- equation

Spanish Cognates

- número
- pares
- grupos
- diferente

- componer
- descomponer
- la ecuación

Standards Connections

K.OA.4 ← K.OA.3

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Standard Explanation


Students build upon the understanding that a number (less than or equal to 10) can be decomposed into parts (K.OA.3) to find a missing part of 10. Through numerous concrete experiences, kindergarteners model the various sub-parts of ten and find the missing part of 10.

Example:


When working with 2-color beans, a student determines that 4 more beans are needed to make a total of 10. In addition, Kindergarteners use various materials to solve tasks that involve decomposing and composing 10.

Example: “A full case of juice boxes has 10 boxes. There are only 6 boxes in this case. How many juice boxes are missing?”

Student A:
Using a Ten-Frame
“I used a ten frame for the case. Then, I put on 6 counters for juice still in the case. There’s no juice in these 4 spaces. So, 4 are missing.”



Student B:
Think Addition
“I counted out 10 counters because I knew there needed to be ten. I pushed these 6 over here because they were in the container. These are left over. So there’s 4 missing.”



Student C:
Fluently add/subtract
“I know that it’s 4 because 6 and 4 is the same amount as 10.”

Teaching Strategies:

- Tape diagram
- Shake and Spill
- Collect Ten *It Makes Sense!* p.100
- Ten frames

K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

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- Shake and Spill
- Collect Ten *It Makes Sense!* p.100
- Ten frames

K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

K.OA.5 Fluently add and subtract within 5.

Essential Skills and Concepts:

- Fluently add within 5
- Fluently subtract within 5
- Symbol recognition (i.e. + - =)

Question Stems and Prompts:

- ✓ Solve a set of given equations within a given amount of time.

Vocabulary

Tier 2

- numbers
- altogether
- left
- more
- take away

Tier 3

- addition
- subtraction
- counting on
- addition sign
- subtraction sign
- equal sign
- equation

Spanish Cognates

número

adición

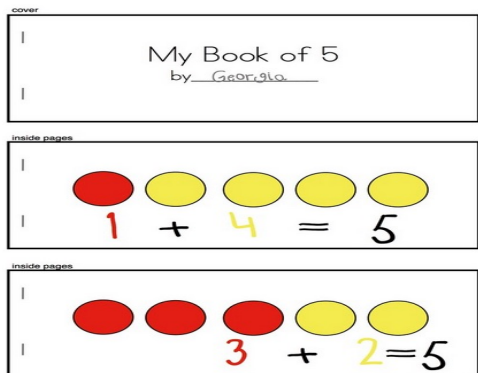
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Standards Connections

K.OA.5 ← K.OA.3

K.OA.5 Illustrative Tasks:

- My Book of Five,
<https://www.illustrativemathematics.org/content-standards/K/OA/A/5/tasks/1408>
- Many Ways to Do Addition1,
<https://www.illustrativemathematics.org/content-standards/K/OA/A/5/tasks/1409>



K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

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Essential Skills and Concepts:

- Fluently add within 5
- Fluently subtract within 5
- Symbol recognition (i.e. + - =)

Question Stems and Prompts:

- ✓ Solve a set of given equations within a given amount of time.

Vocabulary

Tier 2

- numbers
- altogether
- left
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Tier 3

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Spanish Cognates

número

adición

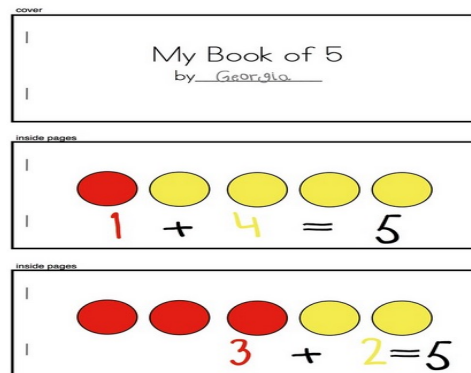
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Standards Connections

K.OA.5 ← K.OA.3

K.OA.5 Illustrative Tasks:

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K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

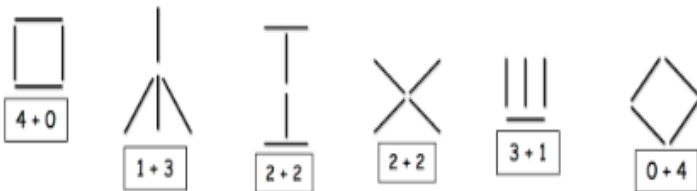
K.OA.5 Fluently add and subtract within 5.

Standard Explanation

Students are fluent when they display accuracy (correct answer), efficiency (a reasonable amount of steps without resorting to counting), and flexibility (using strategies such as the distributive property).

Students develop fluency by understanding and internalizing the relationships that exist between and among numbers. Oftentimes, when children think of each “fact” as an individual item that does not relate to any other “fact”, they are attempting to memorize separate bits of information that can be easily forgotten. Instead, in order to fluently add and subtract, children must first be able to see sub-parts within a number (inclusion, K.CC.4.c).

