? = 11, 5 = -3, 6 + 6 =



Mathematics Continuum: Grades 1-3	Tim A. Hire, County Superintendent of Schools				
Operations and Algebraic Thinking					
Grade 1	Grade 2	Grade 3			
Represent and solve problems involving addition and subtraction. 1.OA.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem. ² { ² See Glossary, Table 1.} 1.OA.2. Solve word problems that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and	Represent and solve problems involving addition and subtraction. 2.OA.1. Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown	Represent and solve problems involving multiplication and division. 3.OA.1. Interpret products of whole numbers, e.g., interpret 5 × 7 as the total number of objects in 5 groups of 7 objects each. For example, describe a context in which a total number of objects can be expressed as 5 × 7. 3.OA.2. Interpret whole-number quotients of whole numbers, e.g., interpret 56 ÷ 8 as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each. For example, describe a context in which a number of shares or a number of groups can be expressed as			
equations with a symbol for the unknown number to represent the problem. Understand and apply properties of operations and the relationship between addition and subtraction. 1.OA.3. Apply properties of operations as strategies to add and subtract. ³	number to represent the problem. ¹ {¹ See Glossary, Table 1.} Add and subtract within 20. 2.OA.2. Fluently add and subtract within 20 using mental strategies.² By end of Grade 2, know from	56÷8. 3.OA.3. Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.¹ [¹ See Glossary, Table 2.] 3.OA.4. Determine the unknown whole number in a multiplication or division equation relating three			
Examples: If 8 + 3 = 11 is known, then 3 + 8 = 11 is also known. (Commutative property of addition.) To add 2 + 6 + 4, the second two numbers can be added to make a ten, so 2 + 6 + 4 = 2 + 10 = 12. (Associative property of addition.) {3 Students need not use formal terms for these properties.}	memory all sums of two one-digit numbers. {2 See standard 1.OA.6 for a list of mental strategies.} Work with equal groups of objects to gain foundations for multiplication.	whole numbers. For example, determine the unknown number that makes the equation true in each of the equations $8 \times ? = 48$, $5 = \div 3$, $6 \times 6 = ?$. Understand properties of multiplication and the relationship between multiplication and division. 3.OA.5. Apply properties of operations as strategies to multiply and divide. *2 Examples: If $6 \times 4 = 24$ is			
1.OA.4. Understand subtraction as an unknown-addend problem. For example, subtract 10 – 8 by finding the number that makes 10 when added to 8.	2.OA.3. Determine whether a group of objects (up to 20) has an odd or even number of members, e.g., by	known, then $4 \times 6 = 24$ is also known. (Commutative property of multiplication.) $3 \times 5 \times 2$ can be found by $3 \times 5 = 15$, then $15 \times 2 = 30$, or by $5 \times 2 = 10$, then $3 \times 10 = 30$. (Associative			
Add and subtract within 20. 1.OA.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).	pairing objects or counting them by 2s; write an equation to express an even number as a sum of two equal addends.	property of multiplication.) Knowing that $8 \times 5 = 40$ and $8 \times 2 = 16$, one can find 8×7 as $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$. (Distributive property.) [2Students need not use formal terms for these properties.]			
1.OA.6. Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., $8+6=8+2+4=10+4=14$); decomposing a number leading to a ten (e.g., $13-4=13-3-1=10-1=9$); using the relationship between addition and subtraction (e.g., knowing that $8+4=12$, one knows $12-8=4$); and creating equivalent but easier or known sums (e.g., adding $6+7$ by creating the known equivalent $6+6+1=12+1=12$	2.OA.4. Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an equation to express the total as a sum of equal addends.	 3.OA.6. Understand division as an unknown-factor problem. For example, find 32 ÷ 8 by finding the number that makes 32 when multiplied by 8. Multiply and divide within 100. 3.OA.7. Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that 8 × 5 = 40, one knows 40 ÷ 5 = 8) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers. Solve problems involving the four operations, and identify and explain patterns in arithmetic. 			
 13). Work with addition and subtraction equations. 1.OA.7. Understand the meaning of the equal sign, and determine if equations involving addition and subtraction are true or false. For example, which of the following equations are true and which are false? 6 = 6, 7 = 8 - 1, 5 + 2 = 2 + 5, 4 + 1 = 5 + 2. 1.OA.8. Determine the unknown whole number in an addition or subtraction 		3.OA.8. Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. ³ [³ This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).] 3.OA.9. Identify arithmetic patterns (including patterns in the addition table or multiplication table), and			
equation relating three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations 8 +		explain them using properties of operations. For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.			