Once they have reached this milestone, children need repeated experiences with many different types of concrete materials (such as cubes, chips, and buttons) over an extended amount of time in order to recognize that there are only particular sub-parts for each number. Therefore, children will realize that if 3 and 2 is a combination of 5, then 3 and 2 cannot be a combination of 6. For example, after making various arrangements with toothpicks, students learn that only a certain number of sub-parts exist within the number 4:



Then, after numerous opportunities to explore, represent and discuss “4”, a student becomes able to fluently answer problems such as, “One bird was on the tree. Three more birds came. How many are on the tree now?”; and “There was one bird on the tree. Some more came. There are now 4 birds on the tree. How many birds came?”

Traditional flash cards or timed tests have not been proven as effective instructional strategies for developing fluency.** Rather, numerous experiences with breaking apart actual sets of objects and developing relationships between numbers help children internalize parts of number and develop efficient strategies for fact retrieval.

K.OA.A Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.

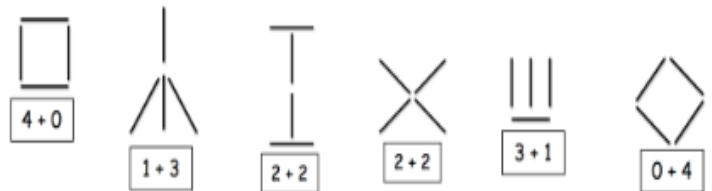
K.OA.5 Fluently add and subtract within 5.

Standard Explanation

Students are fluent when they display accuracy (correct answer), efficiency (a reasonable amount of steps without resorting to counting), and flexibility (using strategies such as the distributive property).

Students develop fluency by understanding and internalizing the relationships that exist between and among numbers. Oftentimes, when children think of each “fact” as an individual item that does not relate to any other “fact”, they are attempting to memorize separate bits of information that can be easily forgotten. Instead, in order to fluently add and subtract, children must first be able to see sub-parts within a number (inclusion, K.CC.4.c).

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K.NBT.A Work with numbers 11-19 to gain foundation for place value.

K.NBT.1 Compose and decompose numbers from 11 to 19 into ten ones and some further ones, e.g., by using objects or drawings, and record each composition or decomposition by a drawing or equation (e.g., $18 = 10 + 8$); understand that these numbers are composed of ten ones and one, two, three, four, five, six, seven, eight, or nine ones.

Essential Skills and Concepts:

- Composing larger numbers from smaller numbers
- Decomposing larger numbers into smaller numbers
- Ten ones and some more ones
- Recording compositions and decompositions

Question Stems and Prompts:

- ✓ Using objects. Compose numbers. If you have ten ones and then you add 4 more ones, how many will you have? Record. ($10 + 4 = 14$)
- ✓ Using drawings. Compose numbers. If you have ten circles and you want to have 15 circles, how many more circles will you need to draw? Record. ($10 + \underline{\quad} = 15$)
- ✓ Using objects. Decompose numbers. If you have 19 objects, and you place ten in the first group, how many objects will be in the second group? Record. ($19 = 10 + \underline{\quad}$)
- ✓ Using drawings. Decompose numbers. If you have 11 lines, and you place ten in the first group, how many objects will be in the second group? Record. ($11 = 10 + \underline{\quad}$).

Vocabulary

Tier 2

- numbers
- altogether
- left
- more
- take away
- recording

Tier 3

- compose
- ten ones
- addition
- subtraction

Spanish Cognates

número

componer

adición

Standards Connections

K.NBT.1 ← K.OA.3

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Vocabulary

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- numbers
- altogether
- left
- more
- take away
- recording

Tier 3

- compose
- ten ones
- addition
- subtraction

Spanish Cognates

número

componer

adición

Standards Connections

K.NBT.1 ← K.OA.3

K.NBT.A.1

Standard Explanation

Students explore numbers 11-19 using representations, such as manipulatives or drawings. Keeping each count as a single unit, kindergarteners use 10 objects to represent “10” rather than creating a unit called a ten (unitizing) as indicated in the First Grade CCSS standard 1.NBT.1a:10 can be thought of as a bundle of ten ones — called a “ten.” Example:

Teacher: “I have some chips here. Do you think they will fit on our ten frame? Why? Why Not?”

Students: Share thoughts with one another.

Teacher: “Use your ten frame to investigate.”

Students: “Look. There’s too many to fit on the ten frame. Only ten chips will fit on it.”

Teacher: “So you have some leftovers?”

Students: “Yes. I’ll put them over here next to the ten frame.”

Teacher: “So, how many do you have in all?”

Student A: “One, two, three, four, five... ten, eleven, twelve, thirteen, fourteen. I have fourteen. Ten fit on and four didn’t.”

Student B: Pointing to the ten frame, “See them—that’s 10... 11, 12, 13, 14. There’s fourteen.”

Teacher: Use your recording sheet (or number sentence cards) to show what you found out.

Student Recording Sheets Examples:

14 is 10 on and 4 off.

K.NBT.A.1

Standard Explanation

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Students: “Look. There’s too many to fit on the ten frame. Only ten chips will fit on it.”

Teacher: “So you have some leftovers?”

Students: “Yes. I’ll put them over here next to the ten frame.”

Teacher: “So, how many do you have in all?”

Student A: “One, two, three, four, five... ten, eleven, twelve, thirteen, fourteen. I have fourteen. Ten fit on and four didn’t.”

Student B: Pointing to the ten frame, “See them—that’s 10... 11, 12, 13, 14. There’s fourteen.”

Teacher: Use your recording sheet (or number sentence cards) to show what you found out.

Student Recording Sheets Examples:

14 is 10 on and 4 off.

Teaching Strategies:

- Tape diagram
- Ten frames

Teaching Strategies:

- Tape diagram
- Ten frames

K.NBT.1 Illustrative Task:

- What Makes a Teen Number?, <https://www.illustrativemathematics.org/content-standards/K/NBT/A/1/tasks/1404>

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- What Makes a Teen Number?, <https://www.illustrativemathematics.org/content-standards/K/NBT/A/1/tasks/1404>

13 = 10 + 3

13 = 10 + 3

K.MD.A Describe and compare measureable attributes.

K.MD.1 Describe measureable attributes of objects, such as length or weight. Describe several measureable attributes of a single object.

Essential Skills and Concepts:

- Describe objects in terms of length, height, or weight
- Describe several features of an object
- Understand measurable and non-measurable attributes

Question Stems and Prompts:

- ✓ Describe a pencil. Is it long or short? Is it heavy or light?
- ✓ Describe a student. Are they tall or short? Are they heavy or light?

Vocabulary

Tier 2

- describe
- long
- tall
- short
- heavy
- light
- attributes

Spanish Cognates

describir

atribuir

Standards Connections

K.MD.1 → K.MD.2

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Tier 2

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Spanish Cognates

describir

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Standards Connections

K.MD.1 → K.MD.2

K.MD.A.1

Standard Explanation

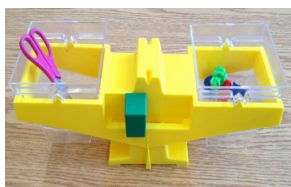
Students describe measurable attributes of objects, such as length, weight, size, and color. For example, a student may describe a shoe with one attribute, “Look! My shoe is blue, too!”, or more than one attribute, “This shoe is heavy! It’s also really long.”

Students often initially hold undifferentiated views of measurable attributes, saying that one object is “bigger” than another whether it is longer, or greater in area, or greater in volume, and so forth. For example, two students might both claim their block building is “the biggest.” Conversations about how they are comparing-one building may be taller (greater in length) and another may have a larger base (greater in area)-help students learn to discriminate and name these measureable attributes. As they discuss these situations and compare objects using different attributes, they learn to distinguish, label, and describe several measureable attributes of a single object. Thus, teachers listen for and extend conversations about things that are “big”, or “small,” as well as “long,” “tall,” or “high,” and name, discuss, and demonstrate with gestures the attribute being discussed.

K.MD.1 Illustrative Task:

- How Heavy?, <https://www.illustrativemathematics.org/content-standards/K/MD/A/1/tasks/798>

You will need various items to measure and weigh, a balance scale, a large set of cubes such as unifix or snap cubes, and a recording sheet with 4 sections. In each section would be the words: _____ cubes heavy, with enough space for a small drawing.

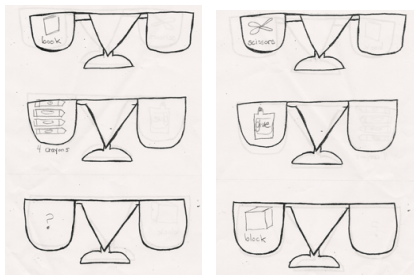


to
with

The students work in pairs. They choose an item to measure. Using the balance scale, they put the item on one side of the balance scale. They then put enough cubes on the other side of the scale to make it balance. They remove the cubes, count them, and record the number. They draw a picture of the item they measured. They continue same routine 3 more times with different items.

Name _____

_____ cubes heavy	_____ cubes heavy
_____ cubes heavy	_____ cubes heavy



K.MD.A.1

Standard Explanation

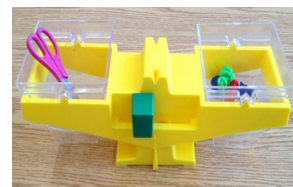
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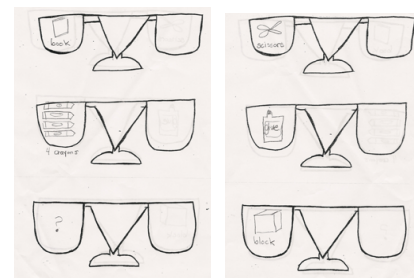
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Name _____

_____ cubes heavy	_____ cubes heavy
_____ cubes heavy	_____ cubes heavy



K.MD.A Describe and compare measurable attributes.

K.MD.2 Directly compare two objects with a measurable attribute in common, to see which object has “more of”/“less of” the attribute, and describe the difference. For example, directly compare the heights of two children and describe one child as taller/shorter.