Number and Operations in Base Ten			
Grade 1	Grade 2	Grade 3	
Extend the counting sequence. 1.NBT.1. Count to 120, starting at any number less than 120. In this range, read and write numerals and represent a number of objects with a written numeral. Understand place value. 1.NBT.2. Understand that the two digits of a two-digit number represent amounts of tens and ones. Understand the following as special cases: a. 10 can be thought of as a bundle of ten ones — called a "ten." b. The numbers from 11 to 19 are composed of a ten and one, two, three, four, five, six, seven, eight, or nine ones. c. The numbers 10, 20, 30, 40, 50, 60, 70, 80, 90 refer to one, two, three, four, five, six, seven, eight, or nine tens (and 0 ones). 1.NBT.3. Compare two two-digit numbers based on meanings of the tens and ones digits, recording the results of comparisons with the symbols >, =, and <. Use place value understanding and properties of operations to add and subtract. 1.NBT.4. Add within 100, including adding a two-digit number and a one-digit number, and adding a two-digit number and a multiple of 10, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used. Understand that in adding two-digit numbers, one adds tens and tens, ones and ones; and sometimes it is necessary to compose a ten. 1.NBT.5. Given a two-digit number, mentally find 10 more or 10 less than the number, without having to count; explain the reasoning used. 1.NBT.6. Subtract multiples of 10 in the range 10-90 from multiples of 10 in the range 10-90 (positive or zero differences), using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.	Understand place value. 2.NBT.1. Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones. Understand the following as special cases: a. 100 can be thought of as a bundle of ten tens — called a "hundred." b. The numbers 100, 200, 300, 400, 500, 600, 700, 800, 900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones). 2.NBT.2. Count within 1000; skip-count by 2s, 5s, 10s, and 10os. CA 2.NBT.3. Read and write numbers to 1000 using base-ten numerals, number names, and expanded form. 2.NBT.4. Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using >, =, and < symbols to record the results of comparisons. Use place value understanding and properties of operations to add and subtract. 2.NBT.5. Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction. 2.NBT.6. Add up to four two-digit numbers using strategies based on place value and properties of operations. 2.NBT.7. Add and subtract within 1000, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtraction; relate the strategy to a written method. Understand that in adding or subtraction; relate the strategy to a written method. Understand that in adding or subtraction; relate the strategy to a written method. Understand that in adding or subtraction; relate the strategy to a written method. Understand that in adding or subtraction; relate the strategies to make reasonable estimates in problem solving. CA 2.NBT.7.1 Use estimation strategies to make reasonable estimates in problem solving. CA 2.NBT.8. Mentally add 10 or 100 to a given number 100–900, and mentally subtract 10 or 100 from a given number 100–90	Use place value understanding and properties of operations to perform multi-digit arithmetic.4 [4A range of algorithms may be used] 3.NBT.1. Use place value understanding to round whole numbers to the nearest 10 or 100. 3.NBT.2. Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction. 3.NBT.3. Multiply one-digit whole numbers by multiples of 10 in the range 10–90 (e.g., 9 × 80, 5 × 60) using strategies based on place value and properties of operations.	



Number and Operations - Fractions				
Grade 1	Grade 2	Grade 3		
		Grade 3 expectations in this domain are limited to fractions with denominators 2, 3, 4, 6, and 8.		
None	None	 Develop understanding of fractions as numbers. 3.NF.1. Understand a fraction 1/b as the quantity formed by 1 part when a whole is partitioned into b equal parts; understand a fraction a/b as the quantity formed by a parts of size 1/b. 3.NF.2. Understand a fraction as a number on the number line; represent fractions on a number line diagram. a. Represent a fraction 1/b on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts. Recognize that each part has size 1/b and that the endpoint of the part based at 0 locates the number 1/b on the number line. b. Represent a fraction a/b on a number line diagram by marking off a lengths 1/b from 0. Recognize that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line. 3.NF.3. Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size. a. Understand two fractions as equivalent (equal) if they are the same size, or the same point on a number line. b. Recognize and generate simple equivalent fractions, e.g., 1/2 = 2/4, 4/6 = 2/3). Explain why the fractions are equivalent, e.g., by using a visual fraction model. c. Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. Examples: Express 3 in the form 3 = 3/1; recognize that 6/1 = 6; locate 4/4 and 1 at the same point of a number line diagram. d. Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction model. 		