Essential Skills and Concepts:

- Compare length, height, and weight
- Identify an attribute that an object has more of/less of
- Describe how to objects compare

Question Stems and Prompts:

- ✓ Compare the length of two like objects or two different objects. Which is longer? Which is shorter?
- ✓ Compare the height of two like objects or two different objects.. Which is taller? Which is shorter?
- ✓ Compare the weight of two like objects or two different objects. Which is heavier? Which is lighter?

Vocabulary

Tier 2

- describe
- long
- tall
- short
- heavy
- light
- attributes

Spanish Cognates

describir

atribuir

Standards Connections

K.MD.2 → K.MD.3

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Vocabulary

Tier 2

- describe
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Spanish Cognates

describir

atribuir

Standards Connections

K.MD.2 → K.MD.3

K.MD.A.2**Standard Explanation**

Direct comparisons are made when objects are put next to each other, such as two children, two books, two pencils. For example, a student may line up two blocks and say, “The blue block is a lot longer than the white one.” Students are not comparing objects that cannot be moved and lined up next to each other.

K.MD.2 Illustrative Tasks:

- Size Shuffle,
<https://www.illustrativemathematics.org/content-standards/K/MD/A/2/tasks/455>
- Material: one pair of “taller”/ “shorter” cards for each student.
- The students stand in a circle with the cards in their hands.
- The teacher says "GO." The students find a partner and stand face-to-face. The taller student holds up the "taller" card and the shorter student holds up the "shorter" card.
- When the teacher calls out a student’s name, they respond in a complete sentence:

I am shorter (taller) than

_____.



- The teacher calls on three or four students each round. The teacher says "GO" and calls on three or four different students each time until all the students have had a turn to respond.
- Which Weighs More? Which Weighs Less?,
<https://www.illustrativemathematics.org/content-standards/K/MD/A/2/tasks/456>
- Materials:
- Sheets of paper for each student that are folded in half with the words "Heavier" and "Lighter" written at the top of each side.
- A box of large blocks.
- A box of different objects with different weights to compare with a block from the first box. Some should be lighter than a single block and some should be heavier. The weight differences should be fairly pronounced.

The students begin by choosing a block that they will use to compare with other objects.

Students will then choose an item from the second box and compare its weight to their block. They then draw a picture of it under "Heavier" or "Lighter" depending on which applies. They continue to choose objects from the box to measure against their block until they have two or three drawings on each side of their sheet.

K.MD.A.2**Standard Explanation**

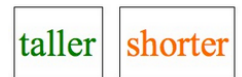
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K.MD.B Classify objects and count the number of objects in each category.

K.MD.3 Classify objects into given categories; count the numbers of objects in each category and sort the categories by count³.

Essential Skills and Concepts:

- Classify objects based upon a variety of measureable attributes
- Counting by ones
- Sort groups by number of objects

Question Stems and Prompts:

- ✓ Sort a given set of objects. How did you sort these? Why did you put this object into this group? Why didn't you put it into this group?

Vocabulary

Tier 2

- classify
- sort
- group

Tier 3

- counting

Spanish Cognates

clasificar

grupo

contar

Standards Connections

K.MD.3 ← K.MD.2, K.CC.6

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- Classify objects based upon a variety of measureable attributes
- Counting by ones
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- ✓ Sort a given set of objects. How did you sort these? Why did you put this object into this group? Why didn't you put it into this group?

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Tier 2

- classify
- sort
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Standards Connections

K.MD.3 ← K.MD.2, K.CC.6

K.MD.B.3**Standard Explanation**

Kindergarten students connect counting and ordering skills and understandings to help them classify objects or people into given categories, count the number of objects in each category, and sort the categories by count (K.MD.3).

Students identify similarities and differences between objects (e.g., size, color, shape) and use these attributes to sort a collection of objects (MP.2, MP.6, MP.7).

When the objects are sorted, students count the objects in each set and then order each of the sets by the amount in each set.

K.MD.3 Illustrative Task(s):

- Sort and Count I, <https://www.illustrativemathematics.org/content-standards/K/MD/B/3/tasks/799>
- You will need sorting cards or items, for example: colors, shapes, animals, foods, etc. Cards should be able to be sorted multiple ways (example, foods could be sorted by color, then sorted by fruit vs. veggie vs. grain). Another example is animals could first be sorted by pet vs. wild animal vs. farm animal and next be sorted by number of legs and finally be sorted by furry animals/skin animals/scale animals. First have students look at the cards and decide two or three different ways to sort. Next each student can randomly choose a card or item. Then when all class has one, they sort themselves into categories according to color, shape, and type of animal or food they have. Then the teacher can ask the questions:
 - “Which group has the most?”
 - “Which group has the least?”
 - “Do any groups have the same number?”

The students count the groups and answer the teacher’s questions.

- Sort and Count II, <https://www.illustrativemathematics.org/content-standards/K/MD/B/3/tasks/990>
- Students get a bag of small objects. Each bag should contain objects that can be sorted in multiple ways. For example, if the bag contains round buttons, students can sort by color, size, or the number of holes in each button. If the bag contains different shapes in different colors, they can sort by color or shape.
 - Students take their bag and spill it onto a large sheet of paper or a tray. Students then sort them according to one attribute such as color, shape, size, or some other attribute.
 - When they have sorted all of the objects, students then count the number of objects in each group.

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K.G.A Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cones, cylinders, and spheres).

K.G.1 Describe objects in the environment using names of shapes and describe the relative positions of these objects using terms such as *above*, *below*, *beside*, *in front of*, *behind*, and *next to*.

Essential Skills and Concepts:

- Describe the position of an object
- Names shapes
- Find shapes in the environment and describe their positions

Question Stems and Prompts:

Students need opportunities to identify and name two- and three-dimensional shapes in and outside of the classroom and describe relative positions.

- ✓ Ask students to find rectangles in the classroom and describe the relative positions of the rectangles they see [(Possible answer: The rectangle (a poster) is over the sphere (globe)].
- ✓ The teacher holds up objects such as an ice cream cone, a number cube or ball, and asks students to identify each shape.
- ✓ The teacher places an object next to, behind, above, below, beside, or in front of another object and asks positional questions--Where is the object?
 - Which way?
 - How far?
 - Where?
 - What type of objects?

Vocabulary

Tier 2

- position
- shape

Tier 3

- square
- circle
- triangle
- rectangle
- hexagon
- cube
- cone
- cylinder
- sphere

Spanish Cognates

posicion

círculo
triángulo
rectángulo
hexagono
cubo
cono
cilindro
esfera

Standards Connections

K.G.1 and K.G.2 → K.G.3 and K.G.4

K.G.A Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cones, cylinders, and spheres).

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Tier 2

- position
- shape

Tier 3

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- circle
- triangle
- rectangle
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- cube
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- sphere

Spanish Cognates

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Standards Connections

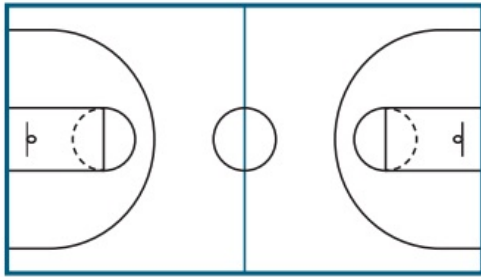
K.G.1 and K.G.2 → K.G.3 and K.G.4

K.G.A.1**Standard Explanation**

Students use positional words to describe objects in the environment (K.G.1). Examples of positional words include in and out, inside and outside, down and up, above and below, over and under, before and after, top and bottom, front and back, right and left, on and off, begin and end, and near and far.

Students develop spatial sense by connecting geometric shapes to their everyday lives. Students need opportunities to identify and name two- and three-dimensional shapes in and outside of the classroom and describe relative positions by answering questions such as these:

- Which way is the cafeteria? (The cafeteria is to the right.) Which shape is near the rectangle? (The circle is near the rectangle.)
- Where is the green ball? (The green ball is on top of the cupboard.)
- What types of shapes do you see on the floor of the basketball court? (I see a rectangle and a circle on the basketball court.)



Students begin to name and describe three-dimensional shapes with mathematical vocabulary, using words such as sphere, cube, cylinder, and cone, and answer related questions (MP.6, MP.7). Examples for standard K.G.1 include the following:

- Ask students to find rectangles in the classroom and describe the relative positions of the rectangles they see. (Possible answer: The rectangle [a poster] is over the sphere [globe]).
- The teacher holds up objects—such as an ice-cream cone, a number cube, or a ball—and asks students to identify each shape.
- The teacher places an object next to, behind, above, below, beside, or in front of another object and asks positional questions such as “Where is the object?” (adapted from ADE 2010; KATM 2012, Kindergarten Flipbook; and UA Progressions Documents 2012c).

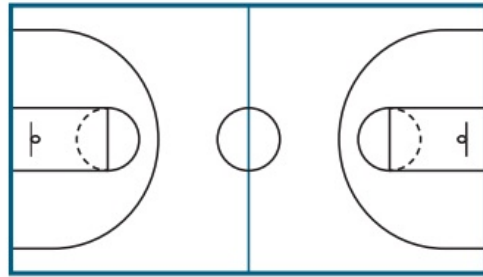
California *Mathematics Framework*, November 6, 2013,
<http://www.cde.ca.gov/ci/ma/cf/draft2mathfwchapters.asp>

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K.G.A Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cones, cylinders, and spheres).

K.G.2 Correctly name shapes regardless of their orientations or overall size.

Essential Skills and Concepts:

- Recognize shapes in different orientations or of different sizes
- Name two-dimensional and three-dimensional shapes

Question Stems and Prompts:

- ✓ What shape is this? How do you know? What if I turn it upside down? What shape is it now? How do you know?
- ✓ What is this little shape? What is that larger shape? Are they the same shape? How do you know?
- ✓ Present a series of shapes of varied sizes and orientations. Is there a circle? How many triangles do you see?