Supporting California Standards

Mathematics Continuum: Grades 1-3



Measurement and Data				
Grade 1	Grade 2	Grade 3		
Measure lengths indirectly and by	Measure and estimate lengths in standard units.	Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects.		
iterating length units.	2.MD.1. Measure the length of an object by selecting and using appropriate tools	3.MD.1 Tell and write time to the nearest minute and measure time intervals in minutes. Solve word problems involving		
1.MD.1. Order three objects by	such as rulers, yardsticks, meter sticks, and measuring tapes.	addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram.		
length; compare the lengths of	2.MD.2. Measure the length of an object twice, using length units of different	3.MD.2. Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and		
two objects indirectly by using	lengths for the two measurements; describe how the two measurements	liters (I).6 Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are		
a third object.	relate to the size of the unit chosen.	given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the		
1.MD.2. Express the length of an	2.MD.3. Estimate lengths using units of inches, feet, centimeters, and meters.	problem. ⁷ [⁶ Excludes compound units such as cm ³ and finding the geometric volume of a container. ⁷ Excludes		
object as a whole number of	2.MD.4. Measure to determine how much longer one object is than another,	multiplicative comparison problems (problems involving notions of "times as much"; see Glossary, Table 2).		
length units, by laying multiple	expressing the length difference in terms of a standard length unit.	Represent and interpret data.		
copies of a shorter object (the	Relate addition and subtraction to length.	3.MD.3. Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one-		
length unit) end to end;	2.MD.5. Use addition and subtraction within 100 to solve word problems involving	and two-step "how many more" and "how many less" problems using information presented in scaled bar graphs. For		
understand that the length	lengths that are given in the same units, e.g., by using drawings (such as	example, draw a bar graph in which each square in the bar graph might represent 5 pets.		
measurement of an object is	drawings of rulers) and equations with a symbol for the unknown number to	3.MD.4. Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show		
the number of same-size	represent the problem.	the data by making a line plot, where the horizontal scale is marked off in appropriate units— whole numbers,		
length units that span it with	2.MD.6. Represent whole numbers as lengths from 0 on a number line diagram	halves, or quarters.		
no gaps or overlaps. Limit to	with equally spaced points corresponding to the numbers 0, 1, 2,, and	Geometric measurement: understand concepts of area and relate area to multiplication and to addition.		
contexts where the object	represent whole-number sums and differences within 100 on a number line	3.MD.5. Recognize area as an attribute of plane figures and understand concepts of area measurement.		
being measured is spanned	diagram.	a. A square with side length 1 unit, called "a unit square," is said to have "one square unit" of area, and can be used		
by a whole number of length	Work with time and money.	to measure area.		
units with no gaps or overlaps.	2.MD.7. Tell and write time from analog and digital clocks to the nearest five	b. A plane figure which can be covered without gaps or overlaps by <i>n</i> unit squares is said to have an area of <i>n</i>		
Tell and write time.	minutes, using a.m. and p.m. Know relationships of time (e.g., minutes	square units.		
1.MD.3. Tell and write time in hours	in an hour, days in a month, weeks in a year). CA	3.MD.6. Measure areas by counting unit squares (square cm, square m, square in, square ft, and improvised units).		
and half-hours using analog	2.MD.8. Solve word problems involving dollar bills, quarters, dimes, nickels, and	3.MD.7. Relate area to the operations of multiplication and addition.		
and digital clocks.	pennies, using \$ and ¢ symbols appropriately. Example: If you have 2	a. Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as		
Represent and interpret data.	dimes and 3 pennies, how many cents do you have?	would be found by multiplying the side lengths.		
1.MD.4. Organize, represent, and	Represent and interpret data.	b. Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real		
interpret data with up to three	2.MD.9. Generate measurement data by measuring lengths of several objects to	world and mathematical problems, and represent whole-number products as rectangular areas in mathematical		
categories; ask and answer	the nearest whole unit, or by making repeated measurements of the same	reasoning.		
questions about the total	object. Show the measurements by making a line plot, where the horizontal	c. Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths a and $b + c$ is		
number of data points, how	scale is marked off in whole-number units.	the sum of $a \times b$ and $a \times c$. Use area models to represent the distributive property in mathematical reasoning.		
many in each category, and	2.MD.10. Draw a picture graph and a bar graph (with single-unit scale) to represent	d. Recognize area as additive. Find areas of rectilinear figures by decomposing them into non-overlapping		
how many more or less are in	a data set with up to four categories. Solve simple put-together, take-apart,	rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real world		
one category than in another.	and compare problems ⁴ using information presented in a bar graph. { ⁴ See	problems.		
	Glossary, Table 1.}	Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and		
		area measures.		
		3.MD.8. Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given		
		the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different		
		areas or with the same area and different perimeters.		



Geometry					
Grade 1	Grade 2	Grade 3			
Reason with shapes and their attributes.	Reason with shapes and their attributes.	Reason with shapes and their attributes.			
 Distinguish between defining attributes (e.g., triangles are closed and three-sided) versus non-defining attributes (e.g., color, orientation, overall size); build and draw shapes to possess defining attributes. Compose two-dimensional shapes (rectangles, squares, trapezoids, triangles, half-circles, and quarter-circles) or three-dimensional shapes (cubes, right rectangular prisms, right circular cones, and right circular cylinders) to create a composite shape, and compose new shapes from the composite shape.⁴ {⁴ Students do not need to learn formal names such as "right rectangular prism."} Partition circles and rectangles into two and four equal shares, describe the shares using the words halves, fourths, and quarters, and use the phrases half of, fourth of, and quarter of. Describe the whole as two of, or four of the shares. Understand for these examples that decomposing into 	 2.G.1. Recognize and draw shapes having specified attributes, such as a given number of angles or a given number of equal faces. Identify triangles, quadrilaterals, pentagons, hexagons, and cubes. Sizes are compared directly or visually, not compared by measuring. 2.G.2. Partition a rectangle into rows and columns of same-size squares and count to find the total number of them. 2.G.3. Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, half of, a third of, etc., and describe the whole as two halves, three thirds, four fourths. Recognize that equal shares of identical wholes need not have the same shape. 	 3.G.1. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories. 3.G.2. Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. For example, partition a shape into 4 parts with equal area, and describe the area of each part as 1/4 of the area of the shape. 			

Standards for Mathematical Practice (K-12)

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others
- 4. Model with mathematics

- 5. Use appropriate tools strategically
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.