Vocabulary

Tier 2

- shape
- size

Tier 3

- square
- circle
- triangle
- rectangle
- hexagon
- cube
- cone
- cylinder
- sphere

Spanish Cognates

- círculo
- triángulo
- rectángulo
- hexagono
- cubo
- cono
- cilindro
- esfera

Standards Connections

K.G.1 and K.G.2 → K.G.3 and K.G.4
 K.G.2 → K.G.6, 1.G.1

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Vocabulary

Tier 2

- shape
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Tier 3

- square
- circle
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- círculo
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Standards Connections

K.G.1 and K.G.2 → K.G.3 and K.G.4
 K.G.2 → K.G.6, 1.G.1

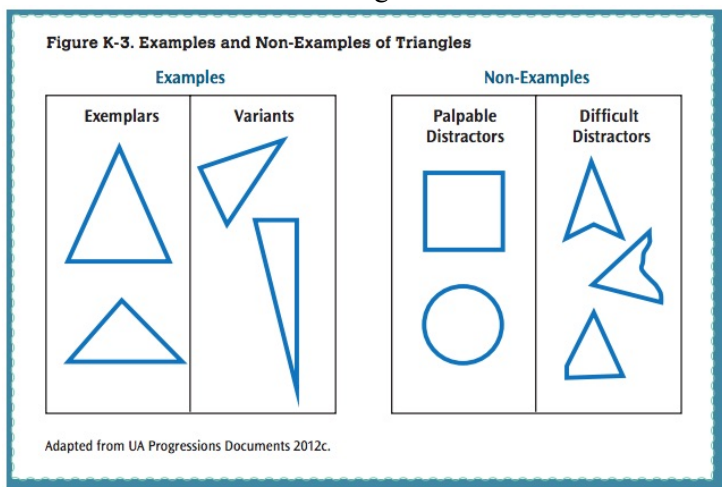
K.G.A.2

Standard Explanation

Kindergarten students work with a variety of shapes that have different sizes. They learn to match two-dimensional shapes even when the shapes have different orientations (K.G.2). Students name shapes that occur in everyday situations, such as circles, triangles, and squares, and distinguish them from non-examples of these categories.

Students develop an intuitive image of each shape category. Figure K-3 includes examples and non-examples of triangles, as described below:

- Examples
 - Exemplars—typical visual prototypes of the shape category
 - Variants—other examples of the shape category
- Non-Examples
 - Palpable distractors—non-examples with little or no overall resemblance to the exemplars
 - Difficult distractors—visually similar to examples, but lack at least one defining attribute



K.G.2 Examples:

1. Teacher makes pairs of paper shapes that are different sizes. Each student is given one shape and the objective is to find the partner who has the same shape.
2. Teacher brings in a variety of spheres (tennis ball, basketball, globe, ping pong ball, etc.) to demonstrate that size doesn't change the name of a shape.

Arizona's College and Career Ready Standards – Mathematics – Kindergarten, Arizona Department of Education, <http://www.azed.gov/azccrs/mathstandards/>

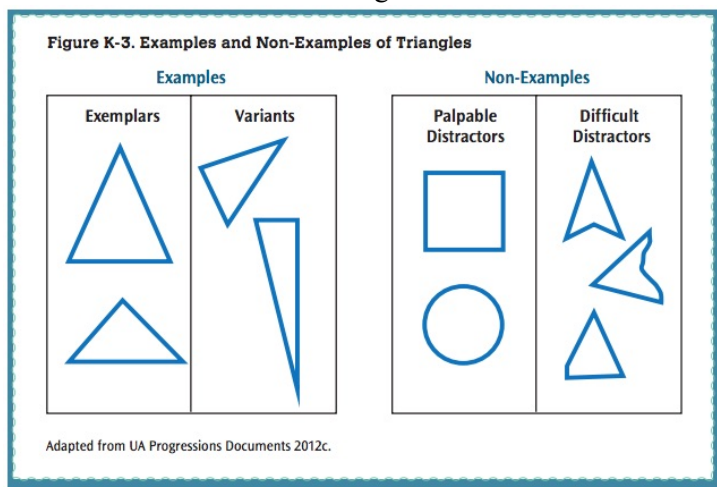
K.G.A.2

Standard Explanation

Kindergarten students work with a variety of shapes that have different sizes. They learn to match two-dimensional shapes even when the shapes have different orientations (K.G.2). Students name shapes that occur in everyday situations, such as circles, triangles, and squares, and distinguish them from non-examples of these categories.

Students develop an intuitive image of each shape category. Figure K-3 includes examples and non-examples of triangles, as described below:

- Examples
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K.G.A Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cones, cylinders, and spheres).

K.G.3 Identify shapes as two-dimensional (lying in a plane, “flat”) or three-dimensional (“solid”).

Essential Skills and Concepts:

- Identify two-dimensional shapes
- Identify three-dimensional shapes

Question Stems and Prompts:

- ✓ Present a number of shapes in various sizes and orientations. Determine which of the objects are two-dimensional and which are three-dimensional.
- ✓ Present images of shapes in various sizes and orientations. Determine which of the objects are two-dimensional and which are three-dimensional.
- ✓ This is a square. Is it two or three dimensional? How do you know?
- ✓ This is a sphere. It is three-dimensional. Yes or no? How do you know?
- ✓ This is a circle. It is three-dimensional. Yes or no? How do you know?

Vocabulary

Tier 2

- identify

Tier 3

- two-dimensional
- three-dimensional
- square
- circle
- triangle
- rectangle
- hexagon
- cube
- cone
- cylinder
- sphere

Spanish Cognates

- circular
- triángulo
- rectángulo
- hexagono
- cubo
- cono
- cilindro
- esfera

Standards Connections

K.G.3 and K.G.4 → K.G.2

K.G.3 and K.G.4 → 1.G.1

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Vocabulary

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Standard Explanation

Students identify shapes as two-dimensional (lying in a plane, “flat”) or three-dimensional (“solid”) [K.G.3] and differentiate between two-dimensional and three-dimensional shapes (MP.6, MP.7). For example:

- Students name a picture of a shape as two-dimensional because it is flat and can be measured in only two ways (by its length and width).
- Students name an object as three-dimensional because it is not flat (it is a solid object or shape) and can be measured by length, width, and height (or depth) [adapted from ADE 2010].

Kindergarten students connect their work with identifying and classifying simple shapes (refer to standards K.G.1–3) to help them compare shapes and manipulate two or more shapes to create a new shape. This understanding also builds foundations for students to “reason with shapes and their attributes” in grade one (refer to standards 1.G.1–3).

California *Mathematics Framework*, November 6, 2013,
<http://www.cde.ca.gov/ci/ma/cf/draft2mathfwchapters.asp>

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K.G.B Analyze, compare, create, and compose shapes.

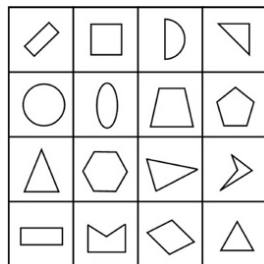
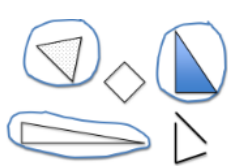
K.G.4 Analyze and compare two- and three-dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g., number of sides and vertices/“corners”) and other attributes (e.g., having sides of equal length).

Standard Explanation

Students describe similarities and differences between and among shapes using informal language (K.G.4). These experiences help young students begin to understand how three-dimensional shapes are composed of two-dimensional shapes—for example, the base and the top of a cylinder is a circle, the face of a cube is a square, a circle is formed in the shadow of a sphere. In early explorations of geometric properties, students discover how categories of shapes are subsumed within other categories.

Students work with various triangles, rectangles, and hexagons with sides that are not all congruent. Initially, students describe shapes using everyday language and then expand their vocabulary to include geometric terms such as sides and vertices (or corners). Opportunities to work with pictorial representations and concrete objects, as well as technology, will help students develop their understanding and descriptive vocabulary for both two- and three-dimensional shapes (MP.4, MP.6, MP.7). *California Mathematics Framework*, November 6, 2013,

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K.G.4 Illustrative Task:

- Alike and Different Game, <https://www.illustrativemathematics.org/content-standards/K/G/B/4/tasks/515>
- Students in pairs take turns drawing two cards. They should name something that is the ALIKE or DIFFERENT between the two cards. Then the next two cards are drawn and the process repeats until no cards remain.
- In a cooperative game, the students work together to name a property for each pair.
- In a competitive game, the student who can name a property first gets to keep the cards and the student with the most cards at the end of the game wins.

K.G.B Analyze, compare, create, and compose shapes.

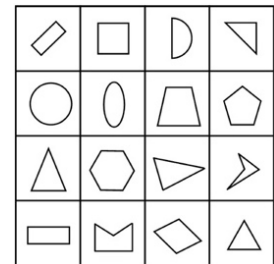
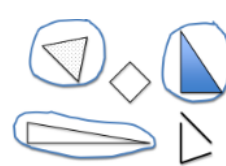
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K.G.B Analyze, compare, create, and compose shapes.

K.G.5 Model shapes in the world by building shapes from components (e.g., sticks and clay balls) and drawing shapes.

Essential Skills and Concepts:

- Build shapes in the environment
- Draw shapes in the environment

Question Stems and Prompts:

- ✓ Draw a circle.
- ✓ Draw a cube.
- ✓ Using clay, make a sphere.
- ✓ Using toothpicks make a square.

Vocabulary

Spanish Cognates

Tier 2

- build
- same
- different
- corner
- sides

diferente

Tier 3

- two-dimensional
- three-dimensional
- vertices
- edges
- faces

vértices

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K.G.B Analyze, compare, create, and compose shapes.

K.G.5 Model shapes in the world by building shapes from components (e.g., sticks and clay balls) and drawing shapes.

Standard Explanation

In kindergarten, students model shapes they observe in everyday life by building shapes from various components (e.g., clay, glue, tape, sticks, paper, straws) and by drawing shapes (K.G.5). Two-dimensional shapes are flat, and three-dimensional shapes are not flat (and can be “solid”), so students should draw or create two-dimensional shapes and build three-dimensional shapes (MP.1, MP.4, MP.7).

California *Mathematics Framework*, November 6, 2013,
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K.G.B Analyze, compare, create, and compose shapes.

K.G.6 Compose simple shapes to form larger shapes. *For example, “Can you join these two triangles with full sides touching to make a rectangle?”*

Standard Explanation

Students compose simple shapes to form larger shapes and answer questions such as, “Can you join these two triangles with full sides touching to make a rectangle?” (K.G.6). Composing shapes is an important concept in kindergarten. Students move from identifying and classifying simple shapes to manipulating two or more shapes to create a new shape. Students rotate, flip, and arrange puzzle pieces, and they move shapes to make a design or picture. Finally, students manipulate simple shapes to make a new shape (MP.1, MP.3, MP.4, MP.7) [adapted from KATM 2012, Kindergarten Flipbook].

Puzzles provide opportunities for students to apply spatial relationships and develop problem-solving skills in an entertaining and meaningful way. Pattern blocks and tangrams are often utilized when students work with two-dimensional shapes.

Composing and decomposing shapes with right angles (squares, rectangles, and right triangles that also make isosceles triangles) provides important foundations for central geometric concepts (such as transformations) in later grades.

Examples of interactive tangram puzzles are available at the National Council of Teachers of Mathematics Web site (<http://www.nctm.org/standards/content.aspx?id=25012> [accessed July 31, 2014]).

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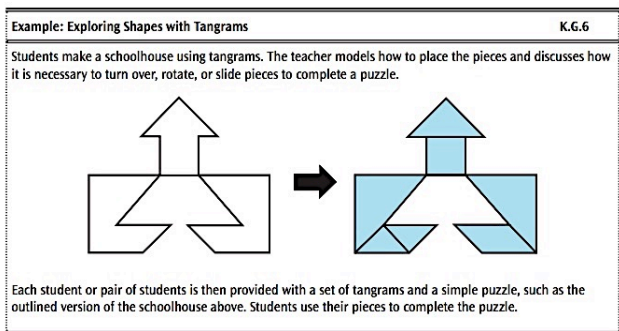
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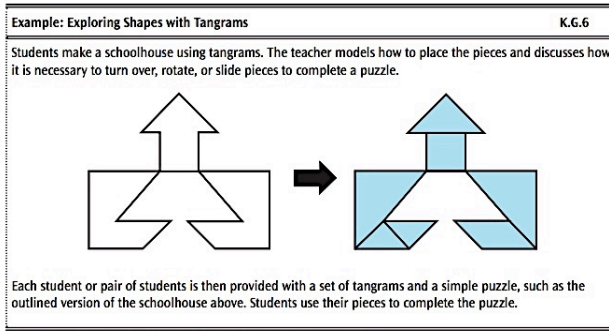
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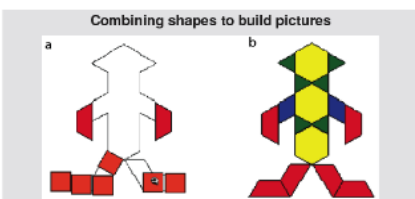
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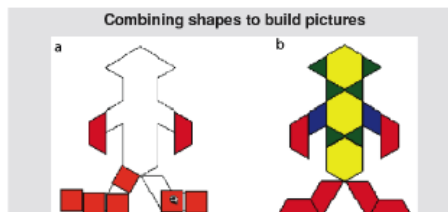
Adapted from National Council of Teachers of Mathematics Illuminations 2013d.



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K – 6, Geometry (2012, June 23),



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<http://ime.math.arizona.edu/progressions/>

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Resources for the CCSS Kindergarten Bookmarks

California *Mathematics Framework*, adopted by the California State Board of Education November 6, 2013, <http://www.cde.ca.gov/ci/ma/cf/draft2mathfwchapters.asp>

Student Achievement Partners, Achieve the Core <http://achievethecore.org/>, Focus by Grade Level, <http://achievethecore.org/dashboard/300/search/1/2/0/1/2/3/4/5/6/7/8/9/10/11/12/page/774/focus-by-grade-level>

Common Core Standards Writing Team. Progressions for the Common Core State Standards in Mathematics Tucson, AZ: Institute for Mathematics and Education, University of Arizona (Drafts), <http://ime.math.arizona.edu/progressions/>

- K, Counting and Cardinality; K – 5 Operations and Algebraic Thinking (2011, May 29)
- K – 5, Number and Operations in Base Ten (2012, April 21)
- K – 3, Categorical Data; Grades 2 – 5, Measurement Data* (2011, June 20)
- K – 5, Geometric Measurement (2012, June 23)
- K – 6, Geometry (2012, June 23)
- Number and Operations – Fractions, 3 – 5 (2013, September 19)

Illustrative Mathematics™ was originally developed at the University of Arizona (2011), nonprofit corporation (2013), Illustrative Tasks, <http://www.illustrativemathematics.org/>

Student Achievement Partners, Achieve the Core <http://achievethecore.org/>, Focus by Grade Level, <http://achievethecore.org/dashboard/300/search/1/2/0/1/2/3/4/5/6/7/8/9/10/11/12/page/774/focus-by-grade-level>

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